

# Strings, Membranes and Quantum foam

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# *Einstein's Universe*



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# *Post-Einstein's Universe*



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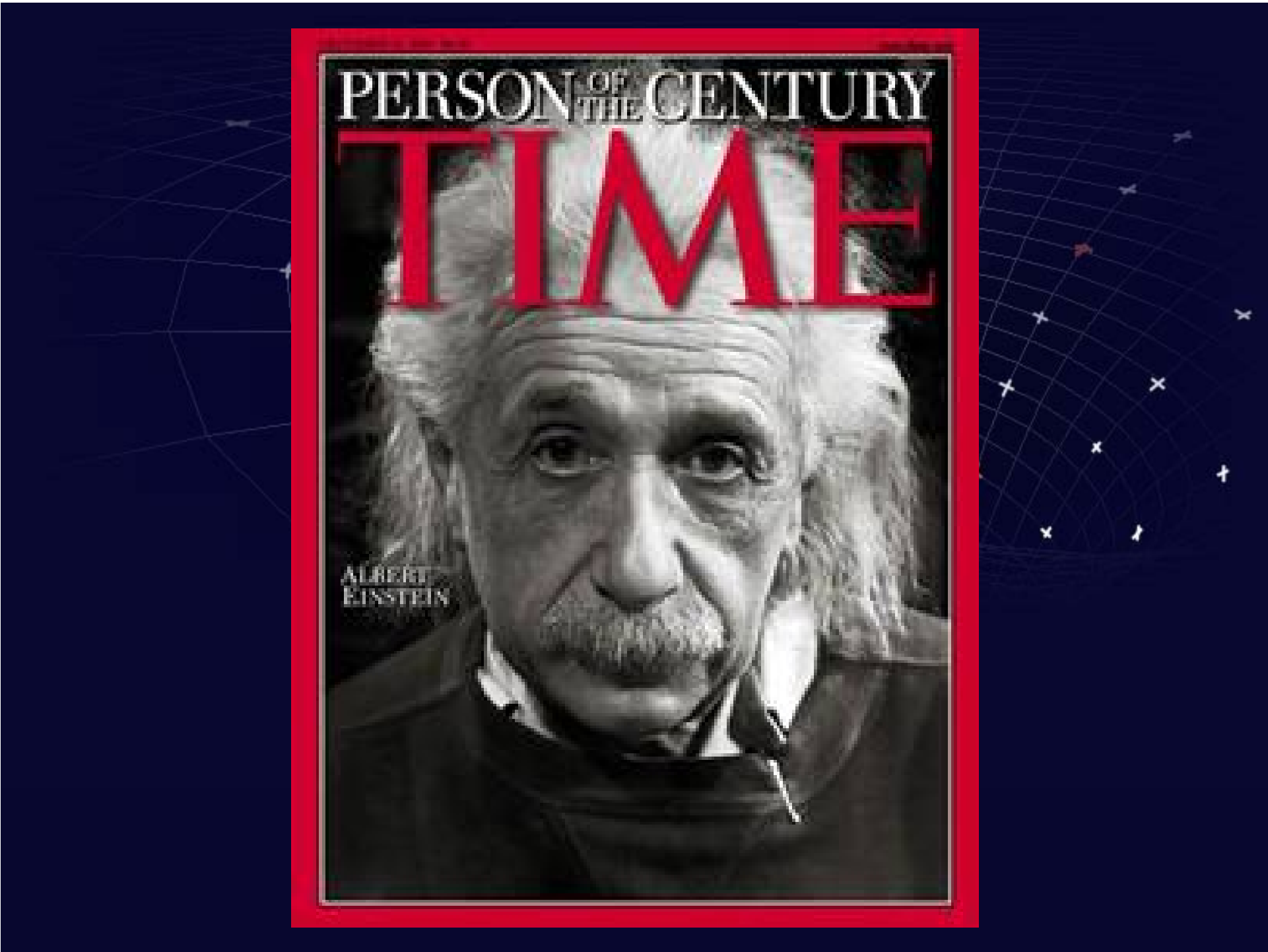
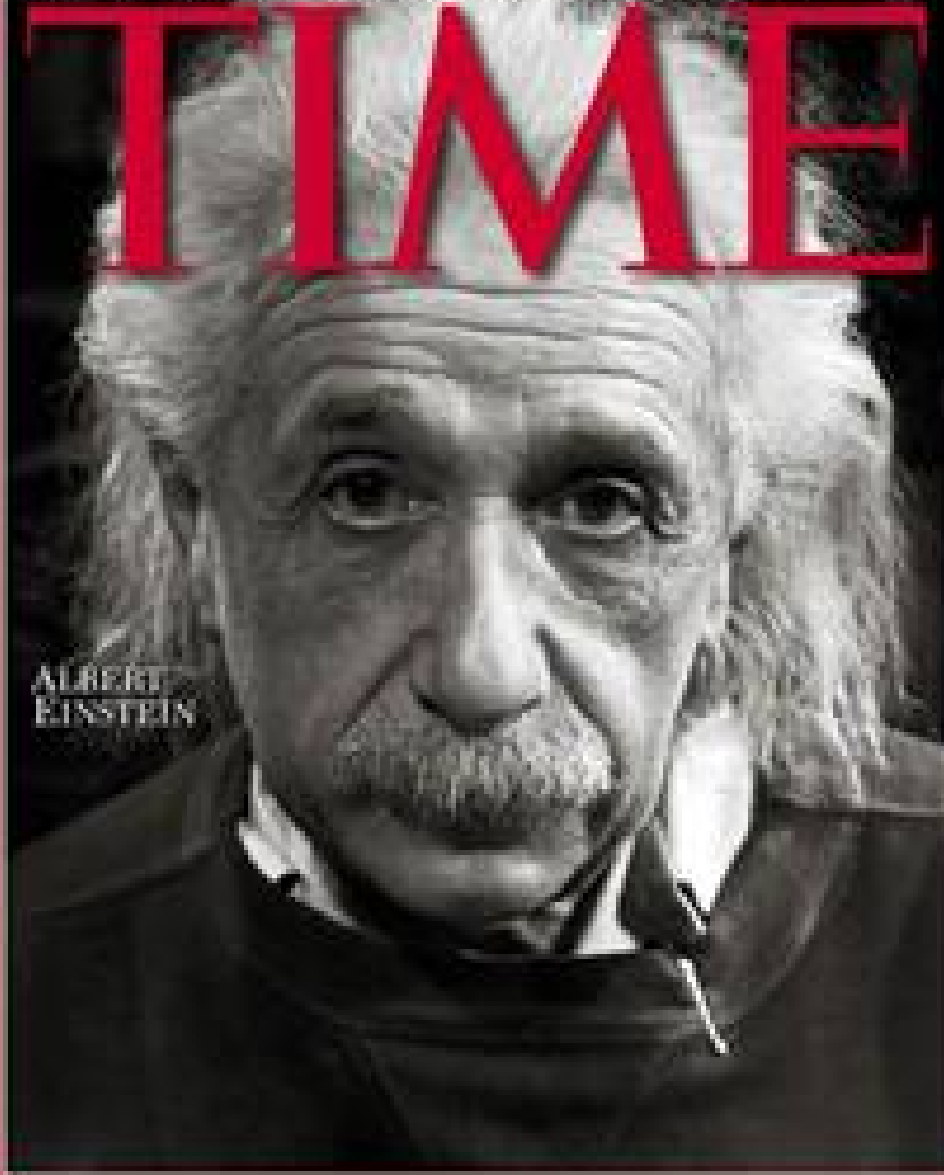
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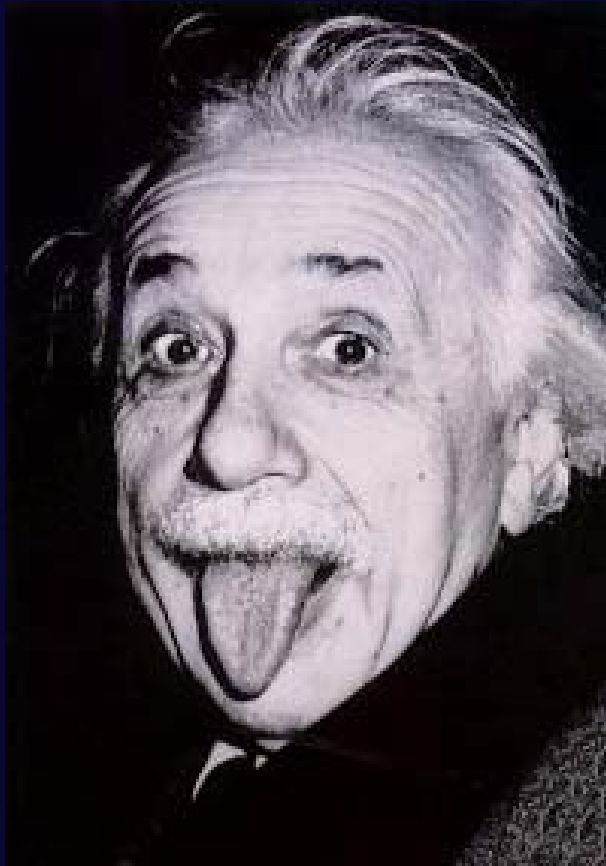
PERSON OF THE CENTURY

TIME

ALBERT  
EINSTEIN







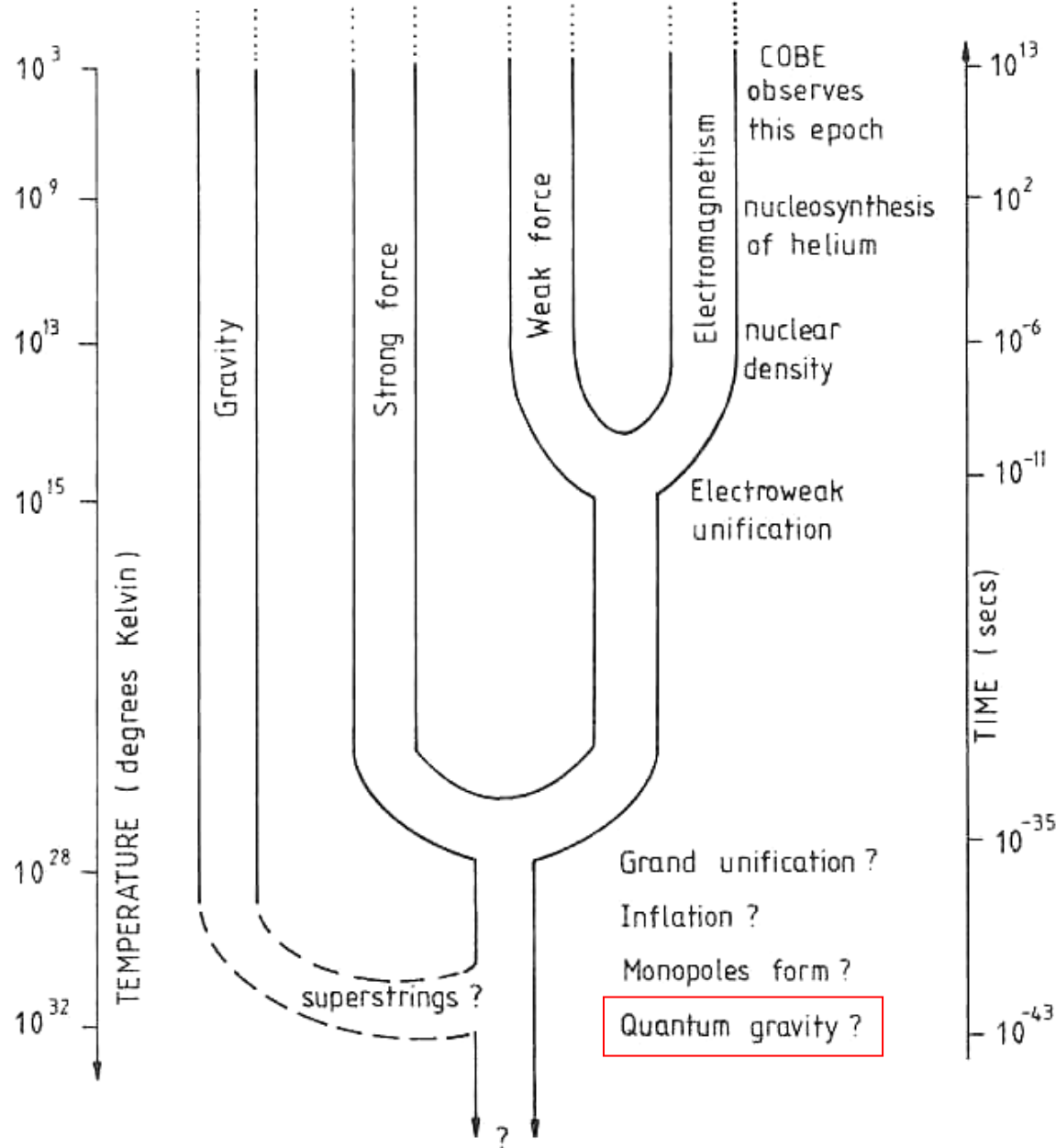
"The generalisation  
of the theory of  
gravitation has  
occupied me  
unceasingly since  
1916"

Einstein, 1953



# Space: The Final Frontier

↑ Present Day ↑



Big Bang



# Standard Model of FUNDAMENTAL PARTICLES AND INTERACTIONS

The Standard Model summarizes the current knowledge in Particle Physics. It is the quantum theory that includes the theory of strong interactions (Quantum Chromodynamics or QCD) and the unified theory of weak and electromagnetic interactions (electroweak). Gravity is included on this chart because it is one of the fundamental interactions even though not part of the "Standard Model."

## FERMIONS

matter constituents  
spin = 1/2, 3/2, 5/2, ...

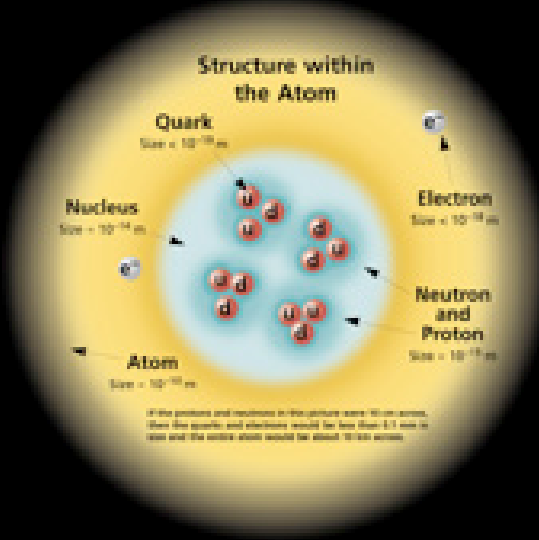
Leptons spin = 1/2			
Flavor	Mass GeV/c <sup>2</sup>	Electric charge	Spin
$\nu_e$ electron neutrino	<1 × 10 <sup>-6</sup>	0	1/2
$e^-$ electron	0.000511	-1	1/2
$\nu_\mu$ muon neutrino	<0.0002	0	1/2
$\mu^-$ muon	0.106	-1	1/2
$\nu_\tau$ tau neutrino	<0.02	0	1/2
$\tau^-$ tau	1.7771	-1	1/2

Quarks spin = 1/2			
Flavor	Approx. Mass GeV/c <sup>2</sup>	Electric charge	Spin
$u$ up	0.003	2/3	1/2
$d$ down	0.006	-1/3	1/2
$c$ charm	1.3	2/3	1/2
$s$ strange	0.1	-1/3	1/2
$t$ top	175	2/3	1/2
$b$ bottom	4.3	-1/3	1/2

**Spin** is the intrinsic angular momentum of particles. Spin is given in units of  $\hbar$ , which is the quantum unit of angular momentum, where  $\hbar = 6.58 \times 10^{-16}$  GeV s =  $1.05 \times 10^{-34}$  J s.

**Electric charges** are given in units of the proton's charge. In SI units the electric charge of the proton is  $1.60 \times 10^{-19}$  coulombs.

The **energy** unit of particle physics is the electronvolt (eV), the energy gained by one electron in crossing a potential difference of one volt. Masses are given in GeV/c<sup>2</sup> (remember  $E = mc^2$ ), where 1 GeV =  $10^9$  eV =  $1.60 \times 10^{-10}$  joules. The mass of the proton is  $0.938$  GeV/c<sup>2</sup> =  $1.67 \times 10^{-27}$  kg.



## BOSONS

force carriers  
spin = 0, 1, 2, ...

Unified Electroweak spin = 1			
Name	Mass GeV/c <sup>2</sup>	Electric charge	Spin
$\gamma$ photon	0	0	1
$W^-$	80.4	-1	1
$W^+$	80.4	+1	1
$Z^0$	91.187	0	1

Strong (color) spin = 1			
Name	Mass GeV/c <sup>2</sup>	Electric charge	Spin
$g$ gluon	0	0	1

**Color Charge**  
Each quark carries one of three types of "flavor charge," also called "color charge." These charges have nothing to do with the colors of visible light. There are eight possible types of color charge for gluons. Just as electric charges interact by exchanging photons, so strong interactions color-charged particles interact by exchanging gluons. Leptons, photons and  $Z^0$  and  $W^{\pm}$  bosons have no strong interactions and hence no color charge.

**Quarks Confined in Mesons and Baryons**  
One cannot isolate quarks and gluons; they are confined in color-neutral particles called **hadrons**. This confinement (binding) results from multiple exchanges of gluons among the color-charged constituents. As color-charged particles (quarks and gluons) move apart, the energy in the color force field between them increases. This energy eventually is converted into additional quark antiquark pairs (see figure below). The quarks and antiquarks then combine into hadrons; these are the particles seen to emerge. Two types of hadrons have been obtained in nature: **mesons** ( $q\bar{q}$ ) and **baryons** ( $qqq$ ).

**Residual Strong Interaction**  
The strong binding of color-neutral protons and neutrons to form nuclei is due to residual strong interactions between their color-charged constituents. It is similar to the residual electrostatic interaction that binds electrically neutral atoms to form molecules. It can also be viewed as the exchange of mesons between the hadrons.

## PROPERTIES OF THE INTERACTIONS

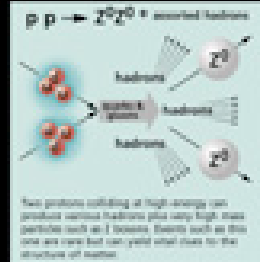
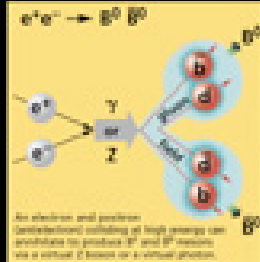
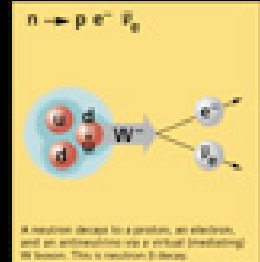
Baryons $qqq$ and Antibaryons $\bar{q}\bar{q}\bar{q}$					
Baryons are fermionic hadrons. There are about 120 types of baryons.					
Symbol	Name	Quark content	Electric charge	Mass GeV/c <sup>2</sup>	Spin
$p$	proton	$uud$	1	0.938	1/2
$\bar{p}$	anti-proton	$\bar{u}\bar{u}\bar{d}$	-1	0.938	1/2
$n$	neutron	$udd$	0	0.940	1/2
$\Lambda$	lambda	$uds$	0	1.116	1/2
$\bar{\Lambda}$	anti-lambda	$\bar{s}\bar{s}\bar{u}$	-1	1.682	1/2

Property \ Interaction	Gravitational	Weak (Electroweak)		Electromagnetic		Strong	
		Fundamental	Residual	Fundamental	Residual		
<b>Acts on:</b>	Mass - Energy	Flavor	Electric Charge	Color Charge	See Residual Strong Interaction table		
<b>Particles experiencing:</b>	All	Quarks, Leptons	Electrically charged	Quarks, Gluons	Hadrons		
<b>Particles mediating:</b>	Graviton (not yet observed)	$W^+ W^- Z^0$	$\gamma$	Gluons	Mesons		
<b>Strength relative to electromagnetism for two quarks at:</b>	$10^{-41}$ $10^{-49}$ $10^{-36}$	0.6 $10^{-4}$ $10^{-7}$	1 1 1	25 60 Not applicable to hadrons	Not applicable to quarks 20		

Mesons $q\bar{q}$					
Mesons are bosonic hadrons. There are about 140 types of mesons.					
Symbol	Name	Quark content	Electric charge	Mass GeV/c <sup>2</sup>	Spin
$\pi^+$	pion	$u\bar{d}$	+1	0.140	0
$K^+$	kaon	$u\bar{s}$	+1	0.494	0
$\rho^+$	rho	$u\bar{d}$	+1	0.770	1
$B^0$	B meson	$d\bar{b}$	0	5.279	0
$\eta_c$	charmonium	$c\bar{c}$	0	2.980	0

**Matter and Antimatter**  
For every particle type there is a corresponding antiparticle type, denoted by a bar over the particle symbol (unless a  $+$  or  $-$  charge is shown). Particle and antiparticle have identical mass and spin but opposite charges. Some electrically neutral bosons (e.g.,  $Z^0$ ,  $\gamma$ , and  $\eta_c$ ,  $\pi^0$ , but not  $K^0$  or  $B^0$ ) are their own antiparticles.

**Figures**  
These diagrams are an artist's conception of physical processes. They are not exact and have no meaningful scale. Green shaded areas represent the cloud of gluons in the gluon field, and red lines the quark paths.

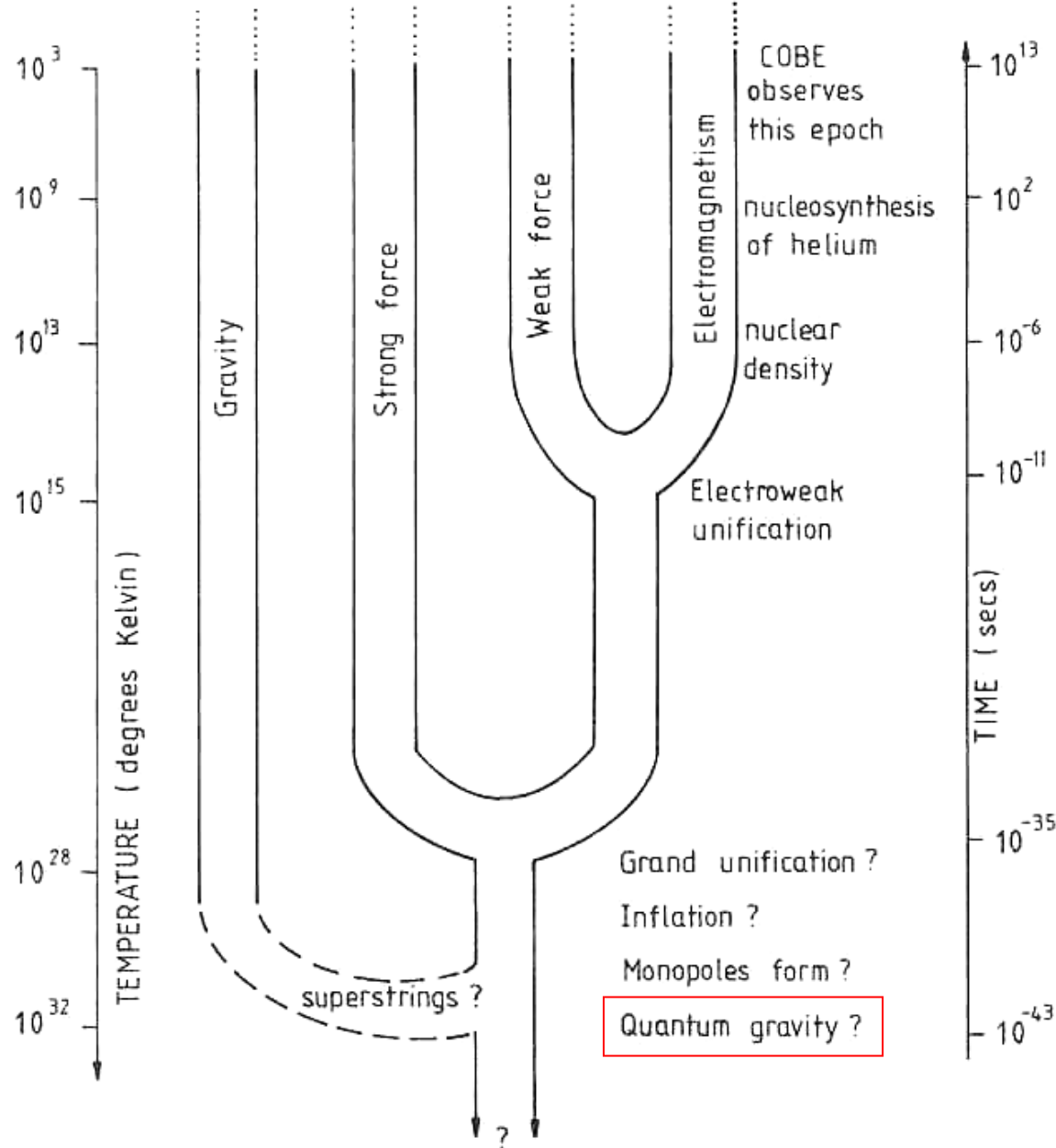


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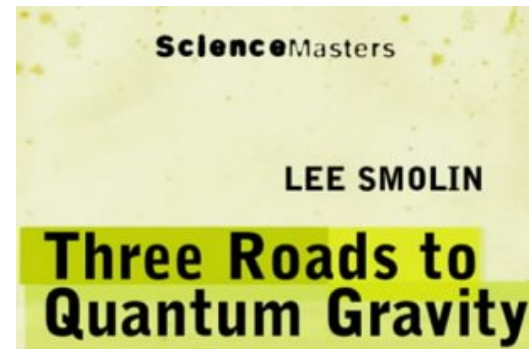
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↑ Present Day ↑



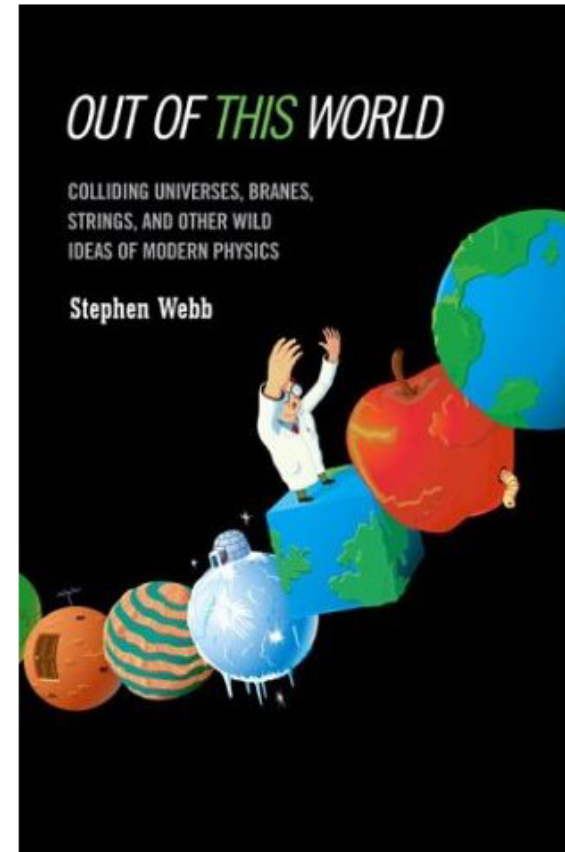
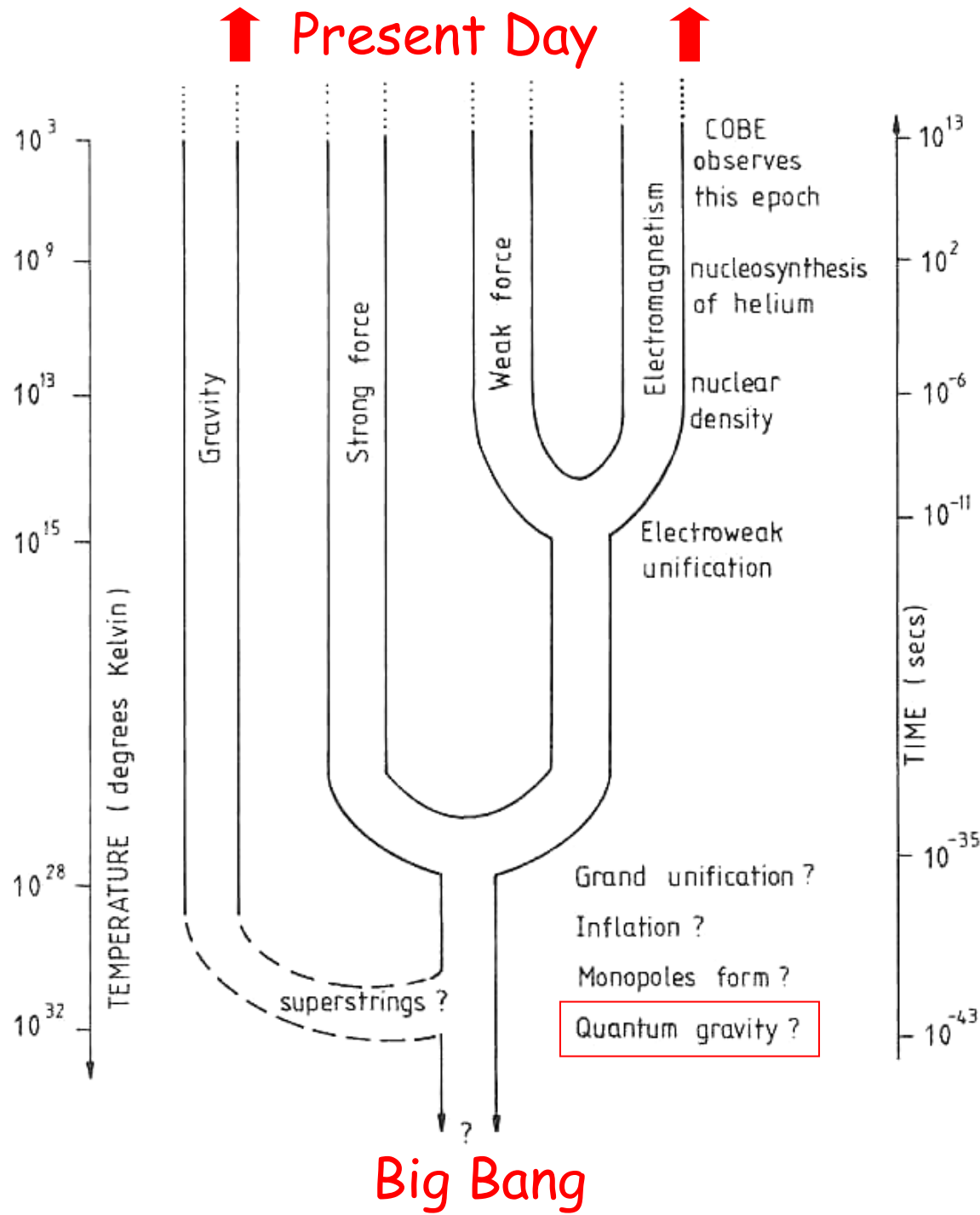
Big Bang



A NEW UNDERSTANDING OF SPACE, TIME AND THE UNIVERSE



"Smolin is a deep and original thinker" Paul Davies



# What should a theory of Quantum Gravity encapsulate?...

- General Relativity:

*No absolute background of space and time*

- Quantum Physics:

*On small scales, things are 'fuzzy'*

# Classical Physics:

## *All the World's A Stage*

- Newton's physics assumes absolute space and time, for all observers.

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# Classical Physics: *All the World's A Stage*

- Newton's physics assumes absolute space and time, for all observers.
- Working out how things look to different observers follows simple rules, in different *reference frames*



Viewed from the red car's rest frame

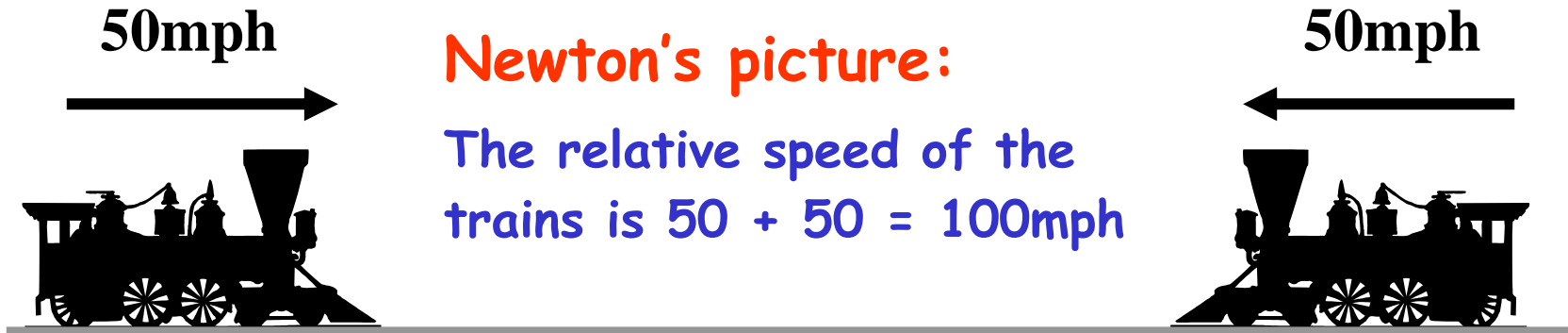
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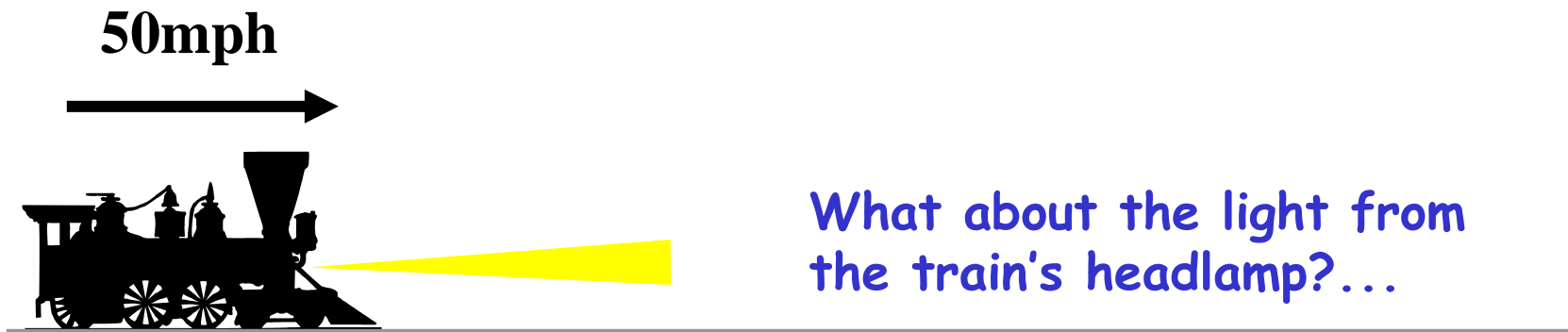
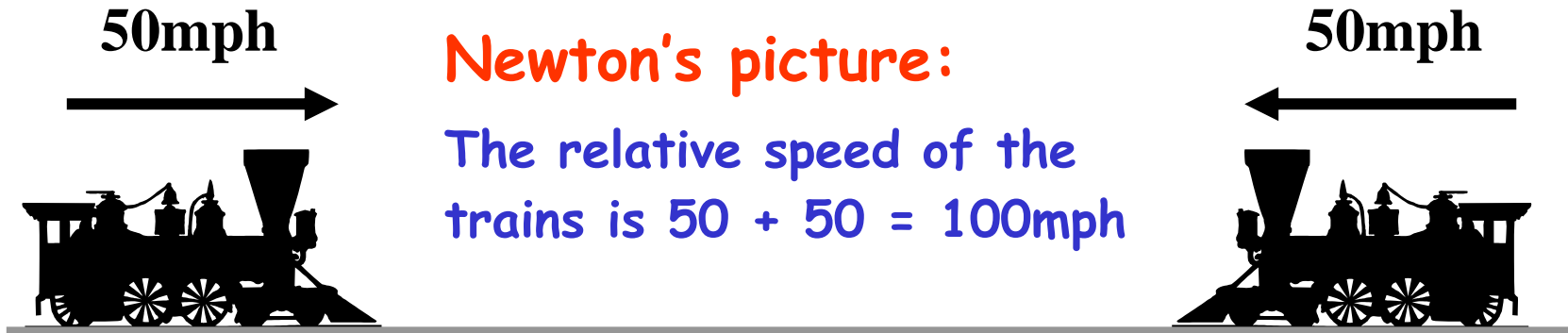
Viewed from the blue car's rest frame





**Newton's picture:**

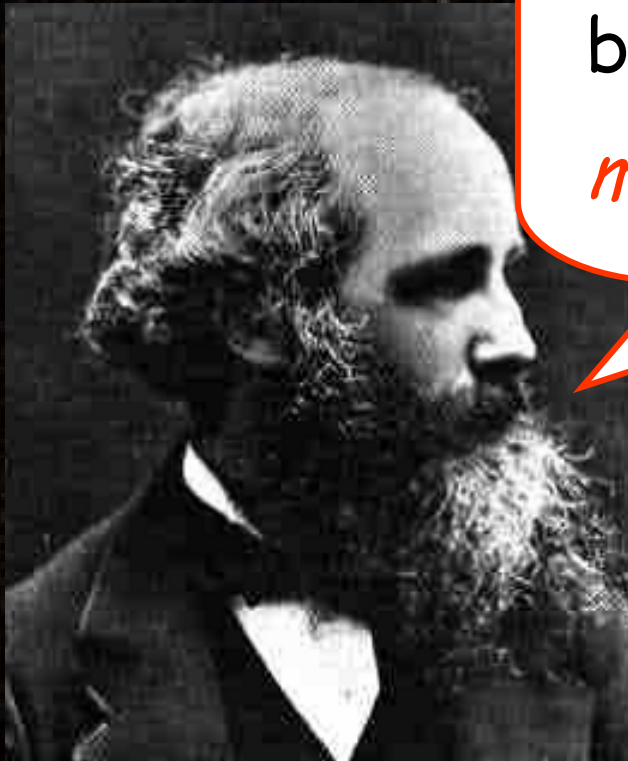
The relative speed of the trains is  $50 + 50 = 100\text{mph}$



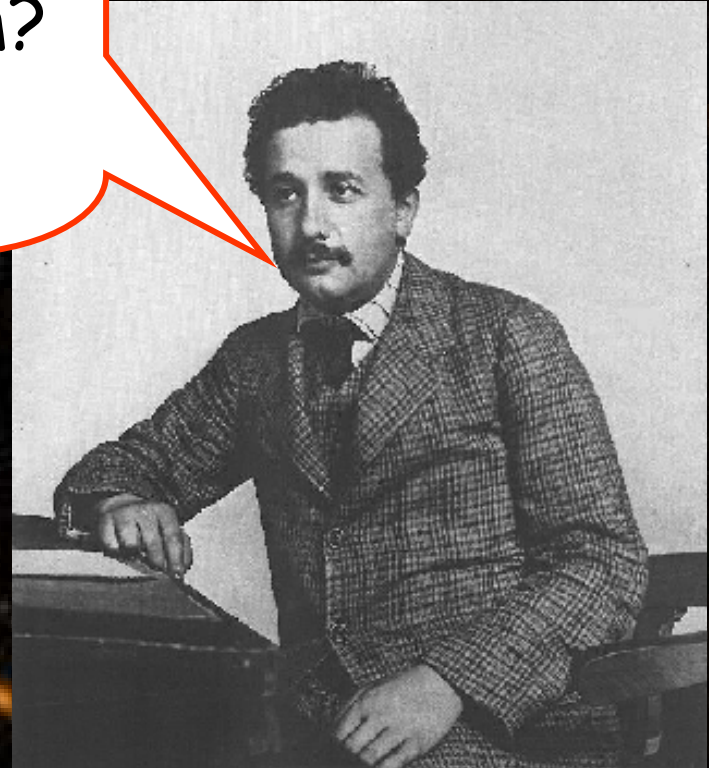
# Classical Physics:

## *James Clerk Maxwell's theory of light*

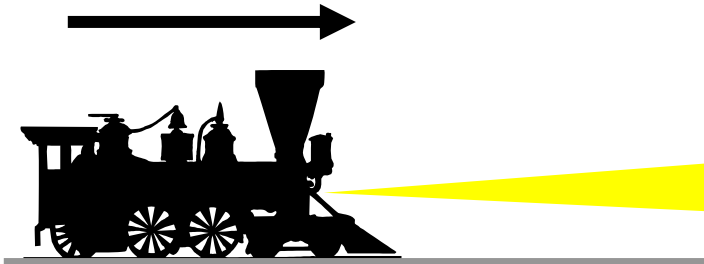
Light is a *wave* caused by varying *electric* and *magnetic* fields



But what if I travelled  
*alongside* a light beam?  
Would it still wave?

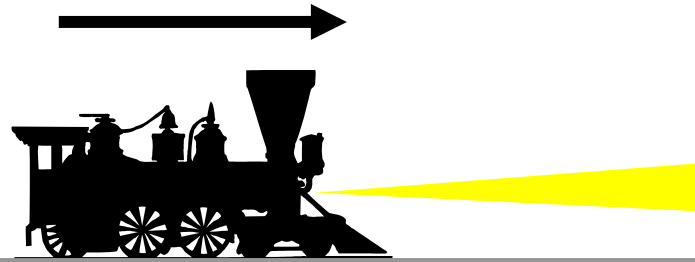


50mph



In Einstein's relativity, the speed of light is *unchanged* by the motion of the train

50mph



In Einstein's relativity, the speed of light is *unchanged* by the motion of the train

ON THE ELECTRODYNAMICS OF MOVING BODIES

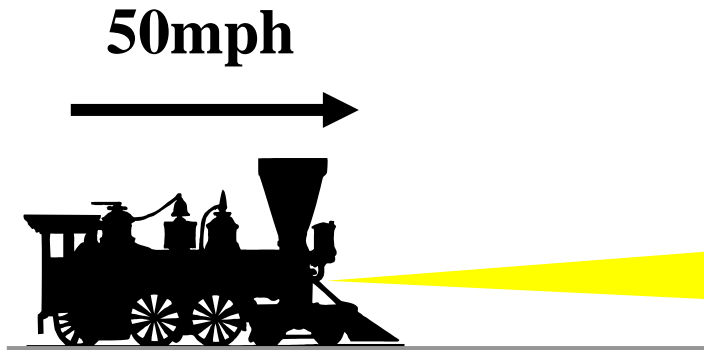
BY A. EINSTEIN

June 30, 1905

It is known that Maxwell's electrodynamics—as usually understood at the present time—when applied to moving bodies, leads to asymmetries which do not appear to be inherent in the phenomena. Take, for example, the reciprocal electrodynamic action of a magnet and a conductor. The observable phenomenon here depends only on the relative motion of the conductor and the magnet, whereas the customary view draws a sharp distinction between the two cases in which either the one or the other of these bodies is in motion. For if the magnet is in motion and the conductor at rest, there arises in the neighbourhood of the magnet an electric field with a certain definite energy, producing a current at the places where parts of the conductor are situated. But if the magnet is stationary and the conductor in motion, no electric field arises in the neighbourhood of the magnet. In the conductor, however, we find an electromotive force, to which in itself there is no corresponding energy, but which gives rise—assuming equality of relative motion in the two cases discussed—to electric currents of the same path and intensity as those produced by the electric forces in the former case.

Examples of this sort, together with the unsuccessful attempts to discover any motion of the earth relatively to the "light medium," suggest that the phenomena of electrodynamics as well as of mechanics possess no properties corresponding to the idea of absolute rest. They suggest rather that, as has already been shown to the first order of small quantities, the same laws of electrodynamics and optics will be valid for all frames of reference for which the equations of mechanics hold good.<sup>1</sup> We will raise this conjecture (the purport of which will hereafter be called the "Principle of Relativity") to the status of a postulate, and also introduce another postulate, which is only apparently irreconcilable with the former, namely, that light is always propagated in empty space with a definite velocity  $c$  which is independent of the state of motion of the emitting body. These two postulates suffice for the attainment of a simple and consistent theory of the electrodynamics of moving bodies based on Maxwell's theory for stationary bodies. The introduction of a "luminiferous ether" will prove to be superfluous inasmuch as the view here to be developed will not require an "absolutely stationary space" provided with special properties, nor

<sup>1</sup>The preceding memoir by Lorentz was not at this time known to the author.



In Einstein's relativity, the speed of light is *unchanged* by the motion of the train

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BY A. EINSTEIN

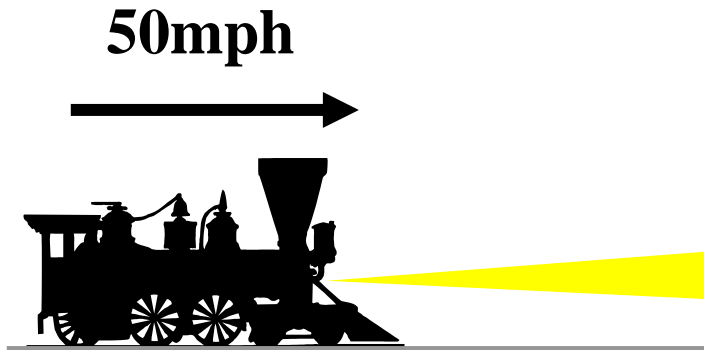
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➤ Measurements of space and time are *relative* and depend on our motion



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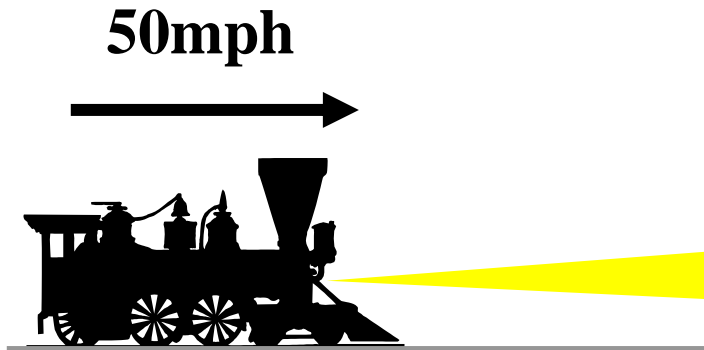
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- Measurements of space and time are *relative* and depend on our motion

"The only reason for time is so that everything doesn't happen at once."





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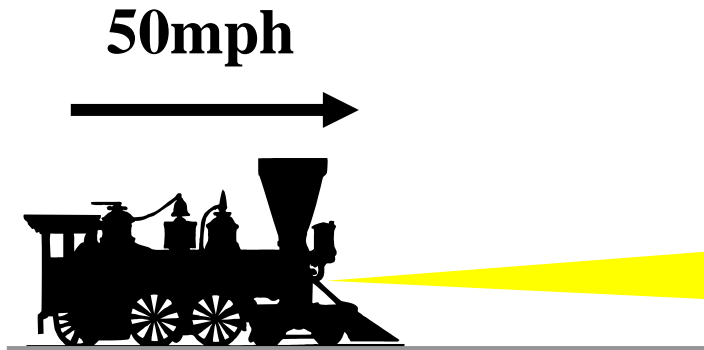
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"Put your hand on a hot stove for a minute, and it seems like an hour. Sit with a pretty girl for an hour and it seems like a minute. THAT'S relativity."



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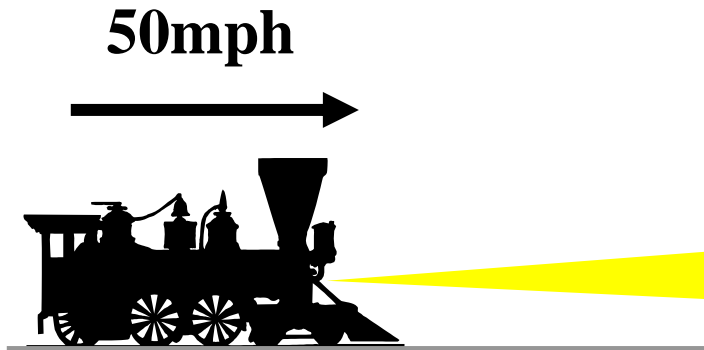
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- Measurements of space and time are *relative* and depend on our motion
- Unified *spacetime* - only measurements of the *spacetime* interval are invariant



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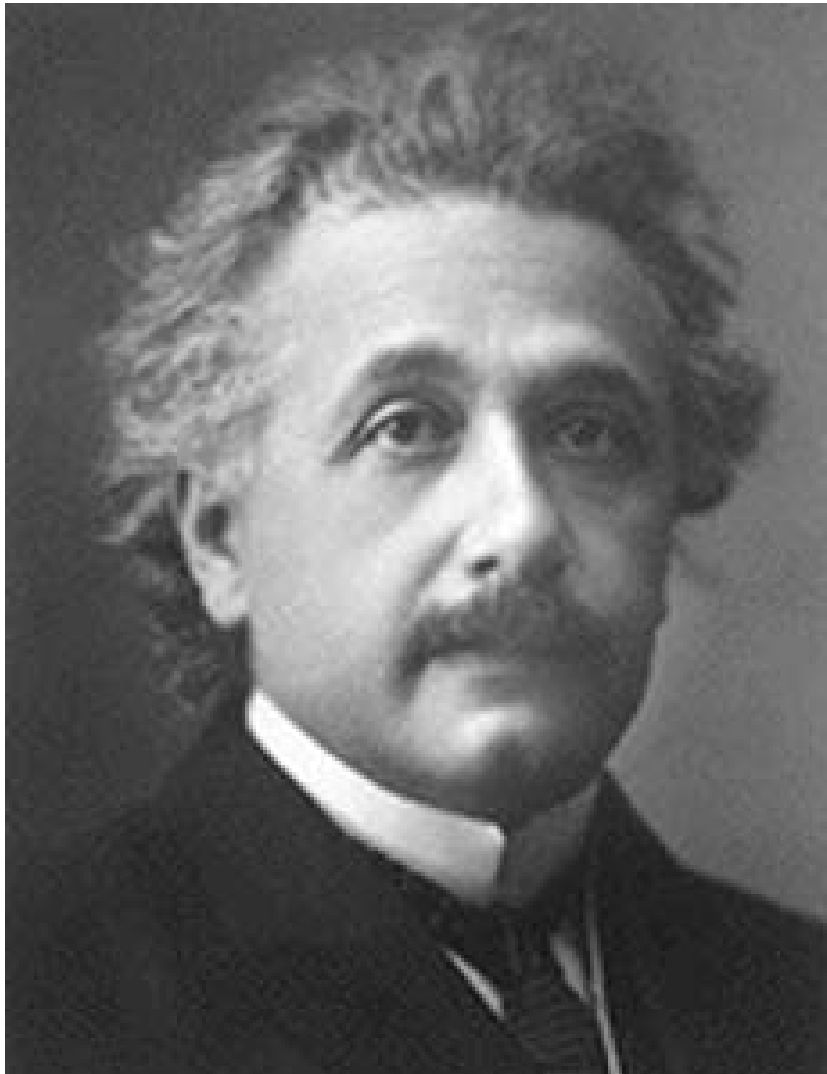
June 30, 1905

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Examples of this sort, together with the unsuccessful attempts to discover any motion of the earth relatively to the "light medium," suggest that the phenomena of electrodynamics as well as of mechanics possess no properties corresponding to the idea of absolute rest. They suggest rather that, as has already been shown to the first order of small quantities, the same laws of electrodynamics and optics will be valid for all frames of reference for which the equations of mechanics hold good.<sup>1</sup> We will raise this conjecture (the purport of which will hereafter be called the "Principle of Relativity") to the status of a postulate, and also introduce another postulate, which is only apparently irreconcilable with the former, namely, that light is always propagated in empty space with a definite velocity  $c$  which is independent of the state of motion of the emitting body. These two postulates suffice for the attainment of a simple and consistent theory of the electrodynamics of moving bodies based on Maxwell's theory for stationary bodies. The introduction of a "luminiferous ether" will prove to be superfluous inasmuch as the view here to be developed will not require an "absolutely stationary space" provided with special properties, nor

<sup>1</sup>The preceding memoir by Lorentz was not at this time known to the author.

- Measurements of space and time are *relative* and depend on our motion
- Unified *spacetime* - only measurements of the *spacetime* interval are invariant
- Equivalence of *matter* and *energy*



1916.

Nr 7.

## ANNALEN DER PHYSIK.

VIERTE FOLGE. BAND 49.

---

1. *Die Grundlage  
der allgemeinen Relativitätstheorie;*  
von *A. Einstein.*

---

Die im nachfolgenden dargelegte Theorie bildet die denkbar weitgehendste Verallgemeinerung der heute allgemein als „Relativitätstheorie“ bezeichneten Theorie; die letztere nenne ich im folgenden zur Unterscheidung von der ersteren „spezielle Relativitätstheorie“ und setze sie als bekannt voraus. Die Verallgemeinerung der Relativitätstheorie wurde sehr erleichtert durch die Gestalt, welche der speziellen Relativitätstheorie durch Minkowski gegeben wurde, welcher Mathematiker zuerst die formale Gleichwertigkeit der räumlichen Koordinaten und der Zeitkoordinate klar erkannte und für den Aufbau der Theorie nutzbar machte. Die für die allgemeine Relativitätstheorie nötigen mathematischen Hilfsmittel lagen festig bereit in dem „absoluten Differentialkalkül“, welcher auf den Forschungen von Gauss, Riemann und Christoffel über nichteuklidische Mannigfaltigkeiten ruht und bereits auf Probleme der theoretischen Physik angewendet wurde. Ich habe im Abschnitt B der vorliegenden Abhandlung alle für uns nötigen, bei dem Physiker nicht als bekannt vorauszusetzenden mathematischen Hilfsmittel in möglichst einfacher und durchsichtiger Weise entwickelt, so daß ein Studium mathematischer Literatur für das Verständnis der vorliegenden Abhandlung nicht erforderlich ist. Endlich sei an dieser Stelle dankbar meines Freundes, des Mathematikers Grossmann, gedacht, der mir durch seine Hilfe nicht nur das Studium der einschlägigen mathematischen Literatur ersparte, sondern mich auch beim Suchen nach den Feldgleichungen der Gravitation unterstützte.

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1916.

Nr 7.

## ANNALEN DER PHYSIK.

### VIERTE FOLGE. BAND 49.

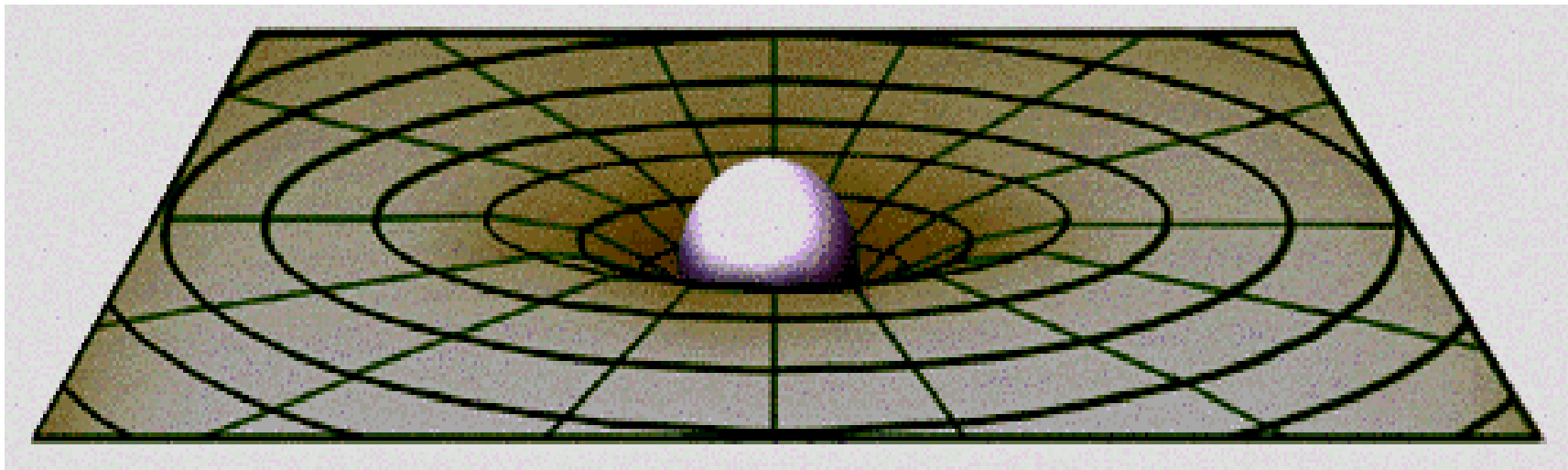
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# Gravity in Einstein's Universe



**"Spacetime tells matter  
how to move, and  
matter tells spacetime  
how to curve"**



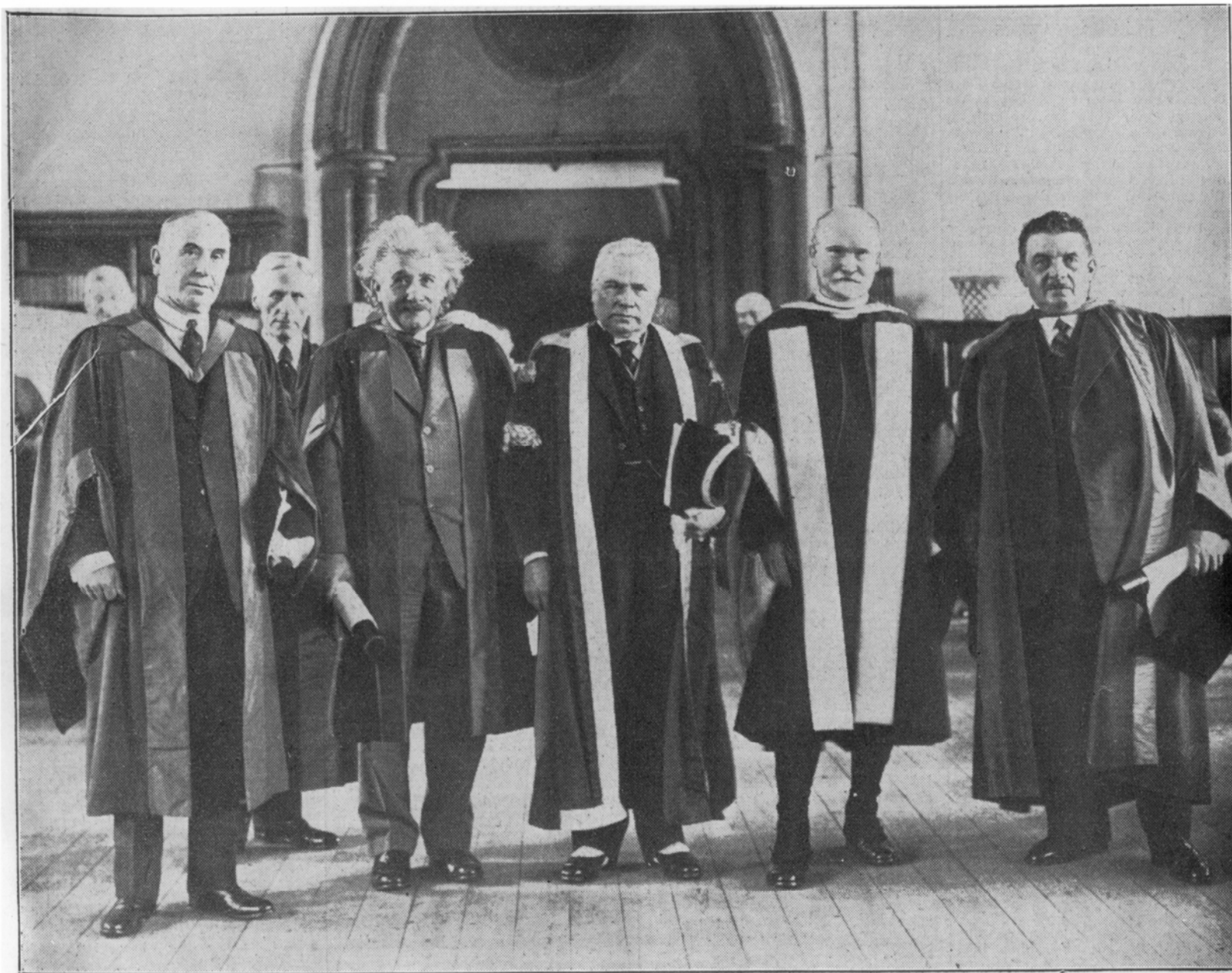


Colleague: *"Professor Eddington, you must be one of only three persons in the world who understand relativity!"*

Eddington: *"oh, I don't know..."*

Colleague: *"Don't be modest Eddington."*

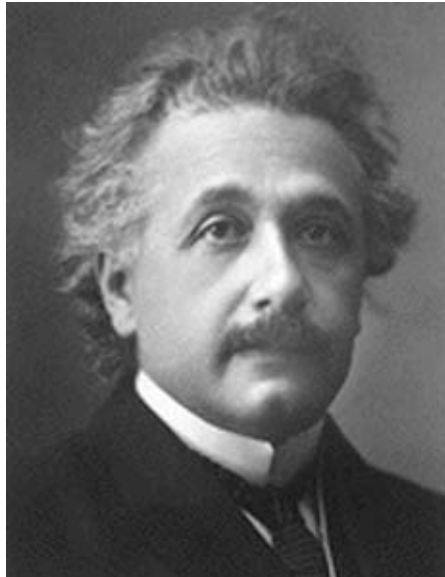
Eddington: *"On the contrary, I am trying to think who the third person is."*



A group of some of the honorary graduates taken after the ceremony in the Butø Hall of Glasgow University yesterday. Left to right—The Right Hon. Sir Robert S. Horne; Emeritus Professor William Blair-Bell, University of Liverpool; Professor Albert Einstein; Principal Sir Robert S. Rait; the Archbishop of Armagh and Primate of All Ireland; and M. Edouard Herriot, former Prime Minister of France.

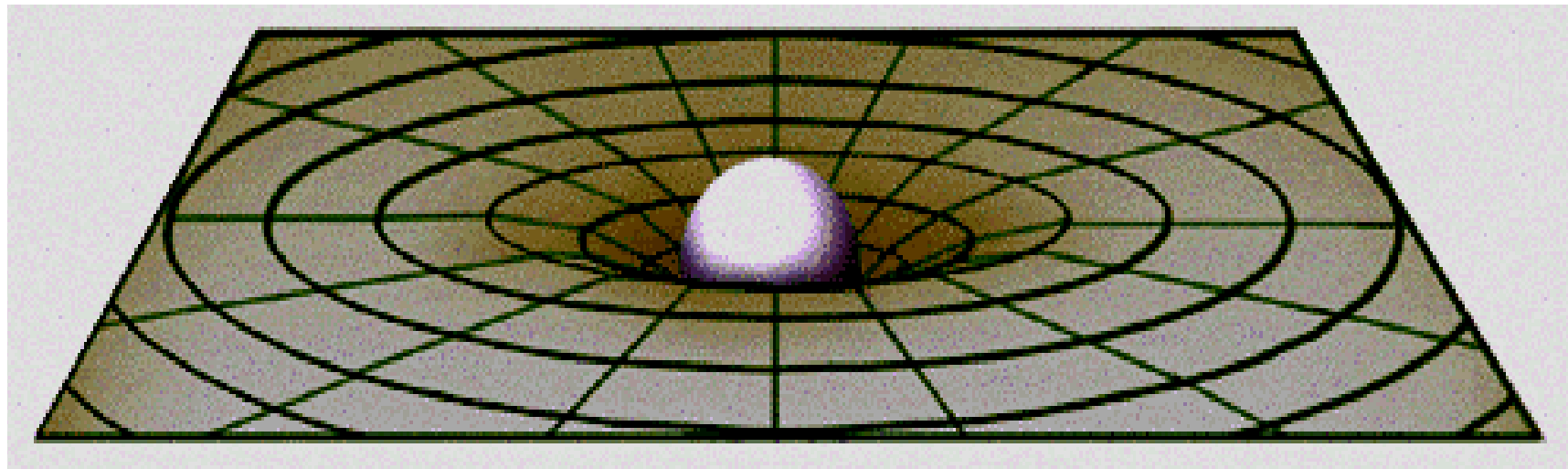


# Gravity in Einstein's Universe

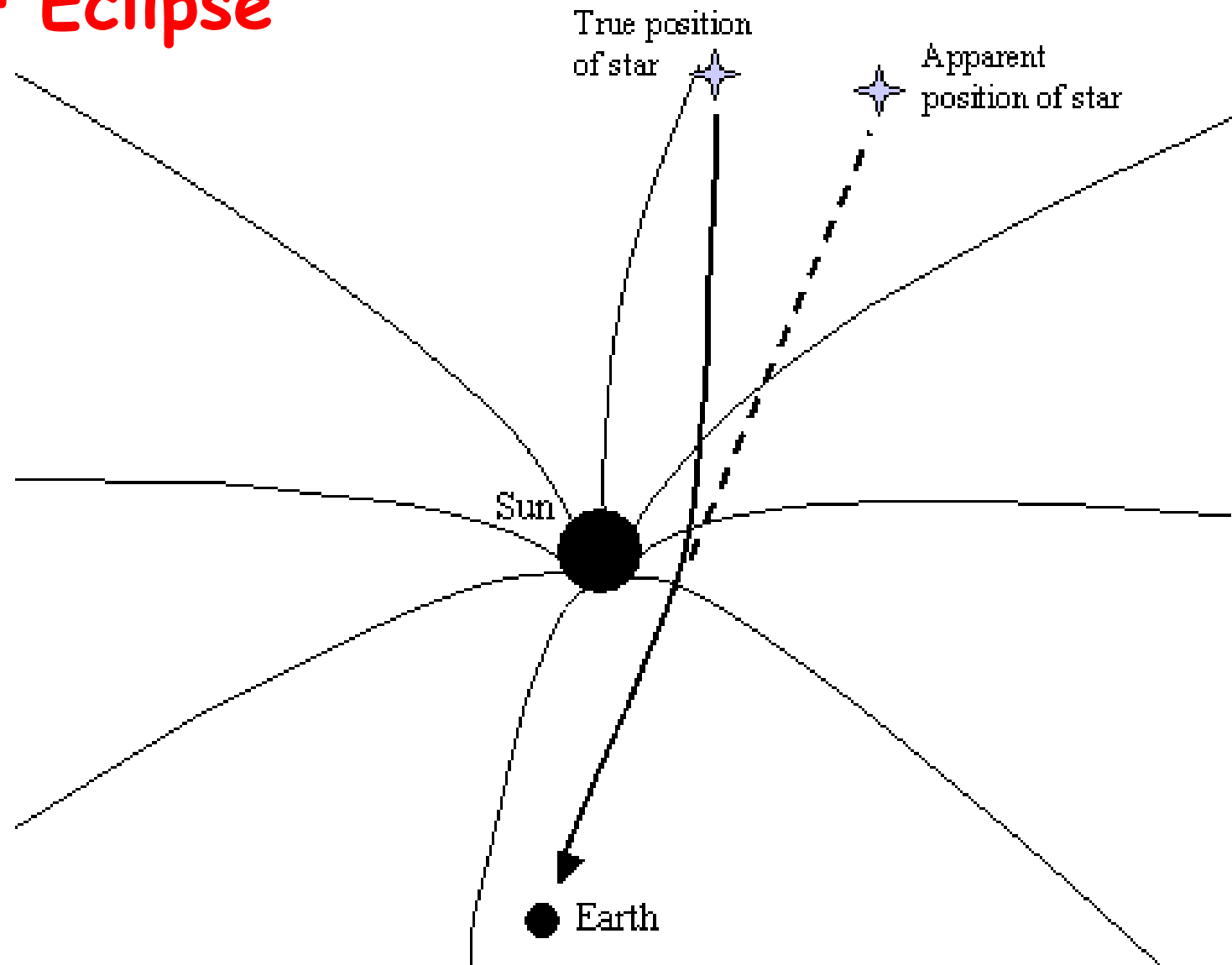


As light passes close to a star its path is bent by the curved spacetime

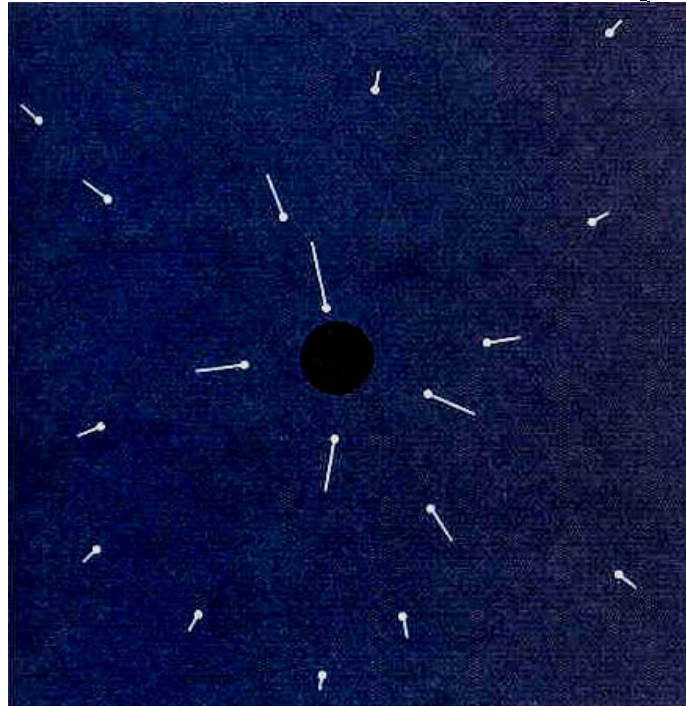
*Gravitational Lensing*



# We can see this during a Solar Eclipse



# We can see this during a Solar Eclipse



True position  
of star

Apparent  
position of star

In 1919 Eddington's expedition to the Southern Hemisphere confirmed Einstein's theory

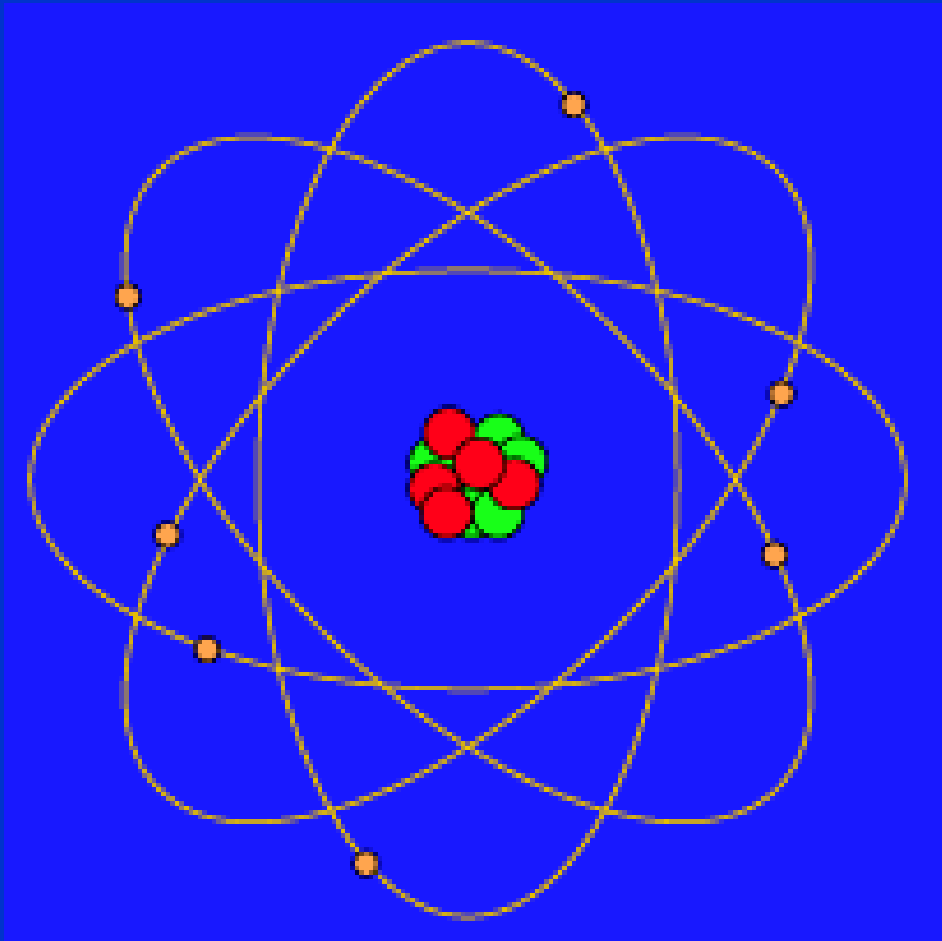
● Earth



*“He was one of the finest people I have ever known....but he didn’t really understand physics. During the eclipse...he stayed up all night to see if it would confirm the bending of light by the gravitational field. If he had really understood general relativity, he would have gone to bed the way I did.”*



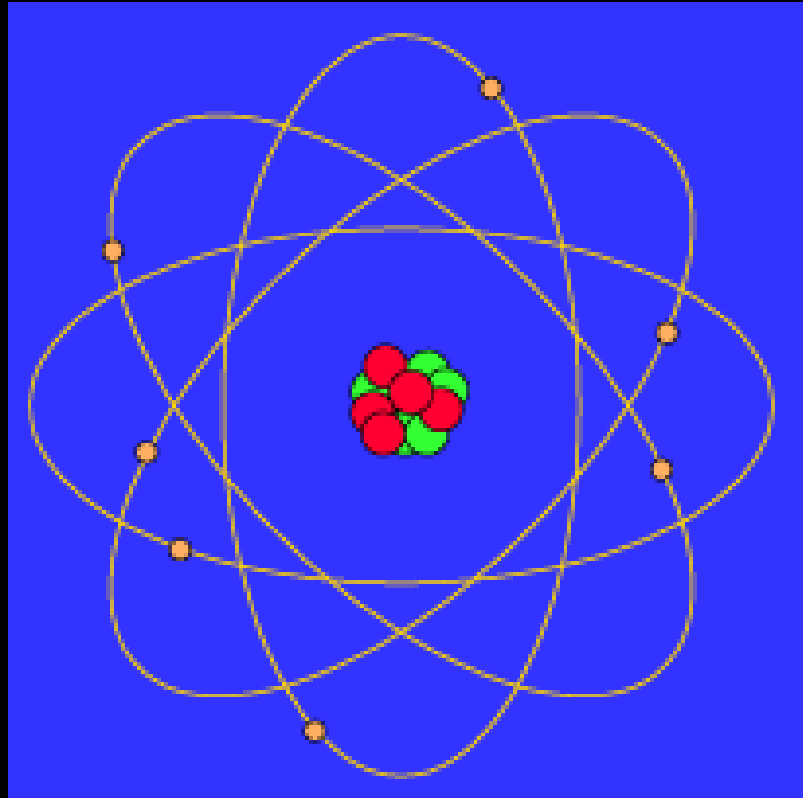
# The Quantum World



Light energy is  
*quantised* in packets,  
or *photons* of energy

Bohr atom, 1913

# The Quantum World



# Heisenberg Uncertainty Principle



The precision of  
measurements in  
a quantum  
system is limited  
*in principle*



# Heisenberg Uncertainty Principle



The precision of measurements in a quantum system is limited *in principle*

$$\Delta p \Delta x \sim \hbar$$

# Heisenberg Uncertainty Principle



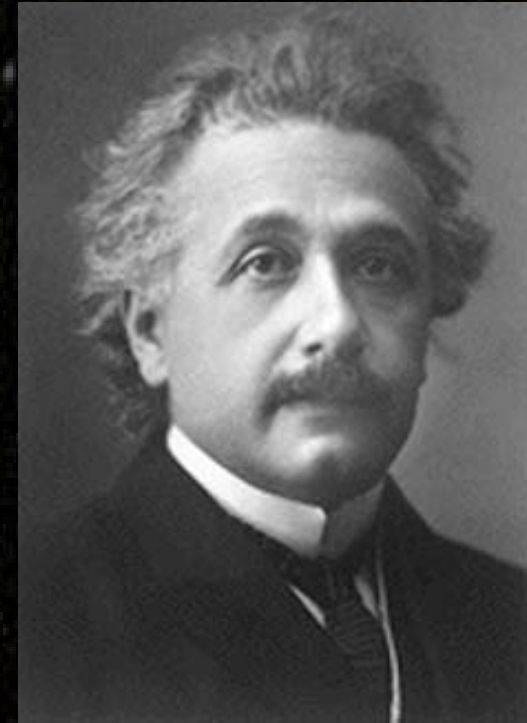
The precision of measurements in a quantum system is limited *in principle*

$$\Delta p \Delta x \sim \hbar$$



Position and momentum are *complementary* properties: the action of measurement determines which of the two properties the quantum system possesses

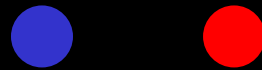
**"God does not  
play dice"**



**Thought experiment, proposed by  
Einstein Podolsky & Rosen (1935)**

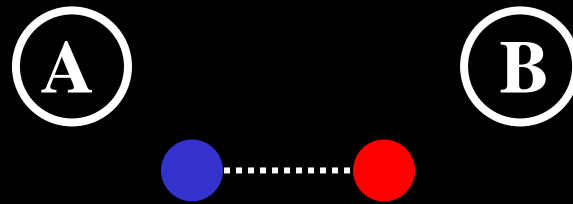
**designed to expose the paradox of  
complementarity**

# The EPR 'Paradox'



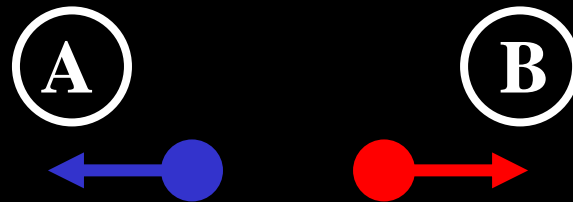
Quantum system: two particles,  
initially coupled, then fly apart

# The EPR 'Paradox'



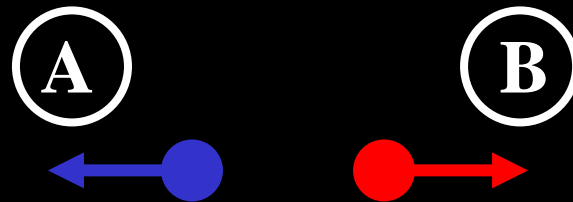
Quantum system: two particles,  
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## The EPR 'Paradox'



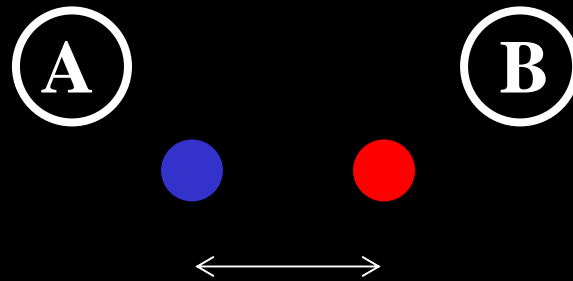
Quantum system: two particles,  
initially coupled, then fly apart

## The EPR 'Paradox'



Quantum system: two particles,  
initially coupled, then fly apart

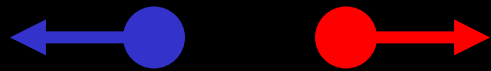
# The EPR 'Paradox'



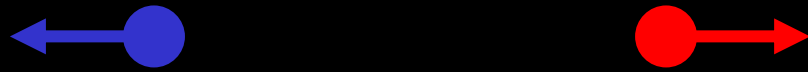
We can set things up so that initially the **total** momentum is zero (say).



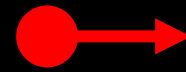
# The EPR 'Paradox'



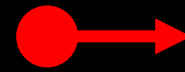
# The EPR 'Paradox'



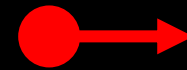
# The EPR 'Paradox'



# The EPR 'Paradox'



# The EPR 'Paradox'

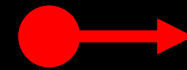


We decide to  
measure the  
momentum of  $\textcircled{A}$

# The EPR 'Paradox'



We decide to  
measure the  
momentum of (A)



(B) *instantaneously*  
adopts 'momentum'  
state

How does it know?

## The EPR 'Paradox'

EPR regarded this prediction as unreasonable, as it violated causality.

“[It] makes the reality of position and momentum in the second system depend upon the measurement carried out in the first system, which does not disturb the second system in any way. *No reasonable definition of reality could be expected to permit this.*”

But this is exactly what **does** happen

# Quantum Entanglement

Quantum states are 'entangled': they can influence each other instantaneously, even when separated by great distances

This is the idea behind the Star Trek 'teleporter'





# Quantum Entanglement

Quantum states are 'entangled': they can influence each other instantaneously, even when separated by great distances

This is the idea behind the Star Trek 'teleporter'

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TRAVEL  
EDUCATION  
IN-DEPTH


EXPERTS AGREE:  
*When offered MONEY for Nothing...*

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### 'Star Trek' teleporter nearer reality

June 17, 2002 Posted: 12:47 AM EDT (0447 GMT)



COURTESY, LASERUIH

CANBERRA, Australia -- It's not quite "Star Trek" yet, but Australian university researchers in quantum optics say they have "teleported" a message in a laser beam using the same technology principles that enabled Scotty to beam up Captain Kirk.

What the team at the Australian National University have managed to achieve is to take apart an encrypted laser beam and simultaneously rebuild a replica one meter away.

Using a process called "quantum entanglement", the team effectively teleported a radio signal contained in the laser beam of light from one place to another.

Team leader Ping Koy Lam said the technology was the same as that used in science-fiction series such as "Star Trek".

"What we have demonstrated here is that we can take billions of photons, destroy them simultaneously, and then recreate them in another place," Lam told The Australian newspaper.

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# Gravity in Einstein's Universe

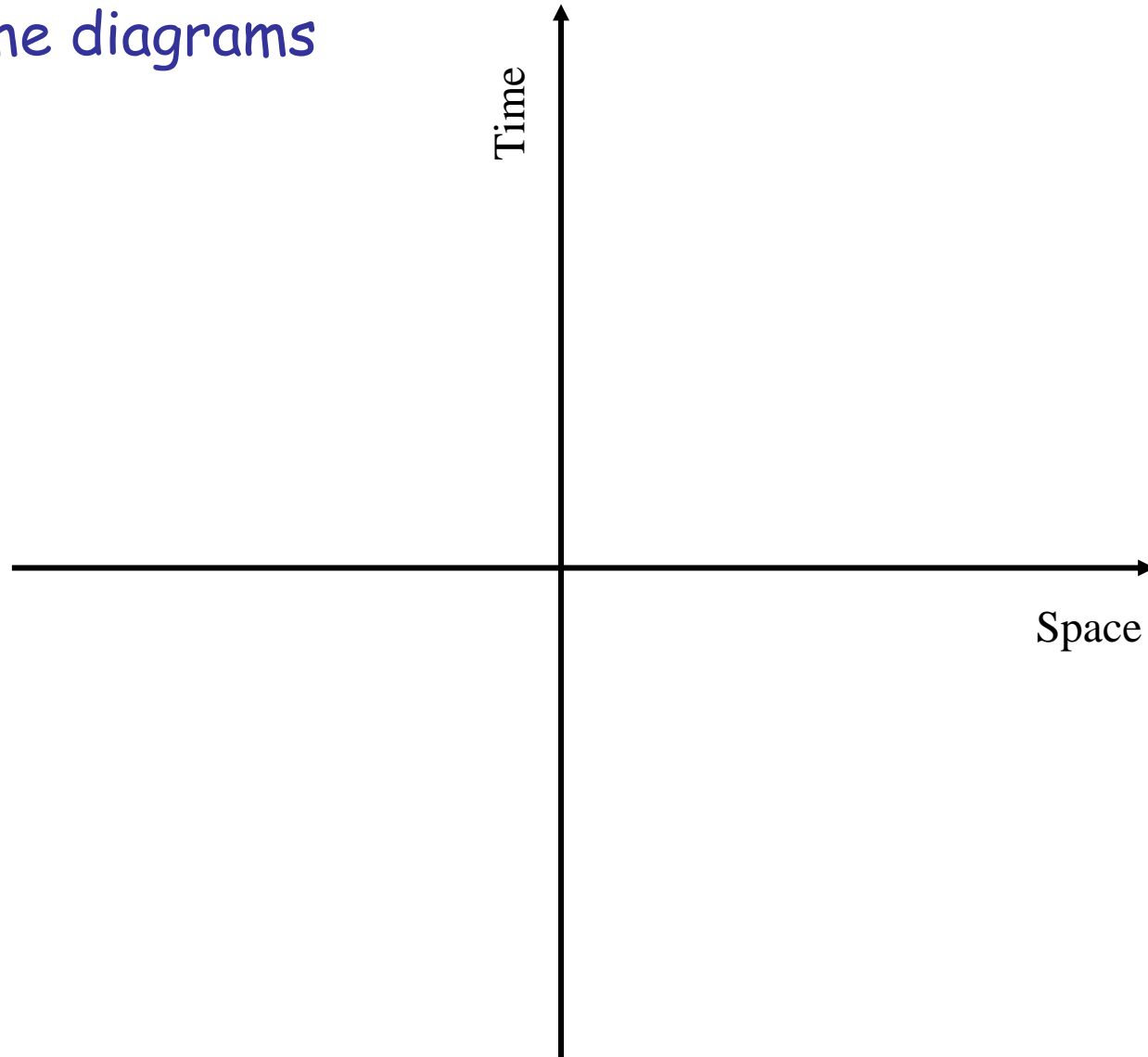
A 'Black Hole' warps spacetime so much that even light can't escape



A Black Hole has an 'event horizon'

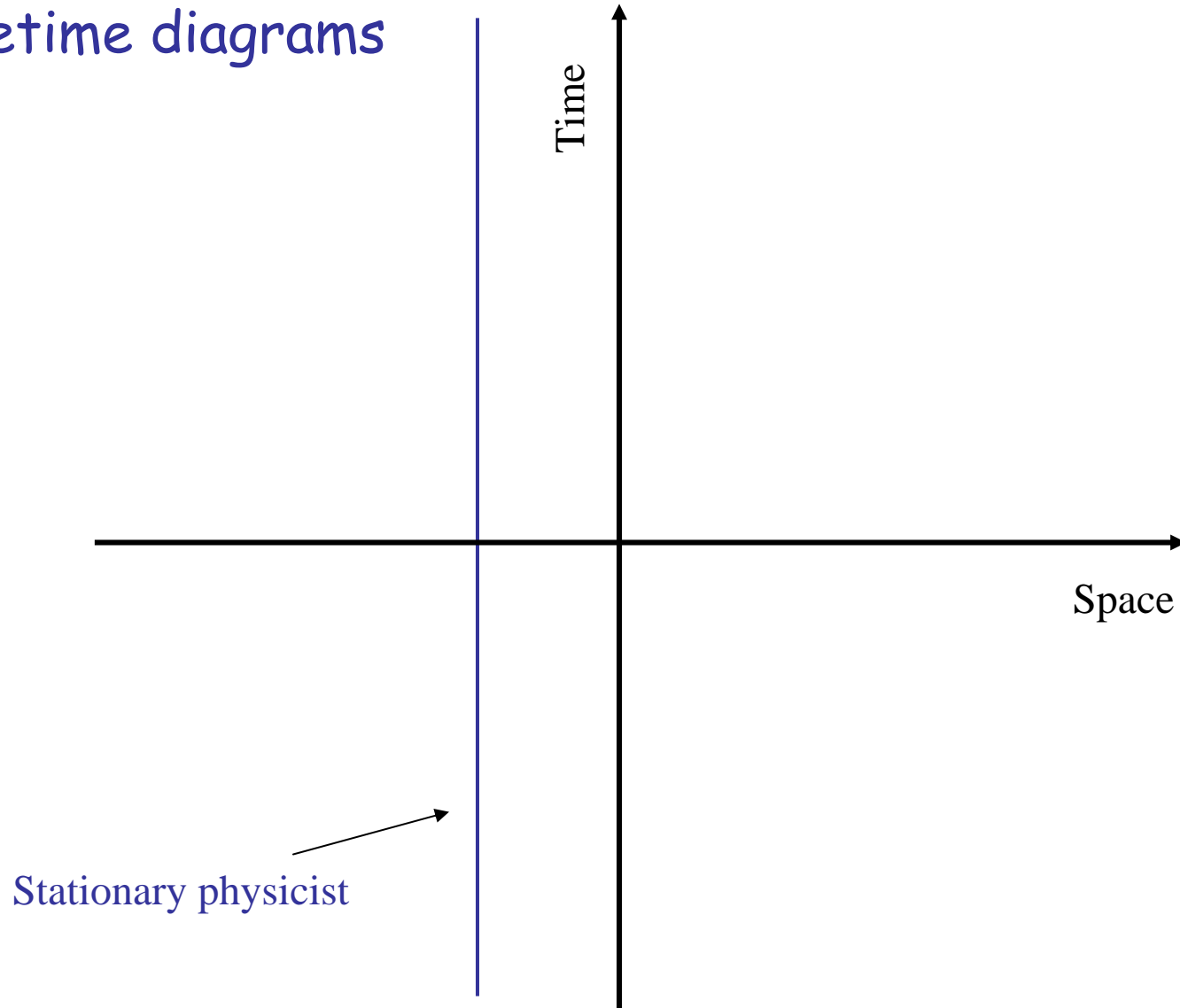
# Making Sense of Einstein's Universe

Spacetime diagrams



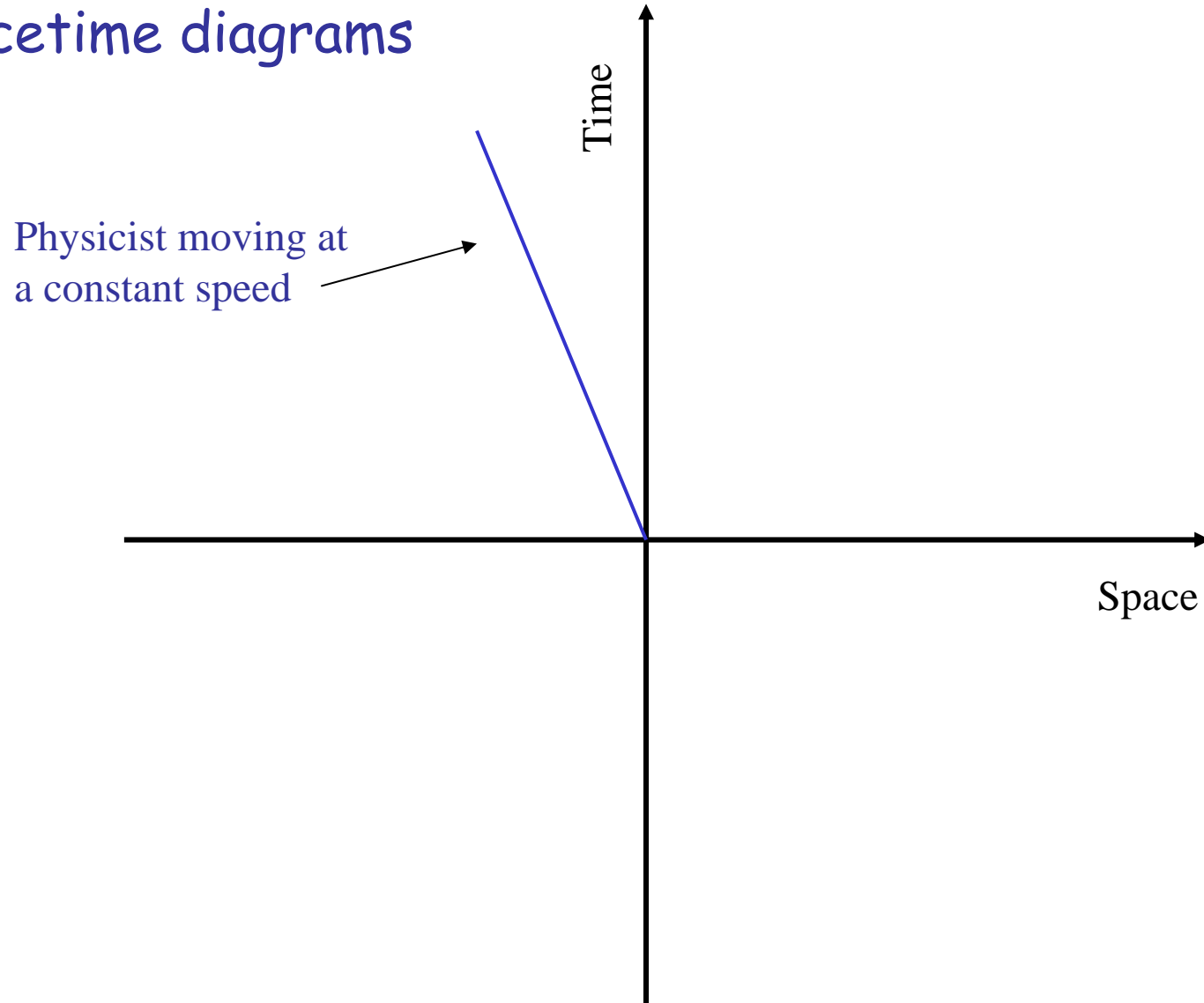
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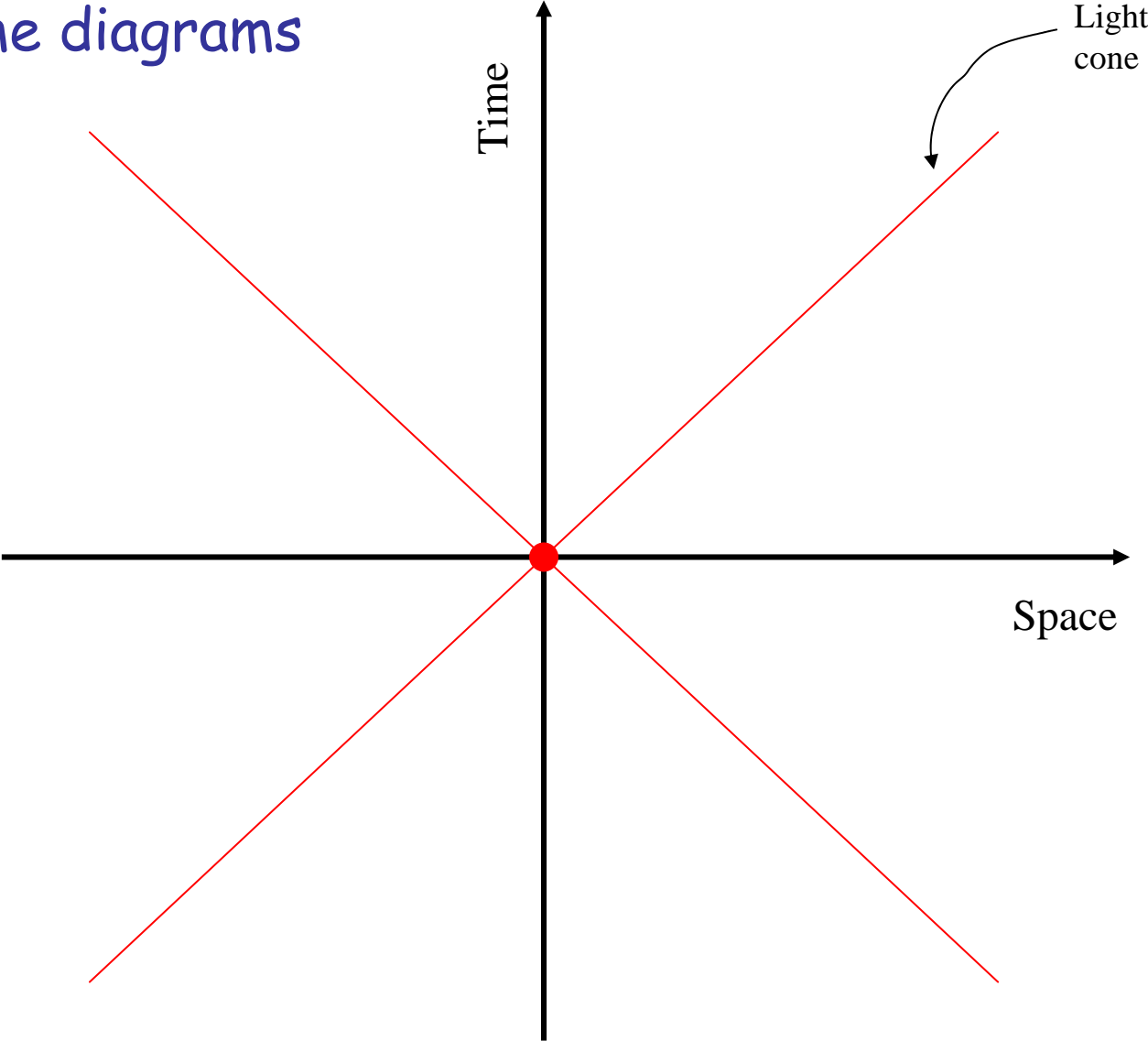
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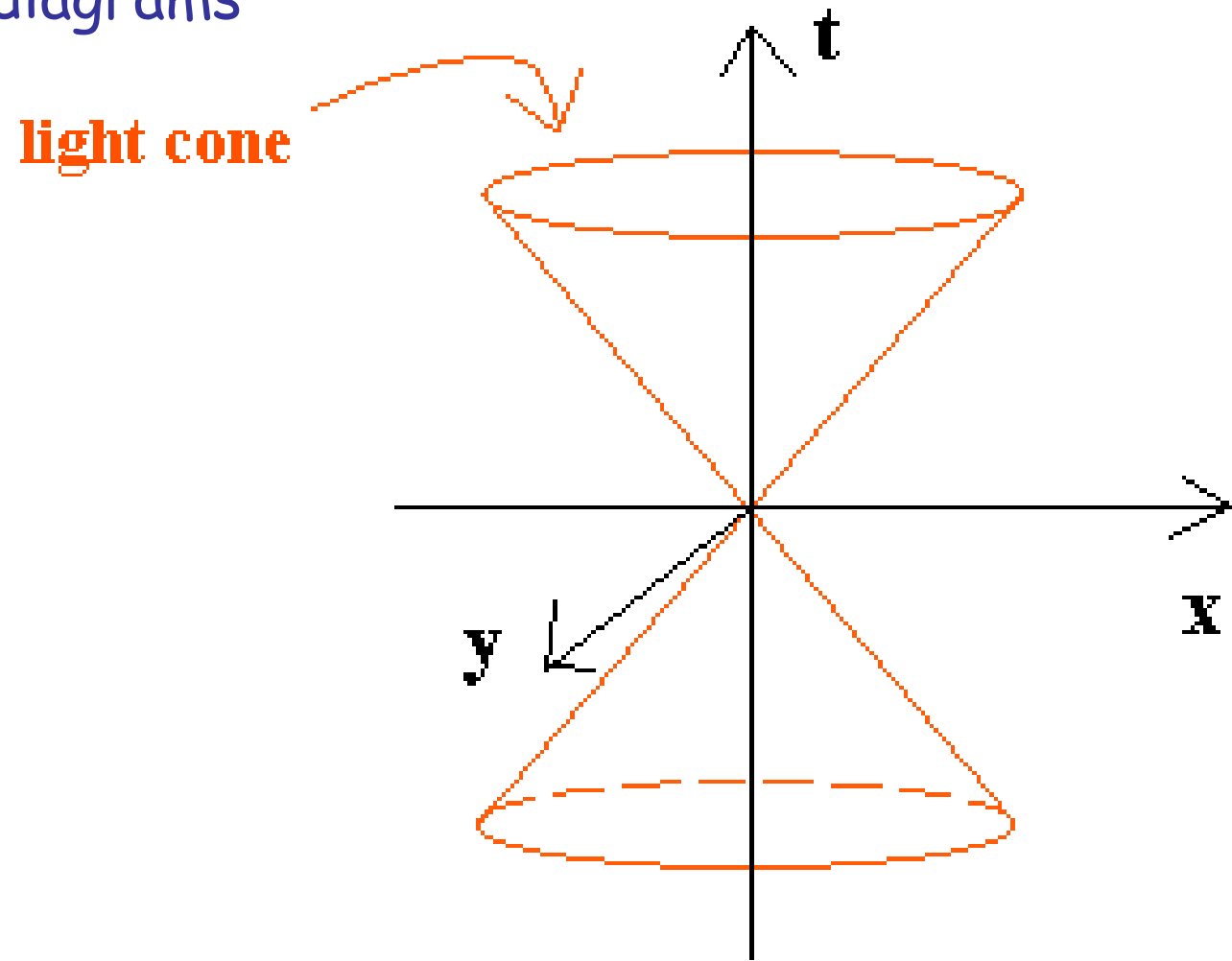
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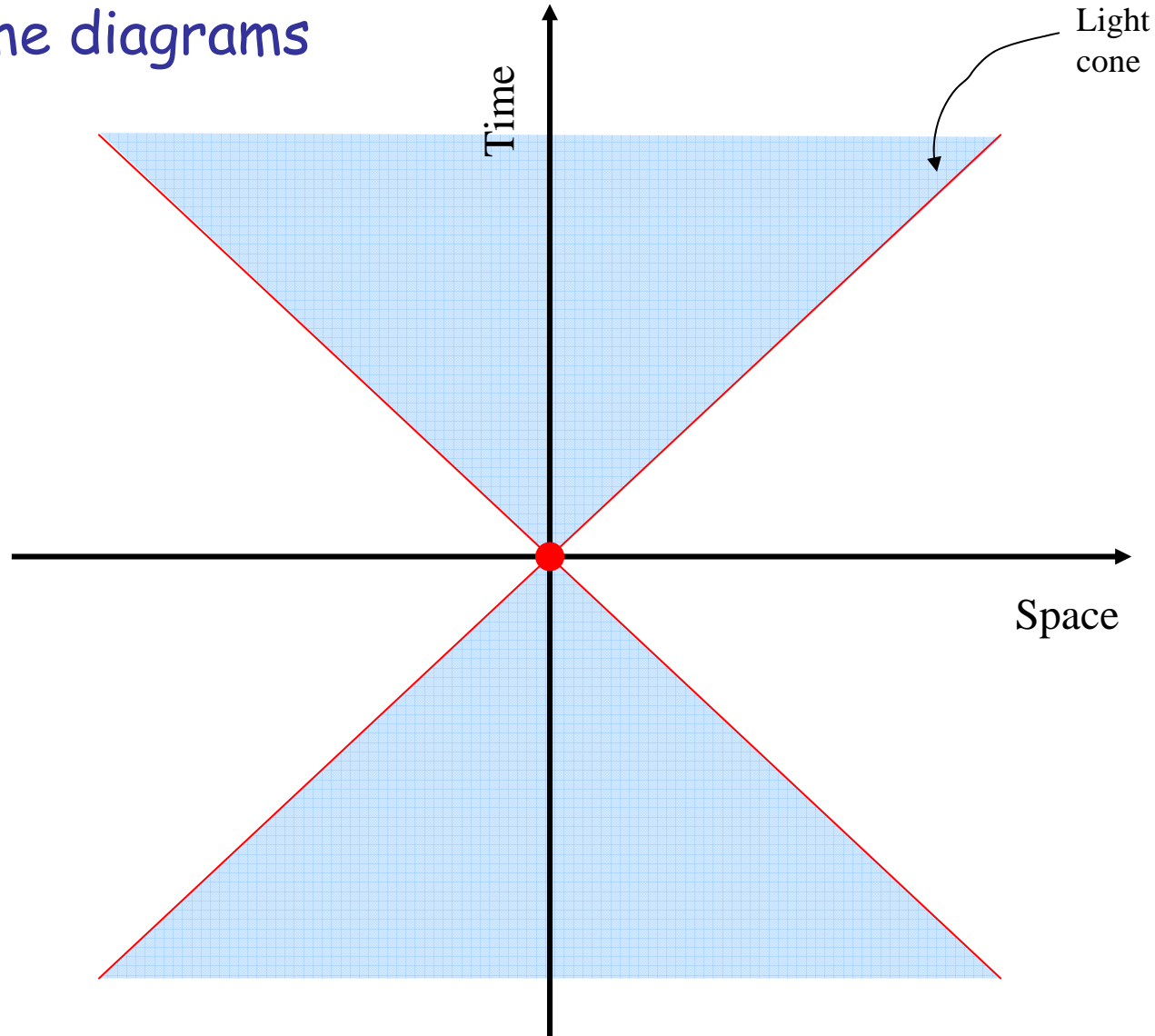
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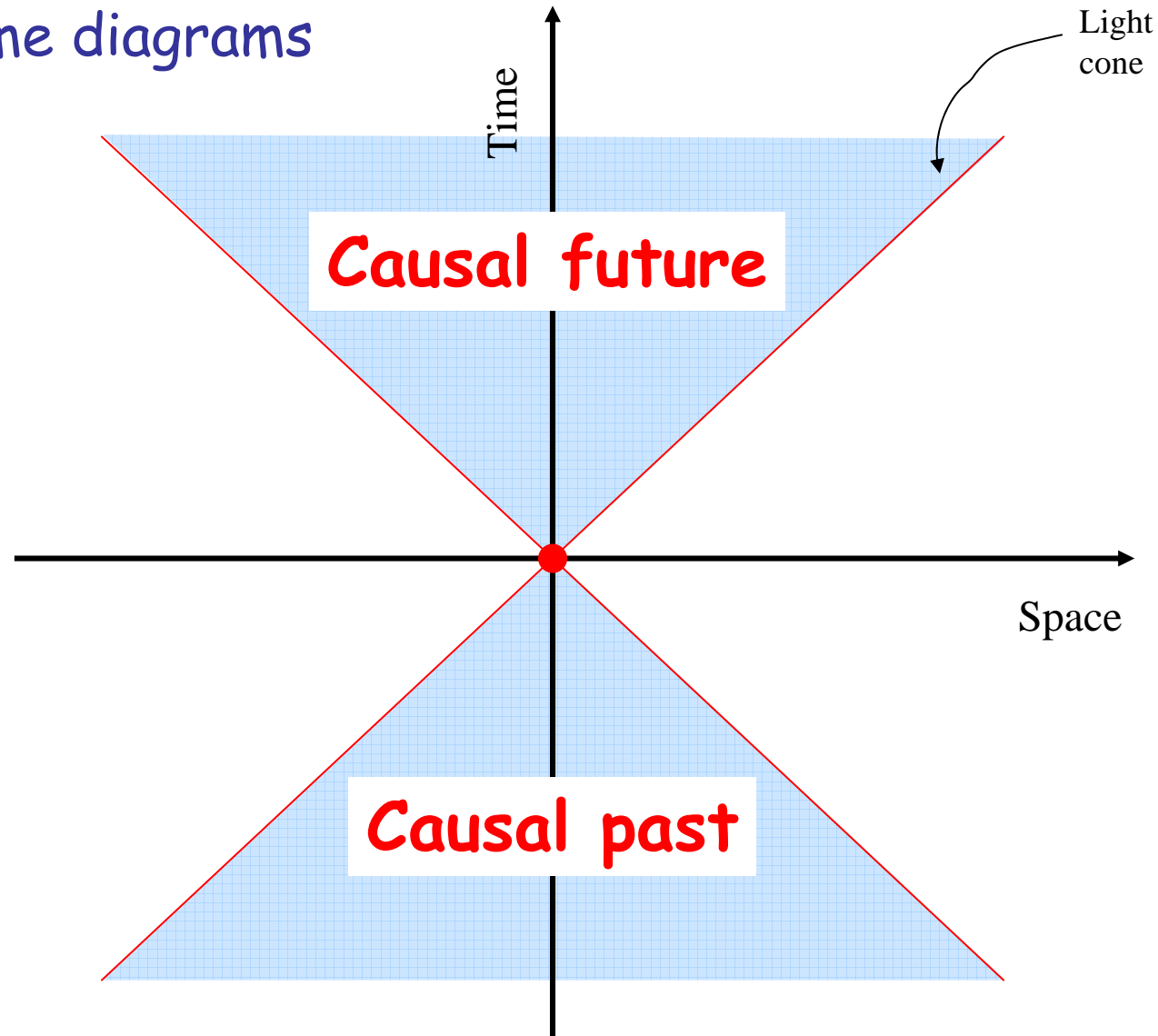
Spacetime diagrams





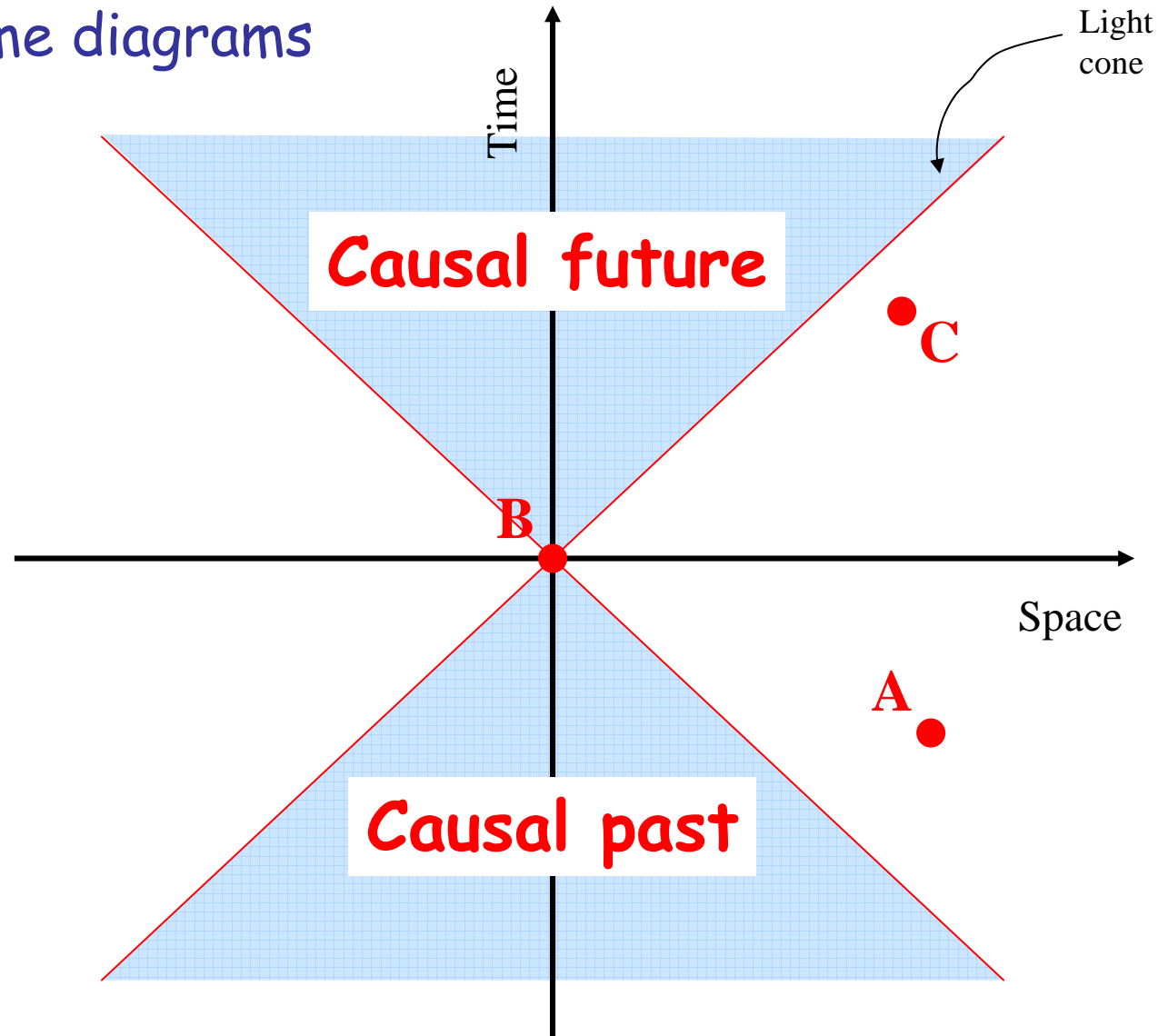
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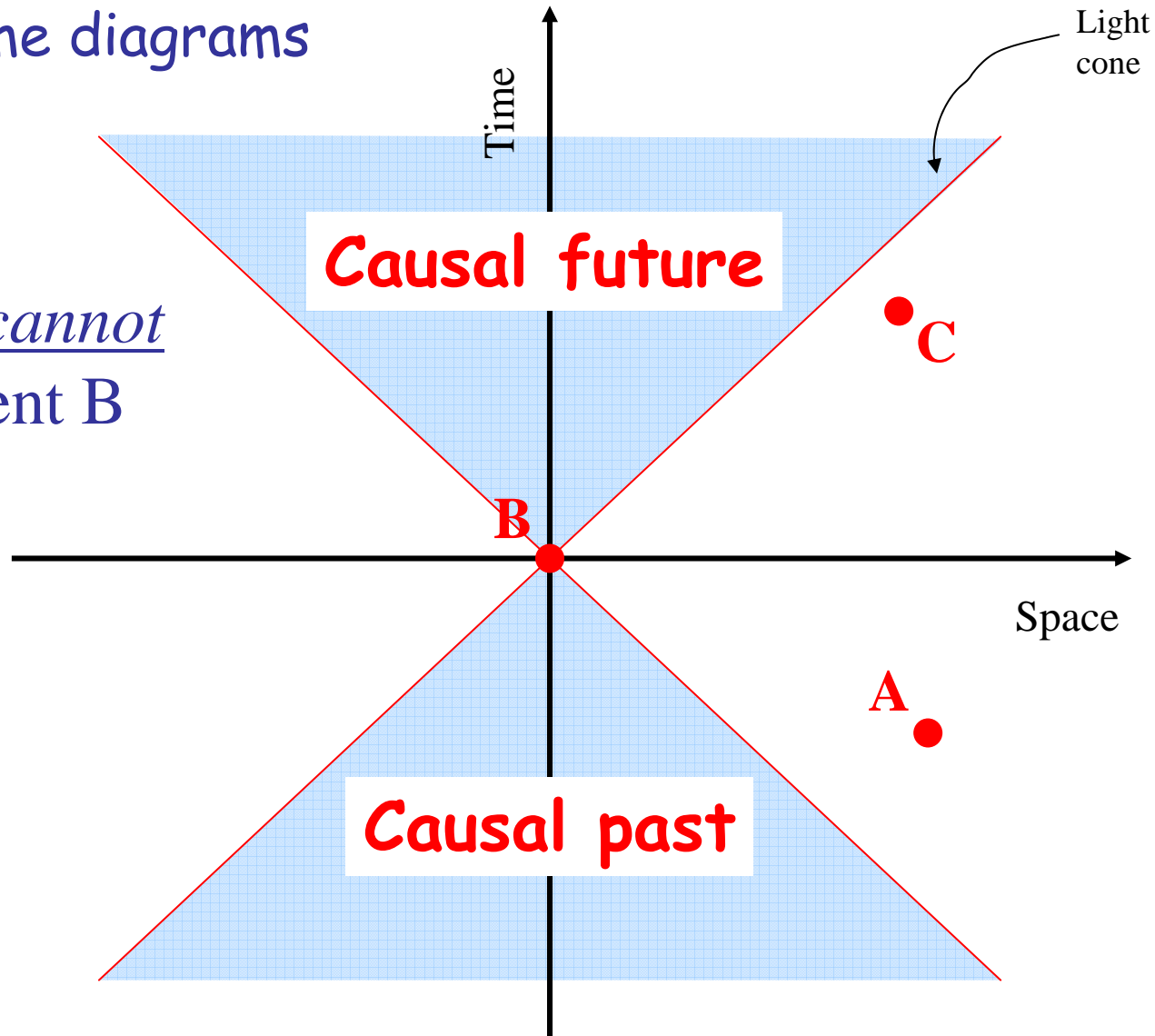
Spacetime diagrams



# Making Sense of Einstein's Universe

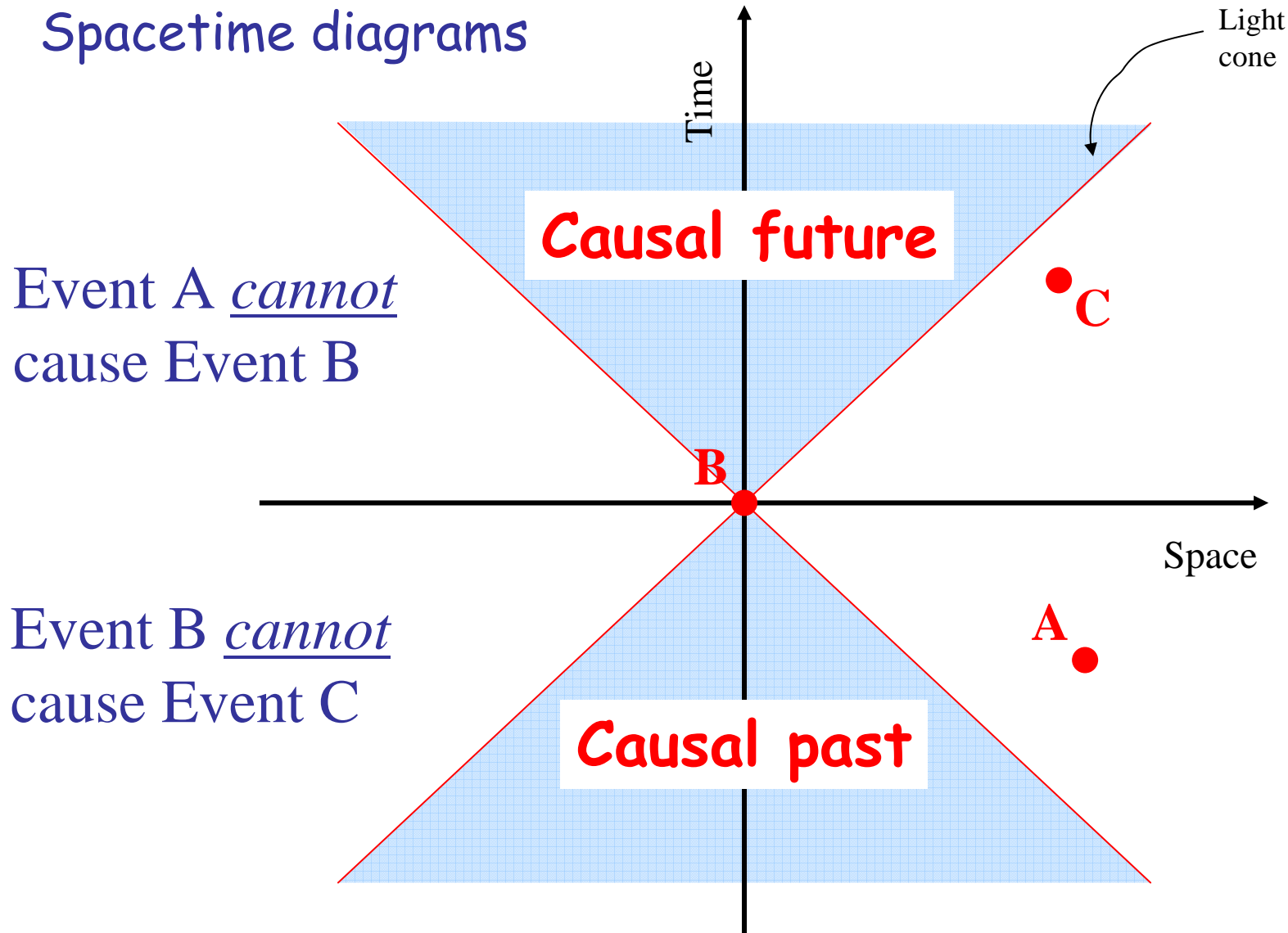
Spacetime diagrams

Event A *cannot*  
cause Event B



# Making Sense of Einstein's Universe

Spacetime diagrams

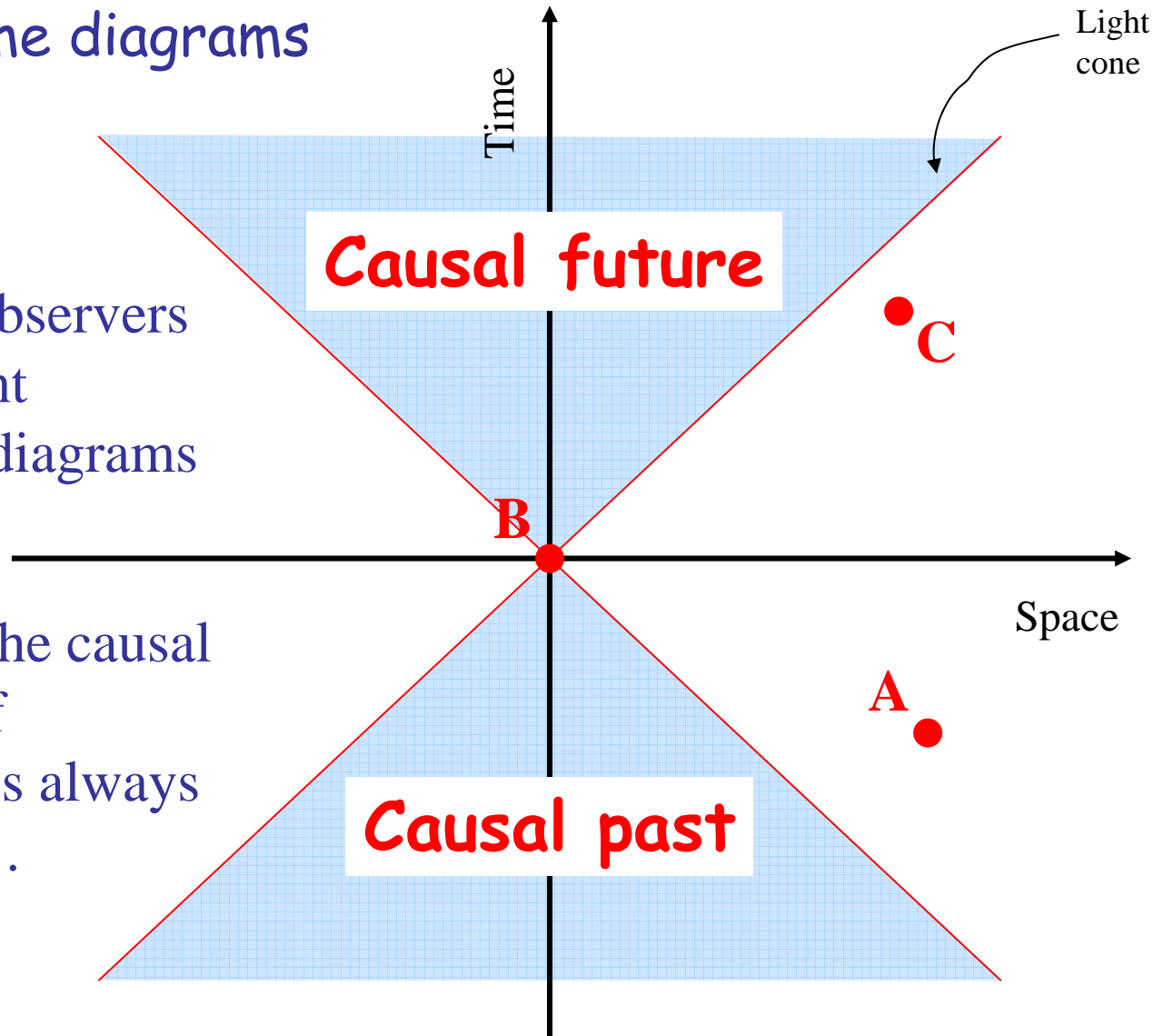


# Making Sense of Einstein's Universe

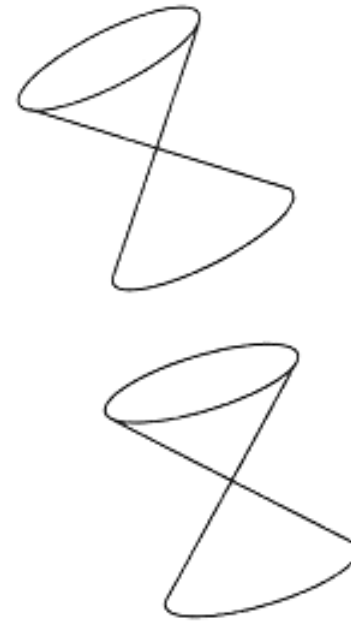
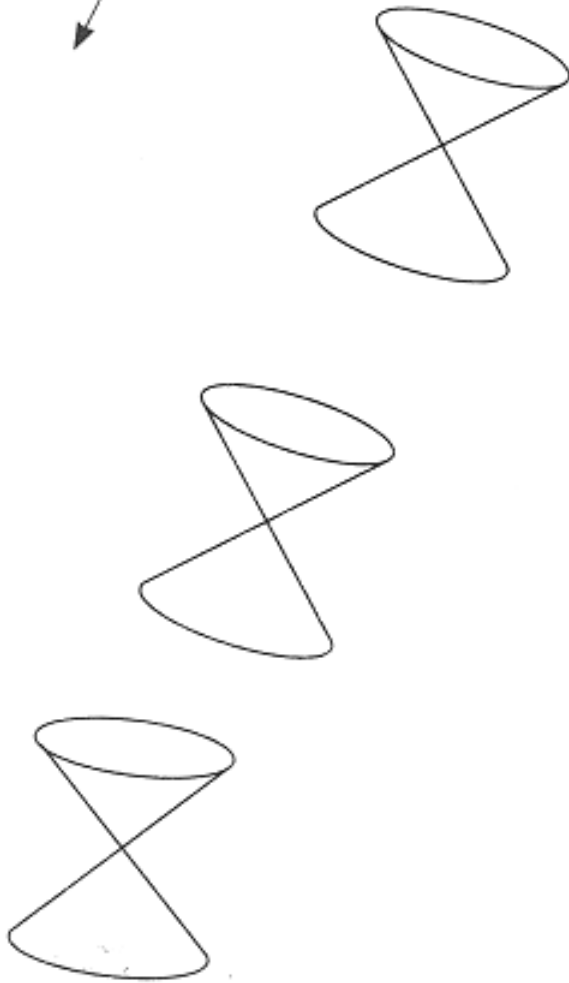
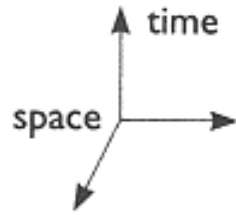
Spacetime diagrams

Different observers  
see different  
spacetime diagrams

However, the causal  
structure of  
spacetime is always  
preserved...

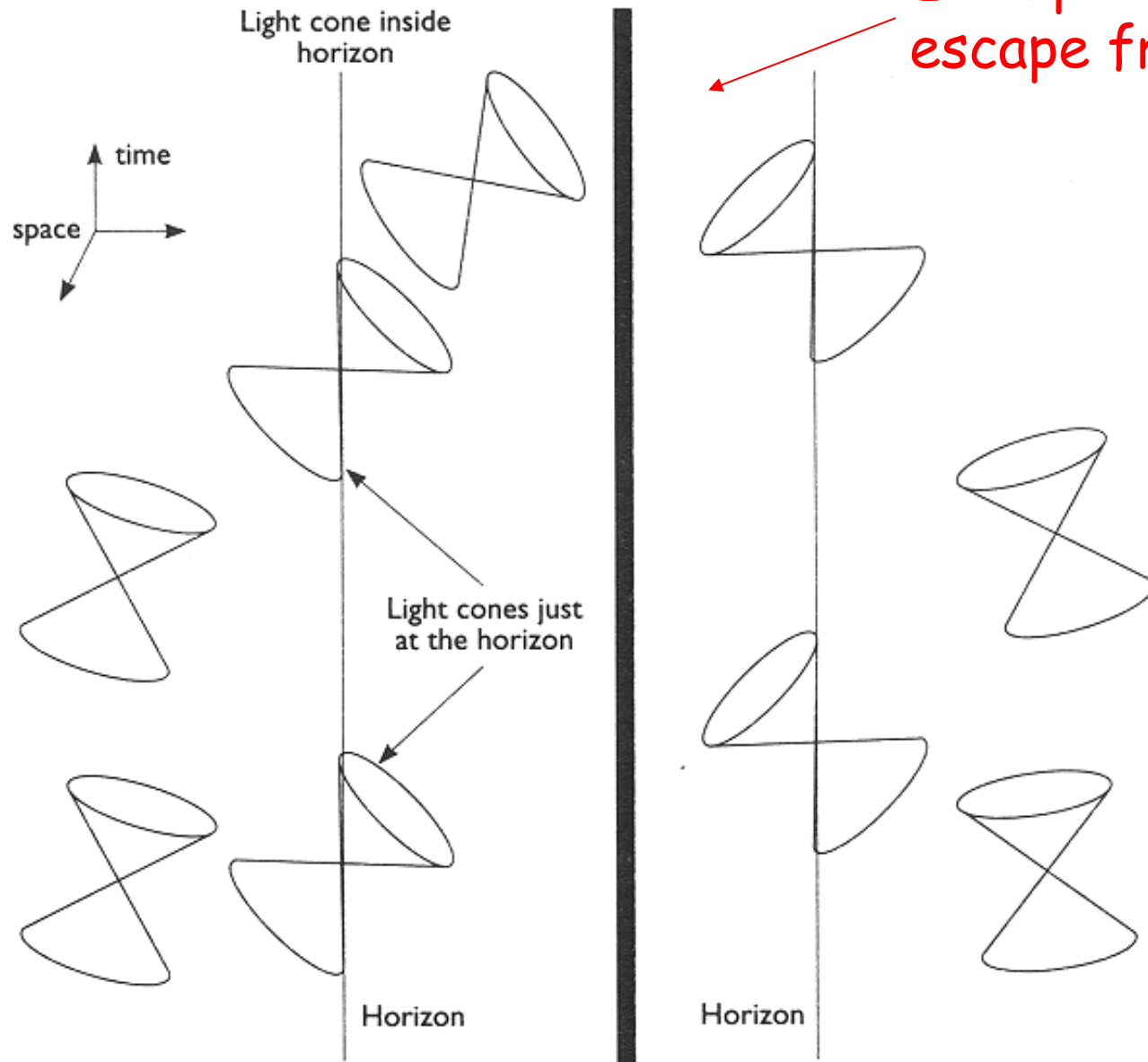


# Gravity 'tilts' light cones



'World line' of a star

# Gravity 'tilts' light cones



Even photons can't escape from here

'World line' of a black hole

# Bekenstein Entropy

In 1971 Jacob Bekenstein drew an important analogy:

Area of the event horizon behaves like the thermodynamic entropy of a Black Hole





# Bekenstein Entropy

In 1971 Jacob Bekenstein drew an important analogy:

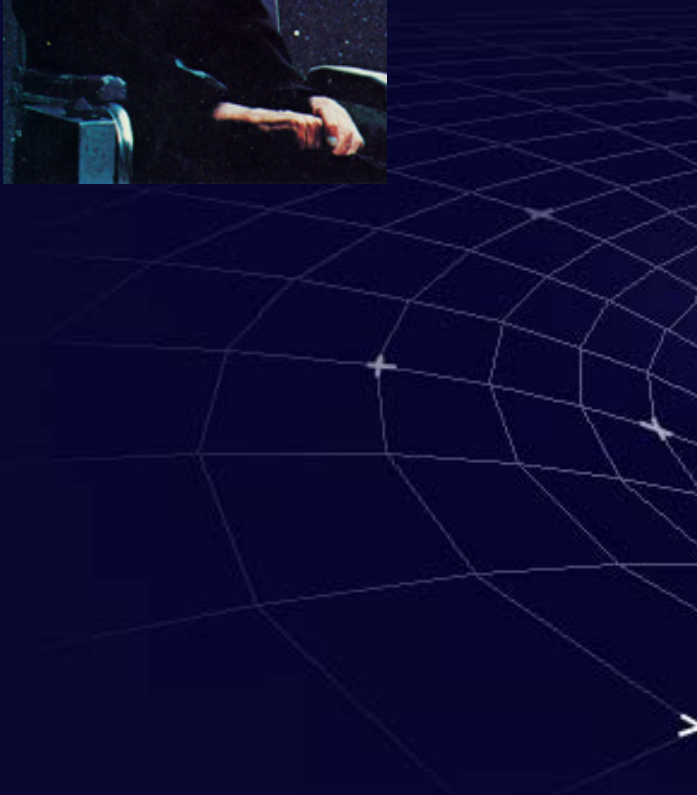
Area of the event horizon behaves like the **thermodynamic entropy** of a Black Hole

But a thermodynamical system also has a **temperature**

**How hot is a Black Hole?...**



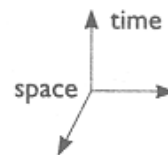
# By studying them as quantum objects, Stephen Hawking showed that Black Holes radiate



The other moves away from the black hole. It is correlated with the one lost beyond the horizon. Because of this its properties are random. The result is that heat is generated

One falls in and disappears behind the horizon. All information about it is apparently lost to outside observers

A pair of photons are created just outside the horizon, in a correlated state as in the EPR experiment



Horizon

Singularity

x

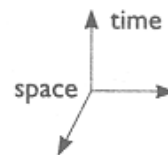
# This completed the link between Black Holes and thermodynamics



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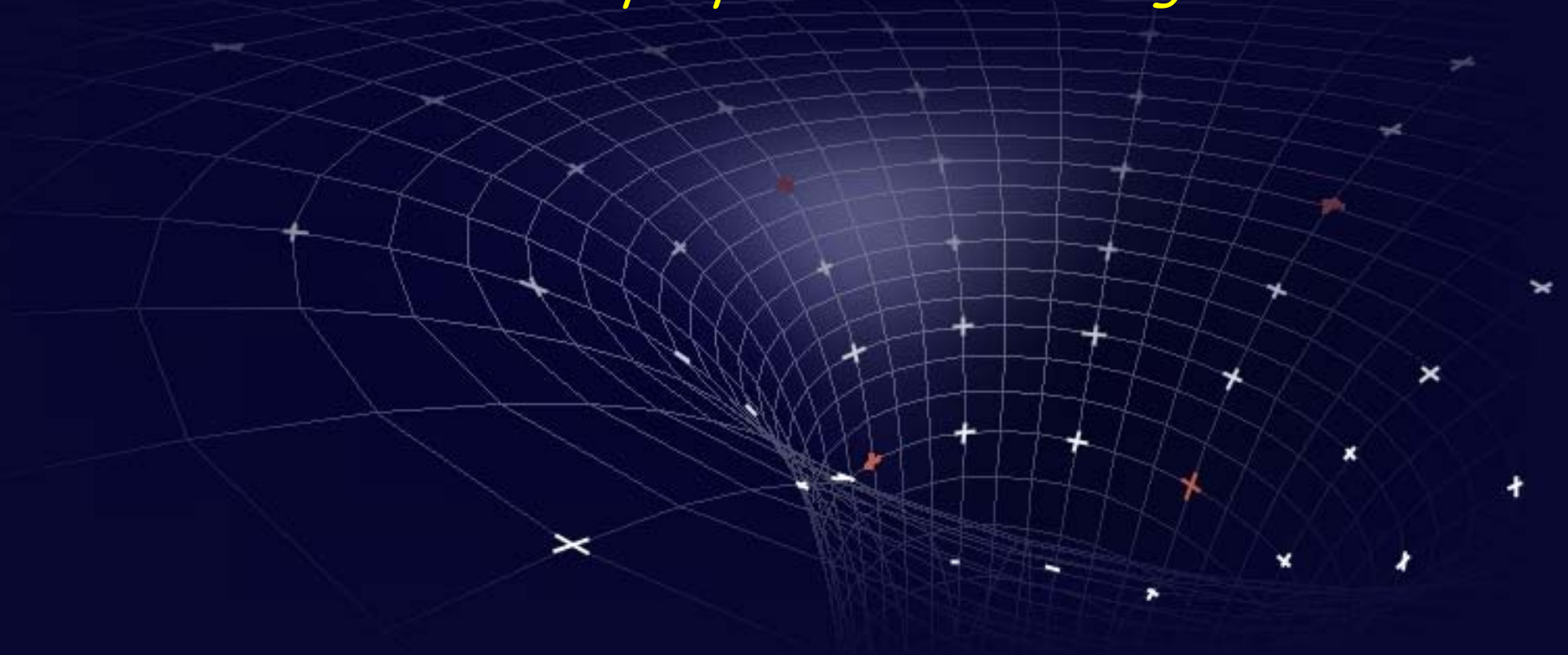
Horizon

Singularity

x

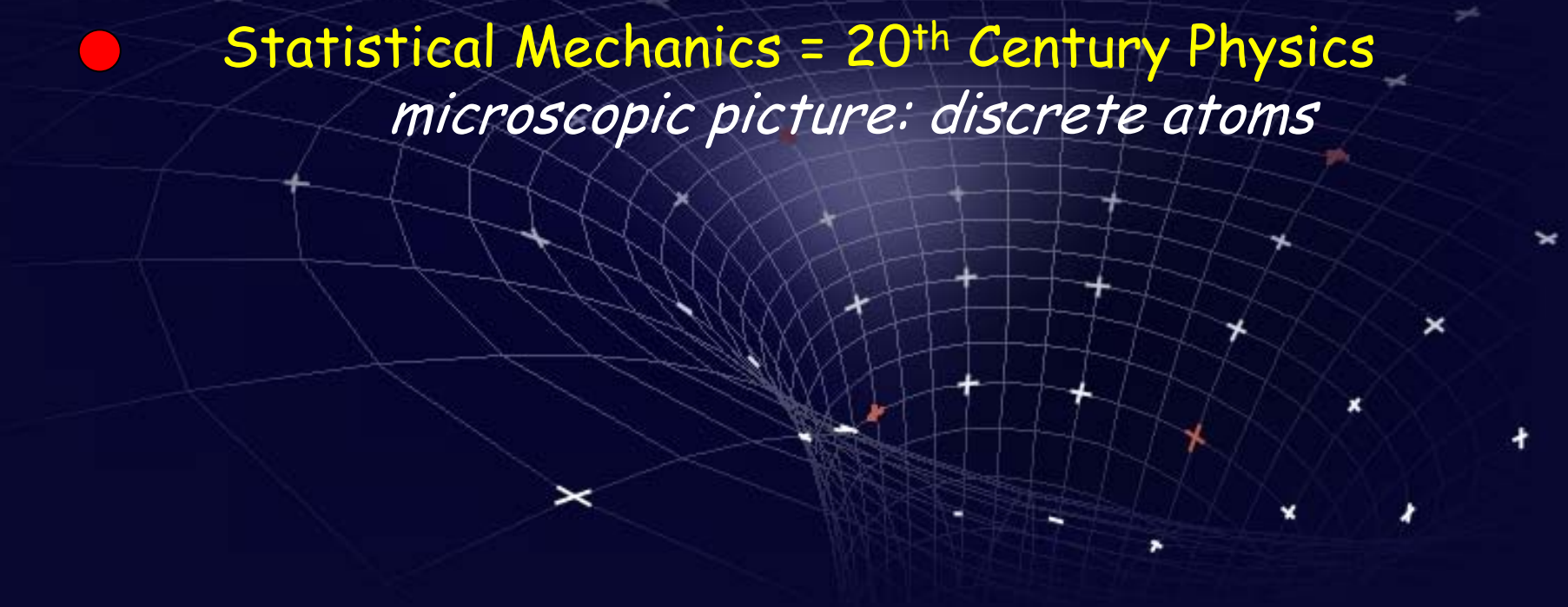
# Quantised spacetime

- Thermodynamics = 19<sup>th</sup> Century Physics  
*macroscopic picture: 'smooth' gas*



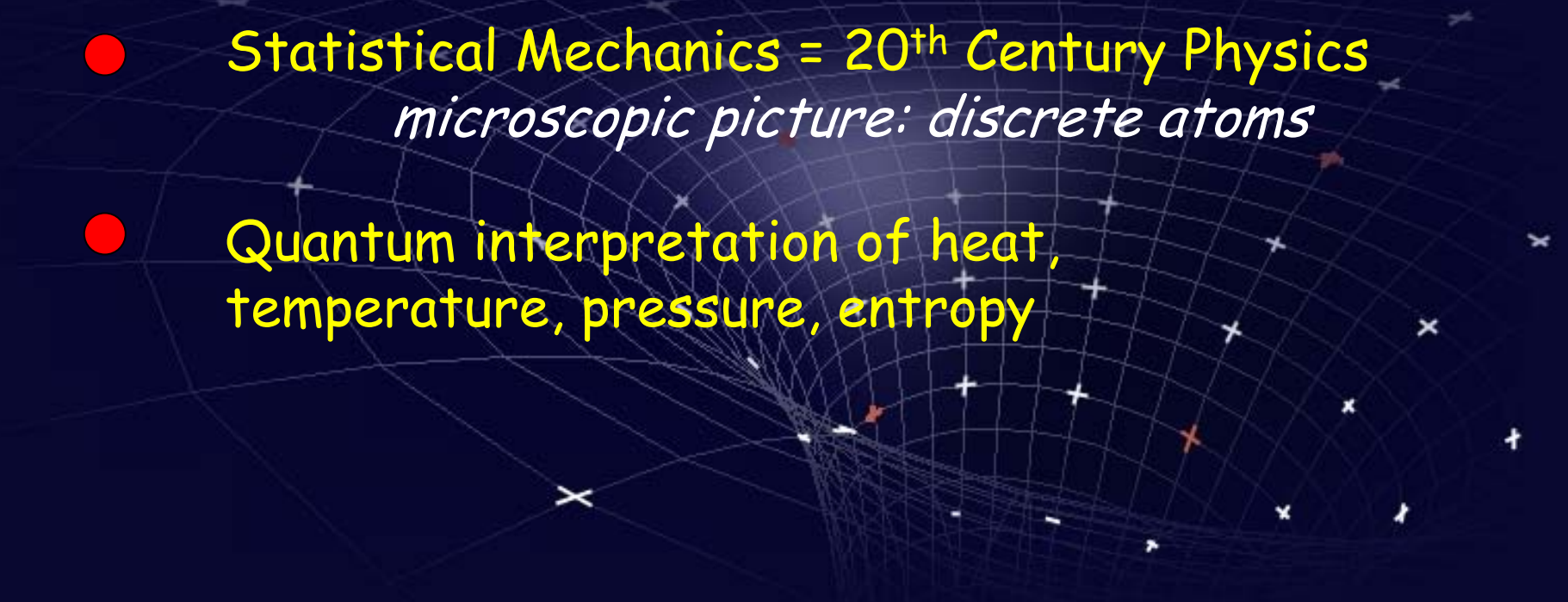
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- Statistical Mechanics = 20<sup>th</sup> Century Physics  
*microscopic picture: discrete atoms*



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*microscopic picture: discrete atoms*
- Quantum interpretation of heat,  
temperature, pressure, entropy



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- Statistical Mechanics = 20<sup>th</sup> Century Physics  
*microscopic picture: discrete atoms*
- Quantum interpretation of heat, temperature, pressure, entropy
- Entropy measures our information about the motions of individual atoms
- Does Bekenstein Entropy indicate a quantum interpretation of spacetime?

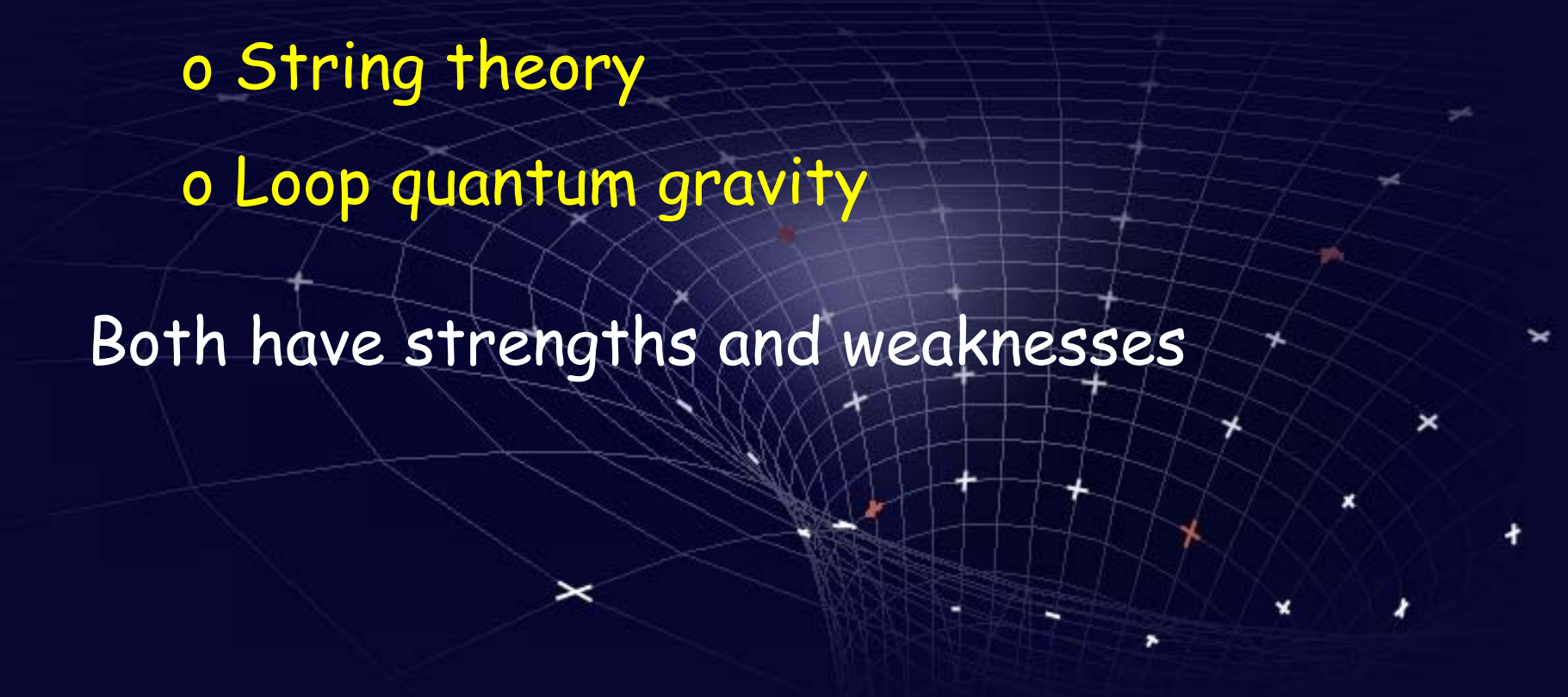


# Theories of Quantum Gravity

Currently two popular candidates:-

- o String theory
- o Loop quantum gravity

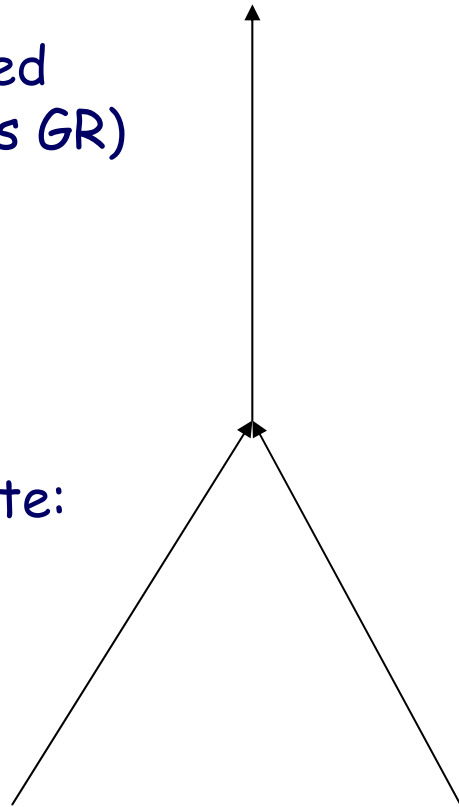
Both have strengths and weaknesses



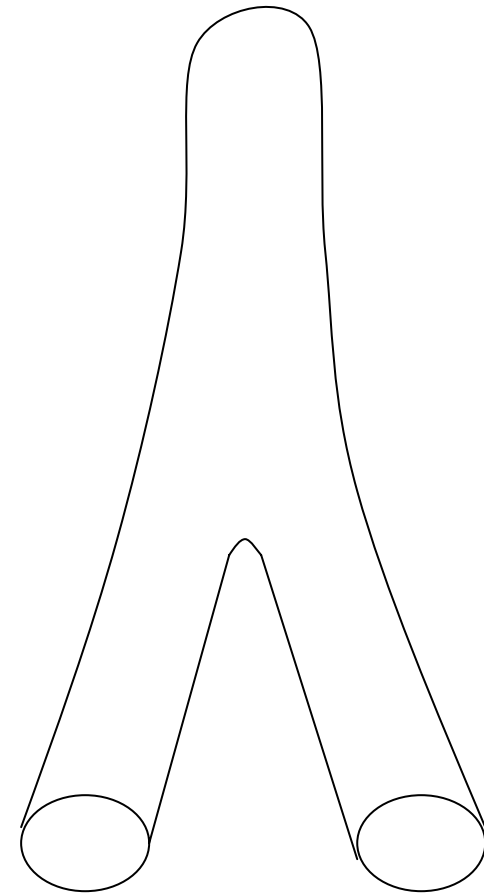
# String Theory

- Point particles replaced by string loops
- Avoids 'infinities'
- BUT defined on fixed background (violates GR)
- No unique theory (e.g. *Membranes* in higher dimensions)
- Spacetime is discrete:

$$\Delta x \sim \frac{\hbar}{\Delta p} + C\Delta p$$



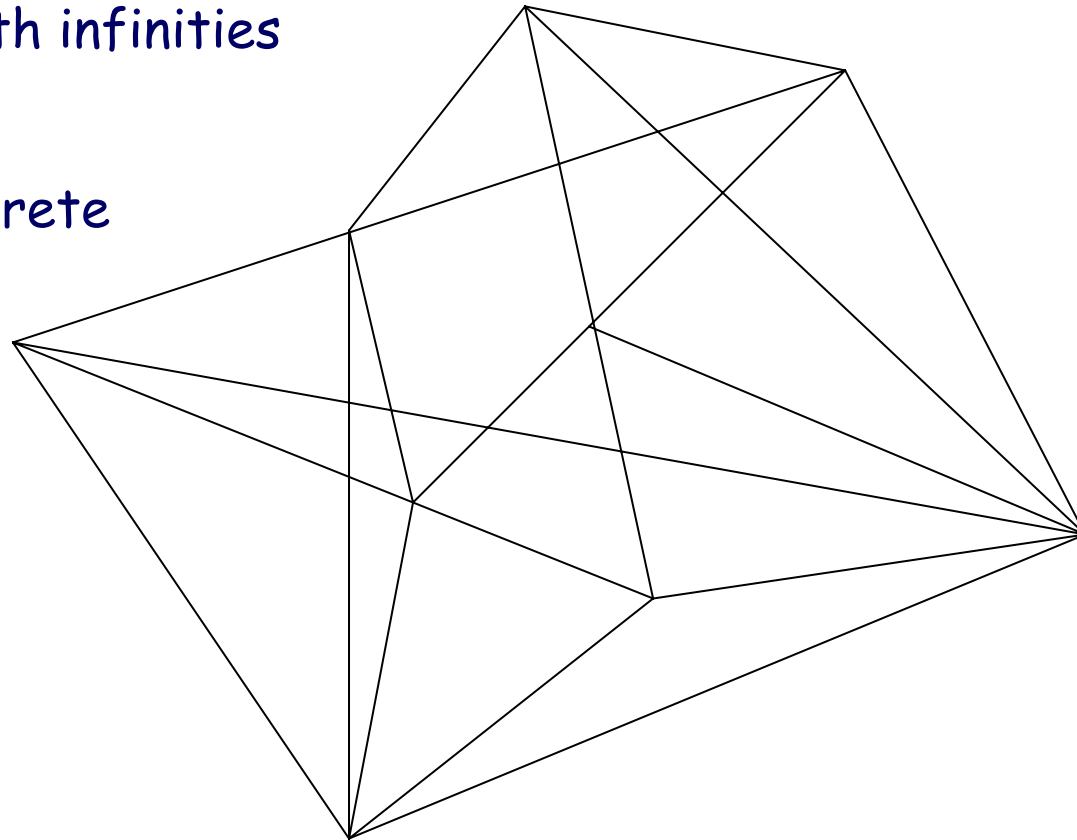
Particle representation



String representation

# Loop Quantum Gravity

- Network of relations between events
- Quantum correlations built in
- BUT problems with infinities (gravitons)
- Spacetime is discrete

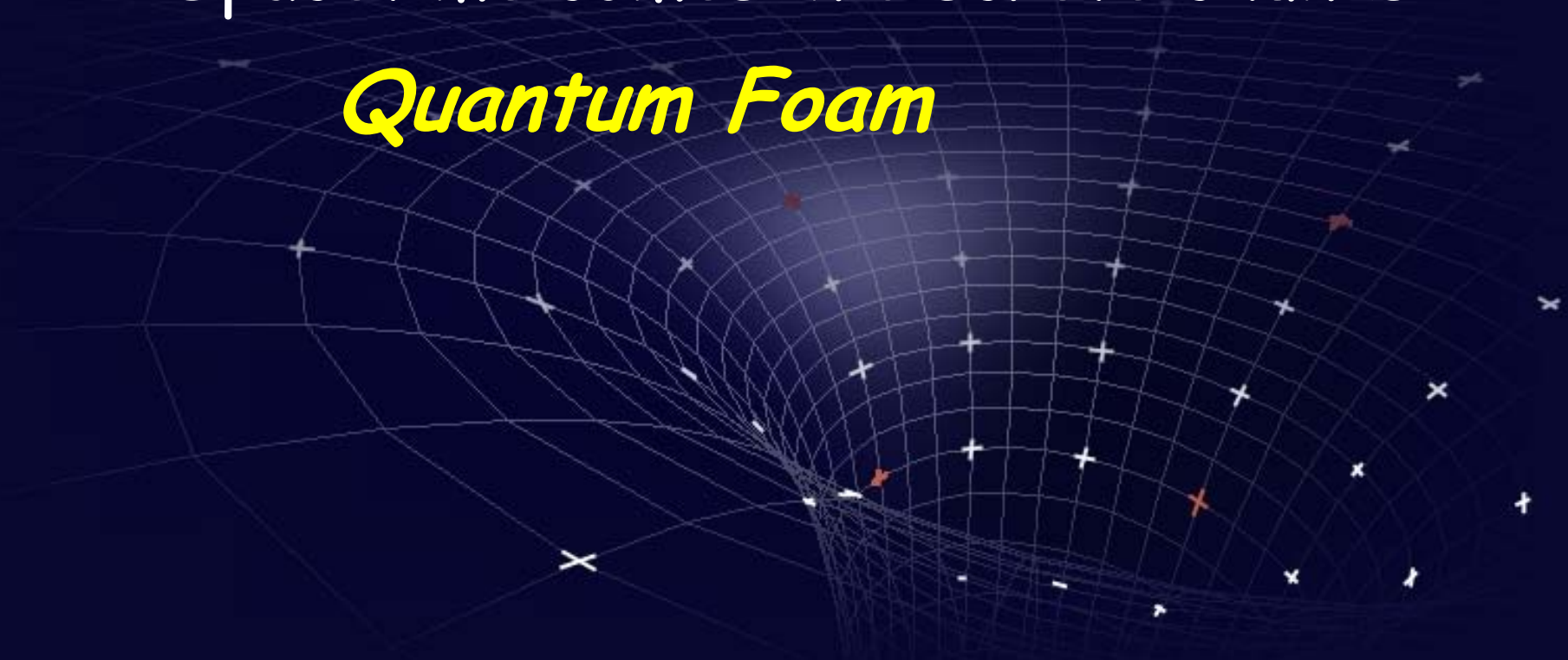


Quantum loop network

Three roads to same result:-

Spacetime comes in discrete chunks

*Quantum Foam*



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## Holographic principle:-

Three roads are different manifestations of same quantum gravity theory

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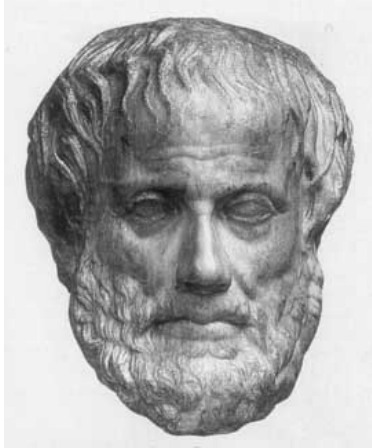
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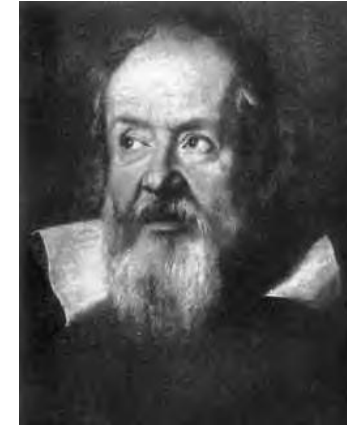
## *Analogous to Galileo and Kepler*

# *How do things move?....*



## *Aristotle's Theory:*

- 1. Objects move only as long as we apply a force to them*
- 2. Falling bodies fall at a constant rate*
- 3. Heavy bodies fall faster than light ones*



## *Galileo's Experiment:*

- 1. Objects keep moving after we stop applying a force (if no friction)*
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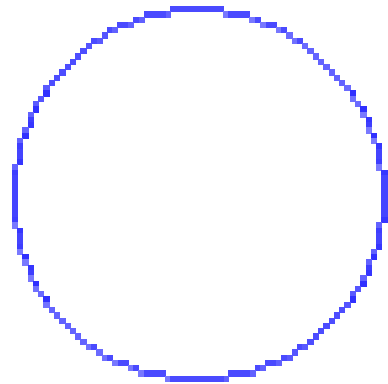
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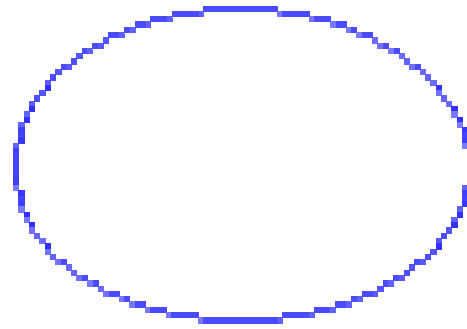
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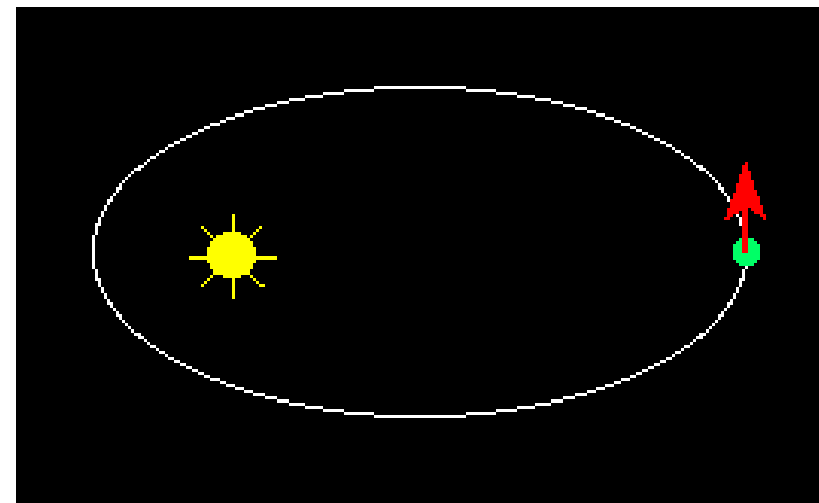
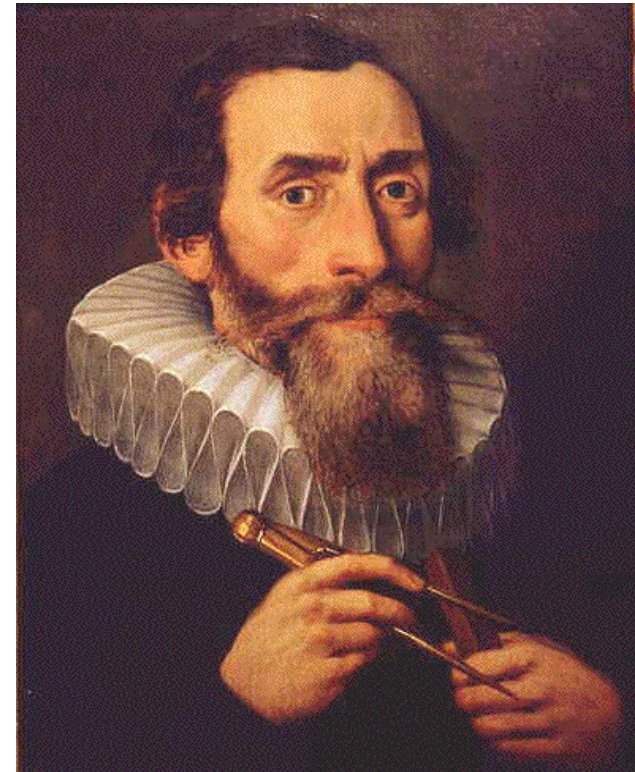
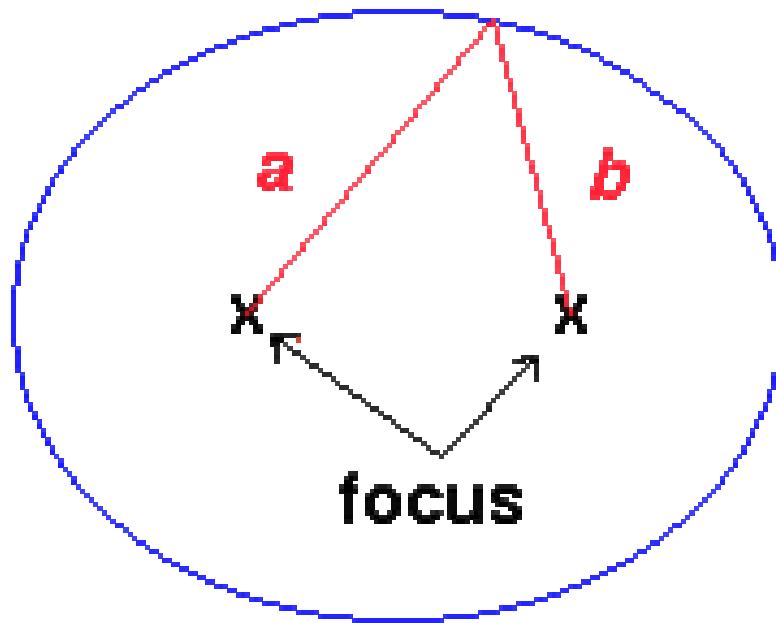




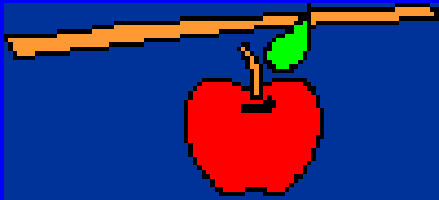
Circle



Ellipse



Kepler's laws, published 1609, 1619




Isaac Newton:  
1642 – 1727 AD

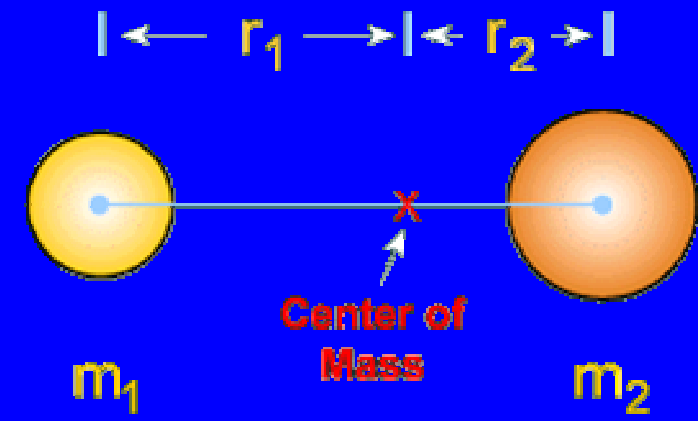
*The Principia: 1684 - 1686*

## Law of Universal Gravitation

Every object in the Universe attracts every other object with a force directed along the line of centers for the two objects that is proportional to the product of their masses and inversely proportional to the square of the separation between the two objects.

$$F_g = G \frac{m_1 m_2}{r^2}$$


A diagram showing two small circles representing masses  $m_1$  and  $m_2$ . A horizontal line connects their centers, with the distance between them labeled as  $r$ .



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- There may be an infinite number of string and loop theories - what chooses the one for 'our' Universe?

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Watch this space!