

# Dynamical Evolution of Planetary Systems and Debris Disks

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Extrasolar Planets: detection, formation, evolution, and dynamics of planetary systems

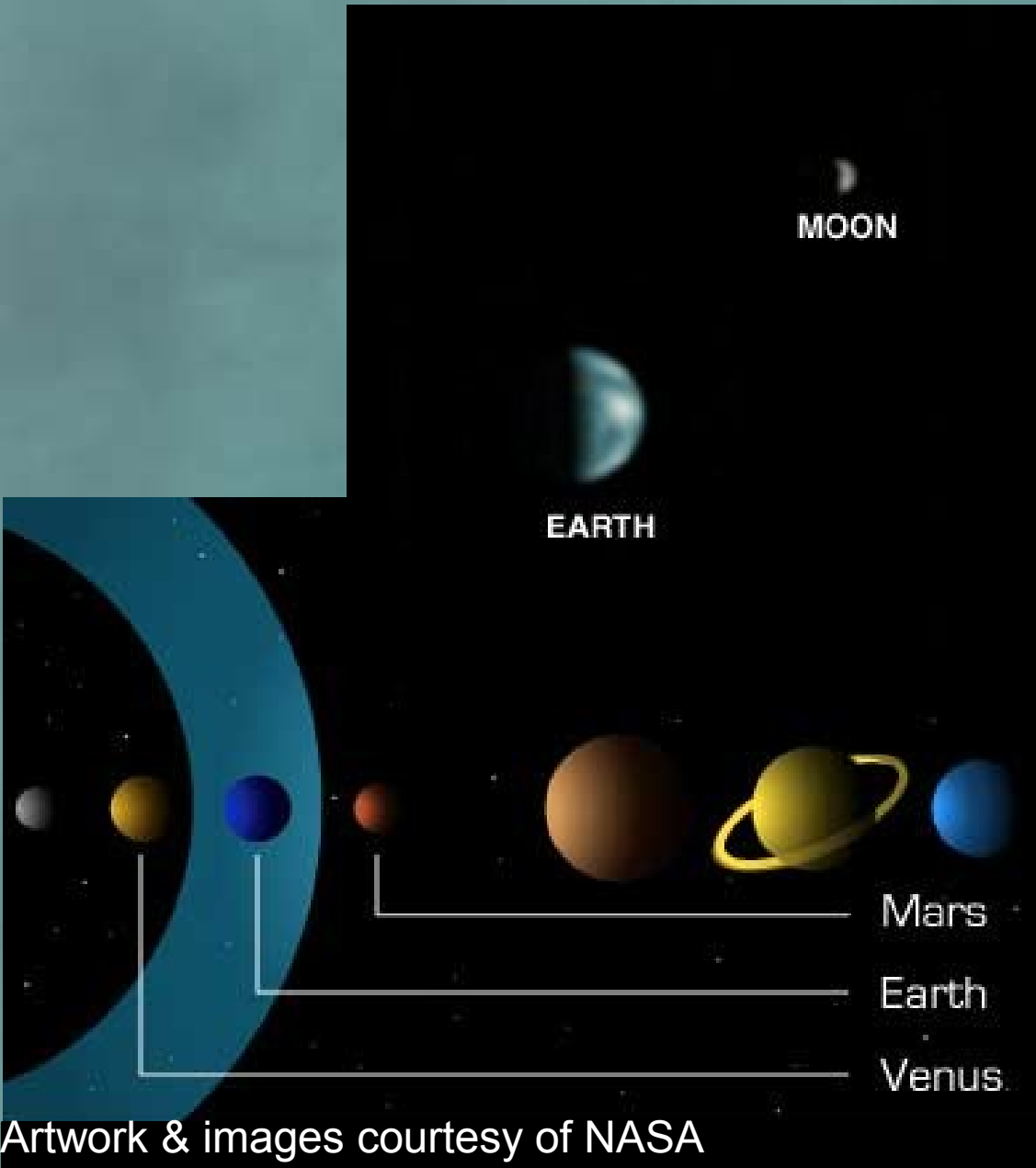
Sabhal Mor Ostaig, Isle of Skye, United Kingdom

Collaborators: Sourav Chatterjee<sup>G</sup>, Eugene Chiang, Scott Gaudi, Matt Holman,  
Kris Joshi<sup>G</sup>, Mario Juric, Boris Kozinsky<sup>U</sup>, Verene Lystad<sup>U</sup>, Fred Rasio,  
Boris Zbarsky<sup>U</sup>

# Motivation

- Understand Formation of Planetary Systems
  - How can extrasolar planet observations provide clues to the physics of planet formation?
  - Do observations of planetary systems today reflect the outcome of planet formation?
  - Or have they evolved since  $\sim 100$  Myr?
- Are planetary systems like our own common/rare?
  - Are Giant Planets in circular orbits at 5 AU common?
  - Are Terrestrial/Habitable Planets common?
- Rapid & dramatic increase in observational data

# Observed Planetary Systems



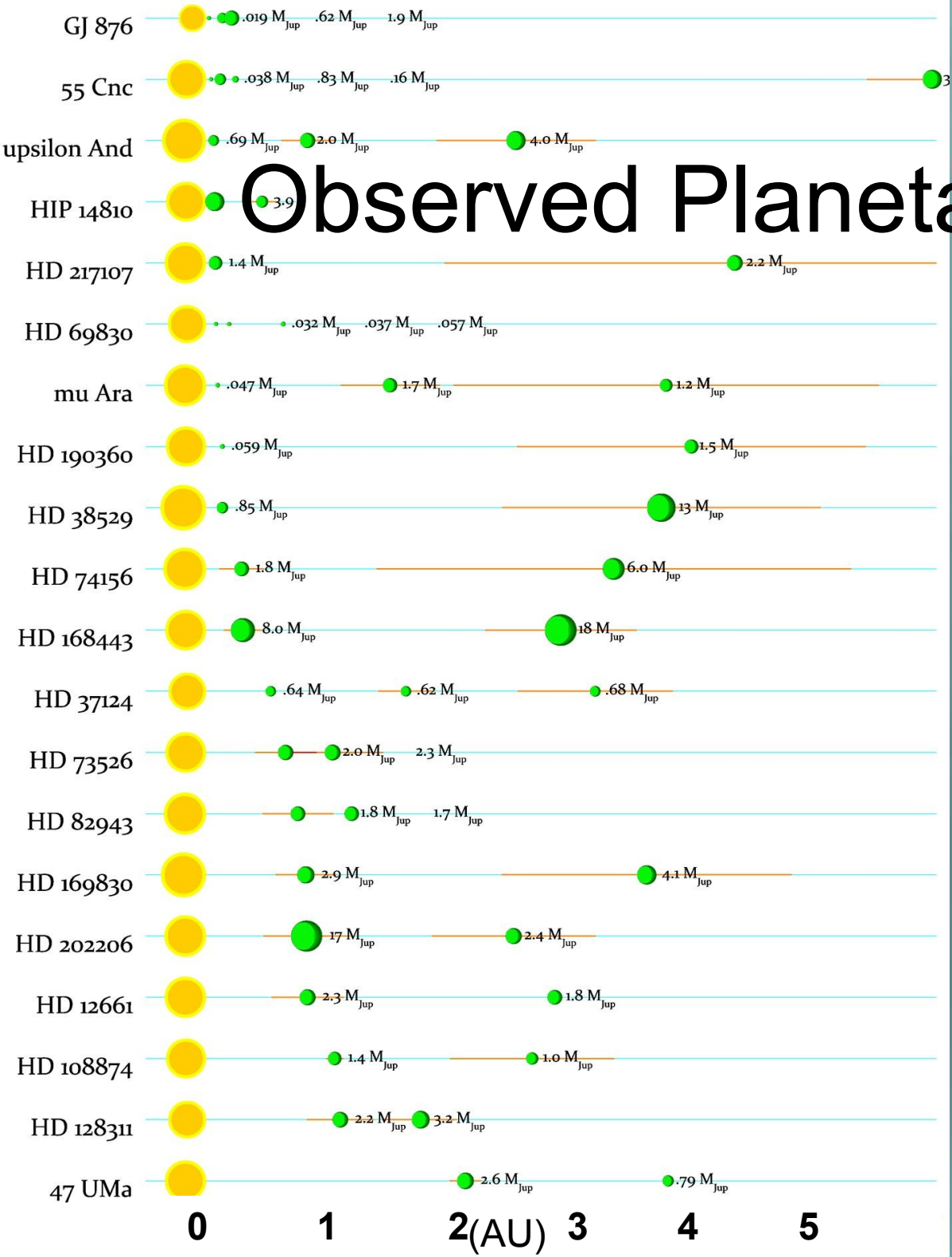
1543: Copernicus: *Revolutionibus*  
1576: Digges: Universe infinite?  
1600: Bruno burned  
1604: Kepler's Supernova  
1609: Galileo's telescope  
1618: Kepler's 3<sup>rd</sup> law

1687: Newton: *Principia*  
1698: Huygens: Distance to Sirius  
1755: Kant on planet formation  
1781: Herschel: Uranus  
1796: Laplace on planet formation

1838: Parallax measured  
1846: Adams & Le Verrier: Neptune

1925: Hubble: Cepheids in "nebulae"  
1926: Eddington: Sun's energy  
1930: Tombaugh: Pluto

# Observed Planetary Systems



1993: PSR B1257+12

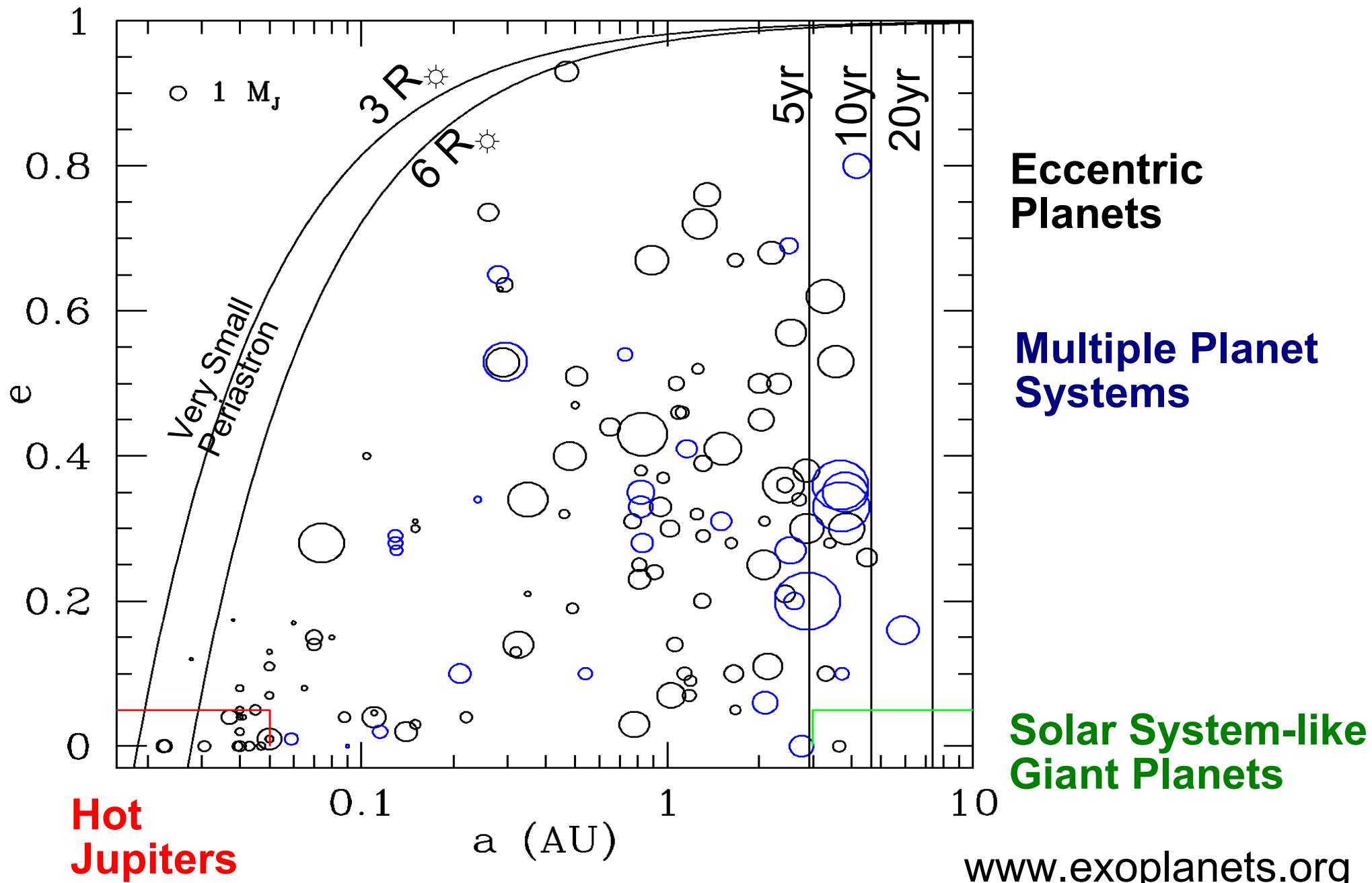
1995: 51 Pegasi

1999: Upsilon Andromedae  
2000: ~50 Planetary Systems

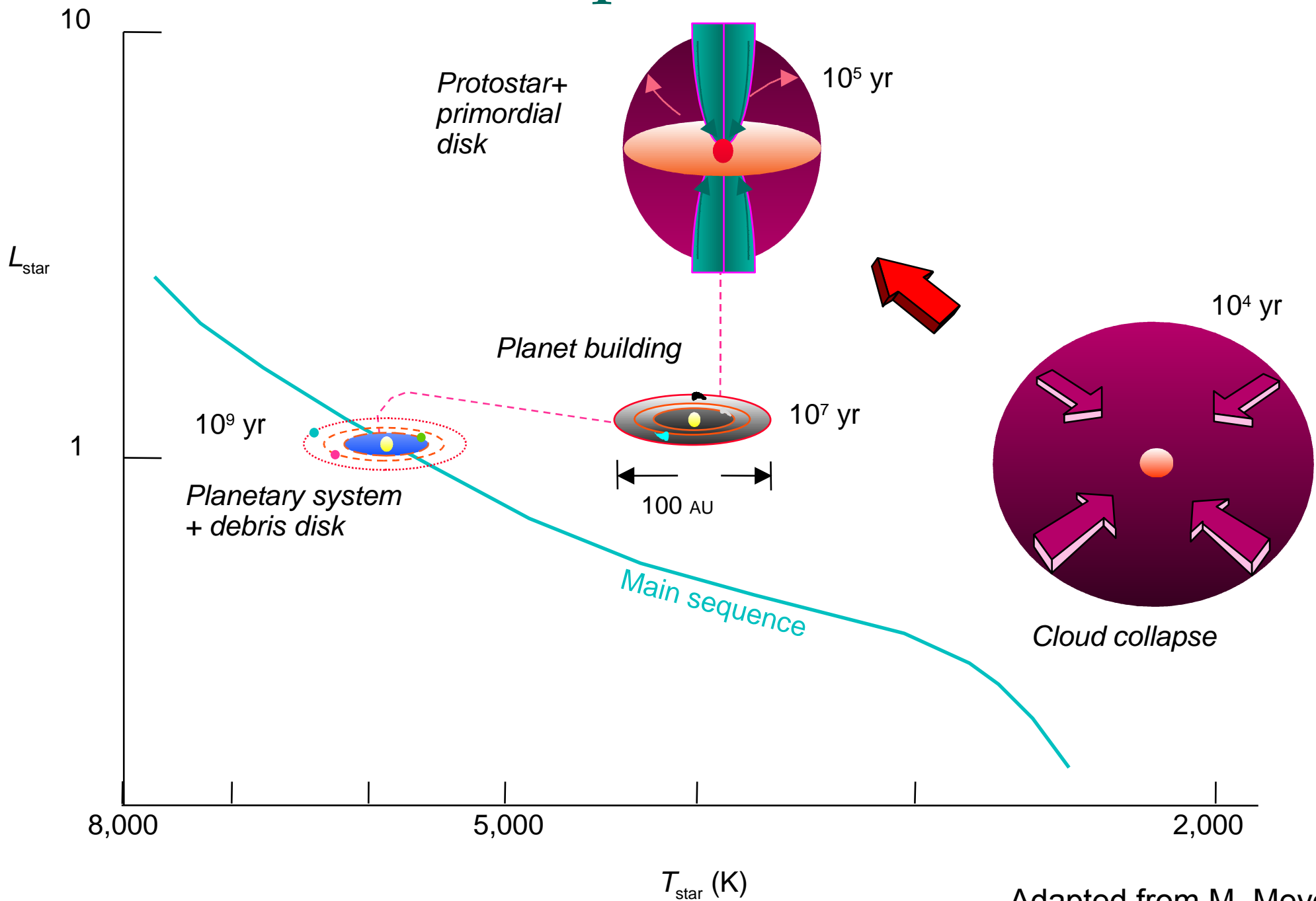
2006: ~147 Planetary Systems  
2007: ~200 Planetary Systems



# Diversity of Extrasolar Planets

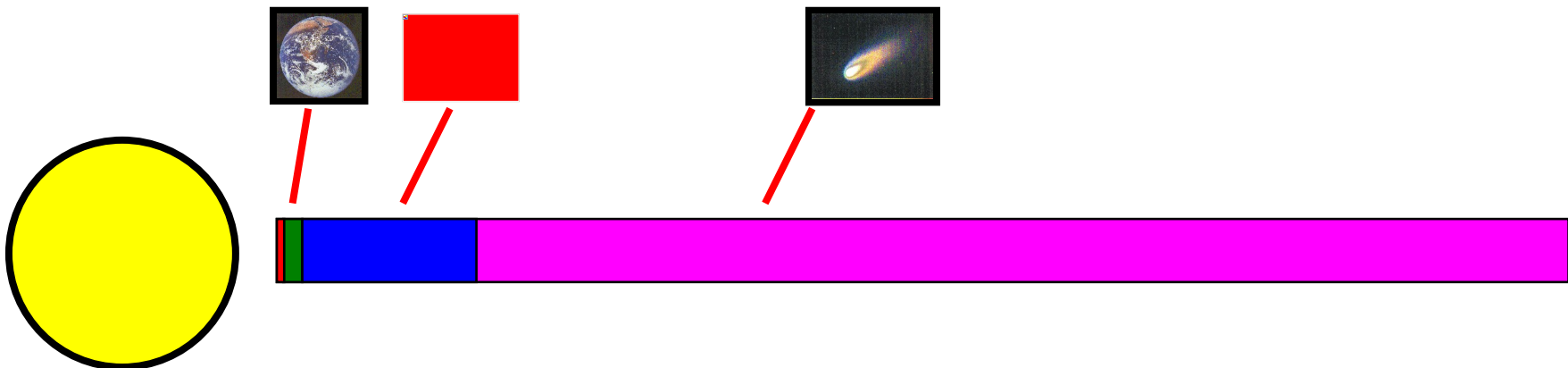
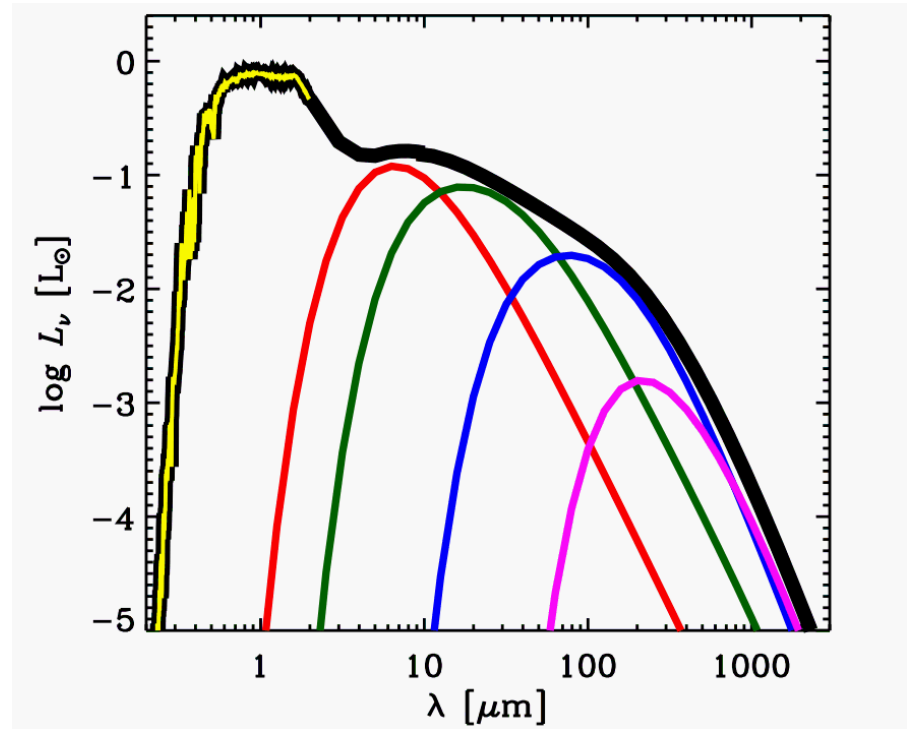


# Pre-main Sequence Evolution



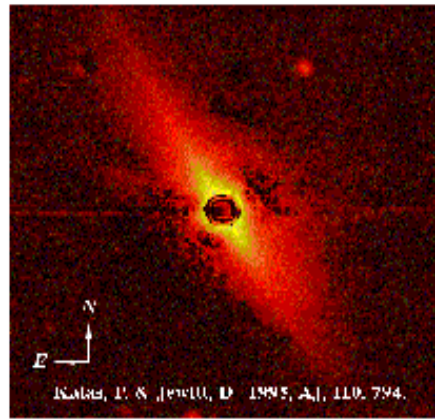
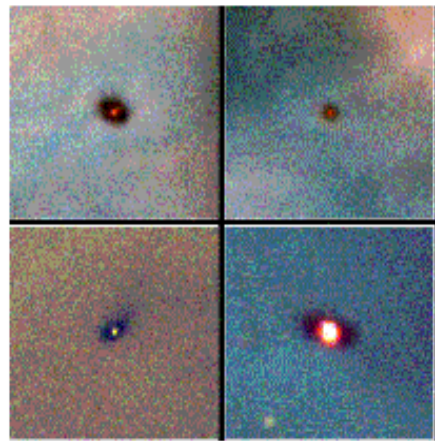
*SED*: thermal emission from irradiated thin dust disk

different disk regions contribute at different  $\lambda$  based on local temperature and density conditions

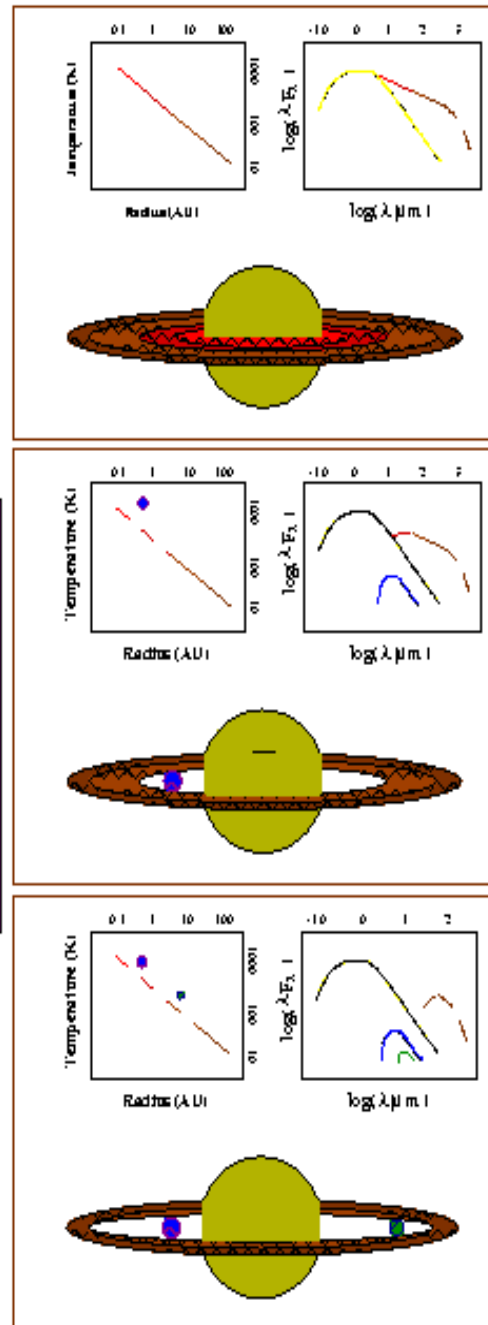




# From Protostellar Disks to Mature Planetary Systems



gas giant formation  
terrestrial planet formation



## Primordial Disks:

- gas rich
- opacity is dominated by primordial grains.

## Transition Disks:

- very short time scale
- planetesimals grow

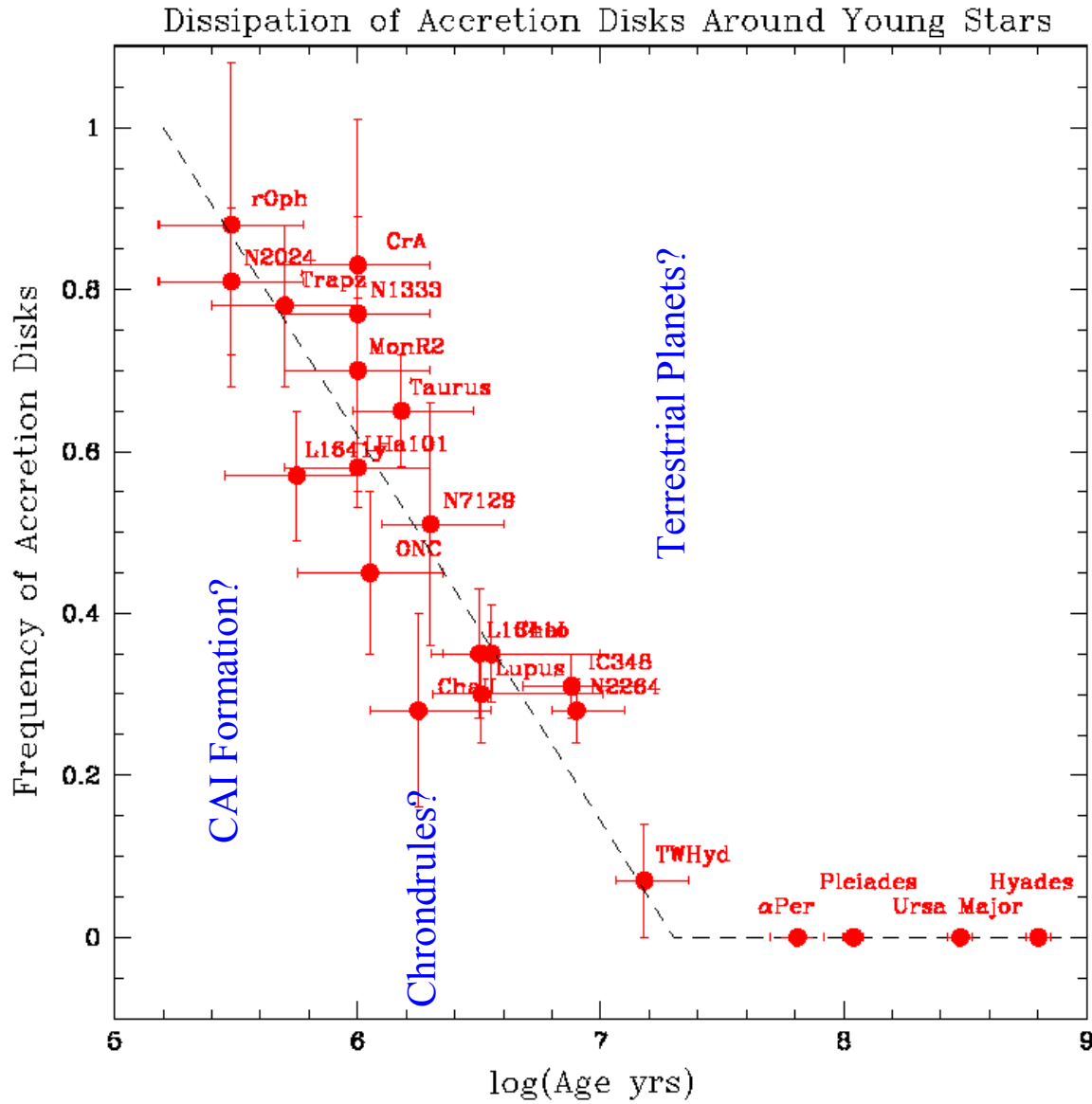
## Debris disks:

- no detection of gas
- Poynting-Robertson (P-R) drag time scale is shorter than the age of system, therefore pristine grains in a disk had been spiraled into the star. Therefore, we expect no residual ISM dust left over from formation.
- opacity is dominated by 2<sup>nd</sup> generation grains produced by collisions of planetesimals.

See recent review by Meyer et al. (2006).



# NIR Excess Fraction (< 0.1 AU) vs. Cluster Age

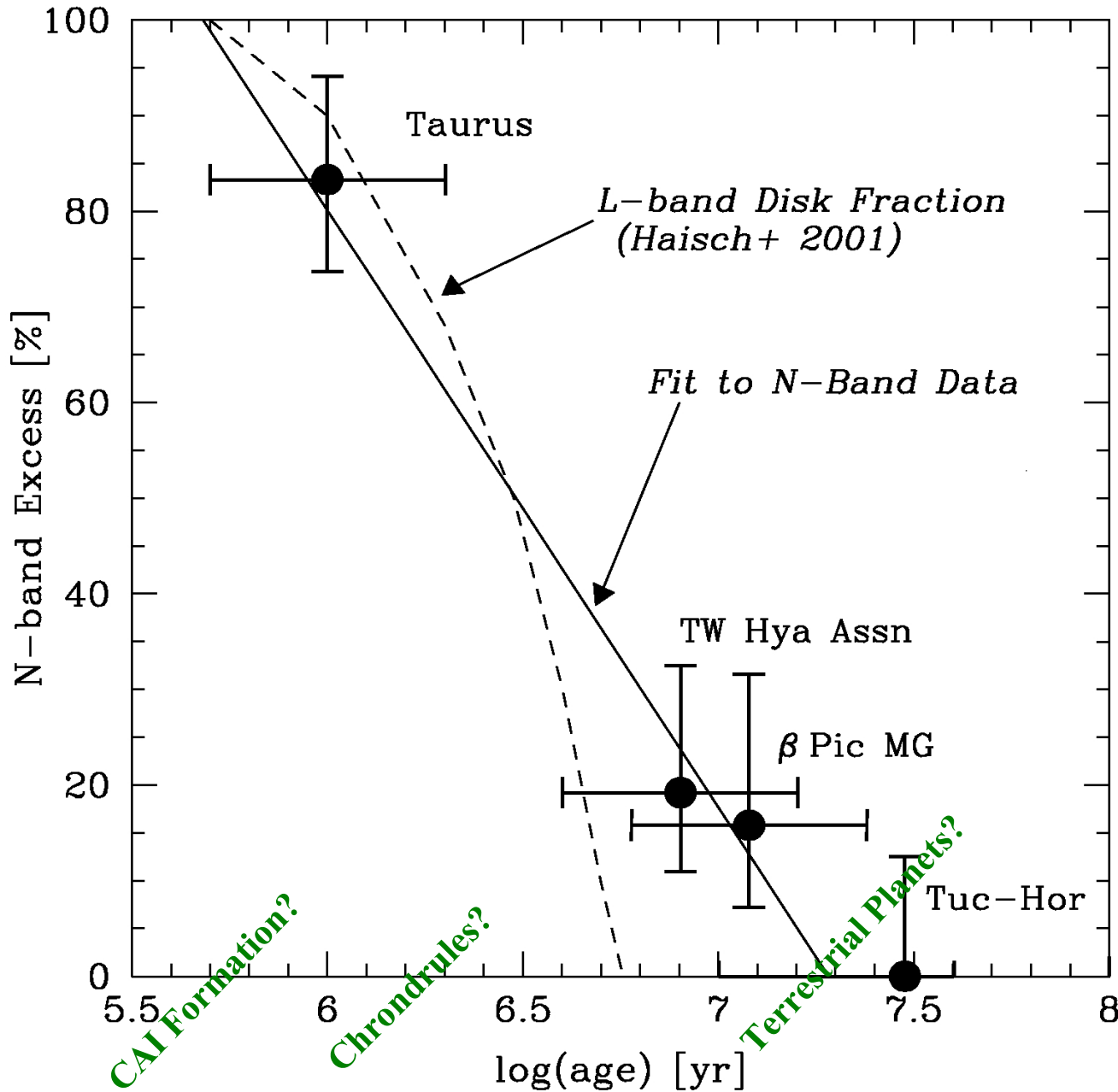


Haisch et al. 2001; see also Hillenbrand, Meyer, and Carpenter (2002).

# MIR Excess (0.3-1.0 AU) vs. Cluster Age



MIR



Dust in terrestrial planet zone dissipates when accretion stops!

Mamajek et al 2004, ApJ.

Metchev, Hillenbrand, and Meyer, 2004, ApJ.

See also Low et al. (2005) as well as Chen et al. (2005).

Adapted from M. Meyer

# The brown dwarf hypothesis

- extrasolar “planets” are simply very low-mass stars that form from collapse of multiple condensations in protostellar clouds
- distribution of eccentricities and periods of extrasolar planets very similar to distributions for binary stars
- but:
  - why is there a brown-dwarf desert?
  - how did planets in solar system get onto circular, coplanar orbits?
  - how do you make planets with solid cores, or terrestrial planets?

# The nebular hypothesis

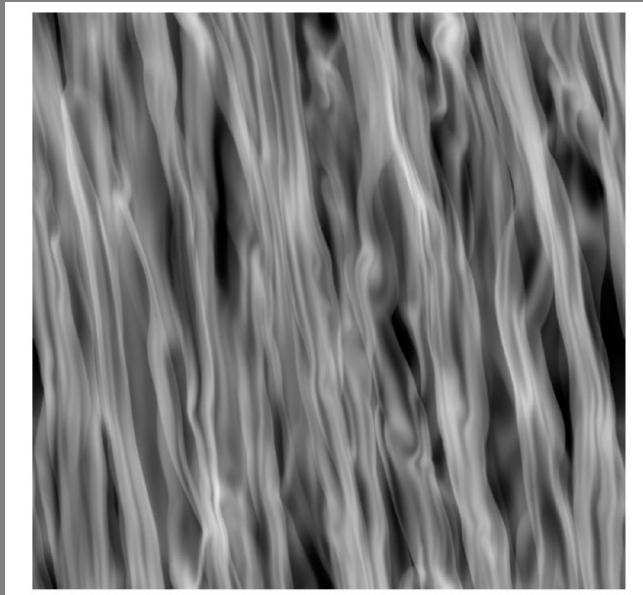
- the Sun and planets formed together out of a rotating cloud of gas (the “solar nebula”)
- gravitational instabilities in the gas disk condense into planets (Kant 1755)
- Good points: variations might work to form Jupiter, Saturn, extrasolar gas giants
- Bad points: how do you make Uranus, Neptune, terrestrial planets?

## Disk fragmentation

Gammie (2001) showed that for fragmentation to set in one needs

$$\Omega t_c < 3$$

$\Omega t_c = 50$  No fragmentation



Gammie '01

2D hydro

$\Omega t_c = 2$  Fragmentation



When  $t_c \sim \Omega^{-1}$  fragments lose thermal support at the same rate at which they collapse. Isothermal gas effectively has  $t_c = 0$

3D simulations confirm this general picture

$$(\Omega t_c < 3.- 5)$$

Rice et al 2003

Adapted from R. Rafikov

# The core accretion hypothesis

- forming Sun is surrounded by a gas disk (like nebular hypothesis)
- planets form by multi-stage process:
  1. as the disk cools, rock and ice grains condense out and settle to the midplane of the disk – chemistry and gas drag are dominant processes
  2. small solid bodies grow from the thin dust layer to form km-sized bodies (“planetesimals”) - gas drag, gravity and chemical bonding are dominant processes
  3. planetesimals collide and grow – gravitational scattering and solar gravity are dominant processes. “Molecular chaos” applies and evolution is described by statistical mechanics

requires growth by ~45 orders of magnitude in mass through ~6 different physical processes!

# Challenges of Planet Formation

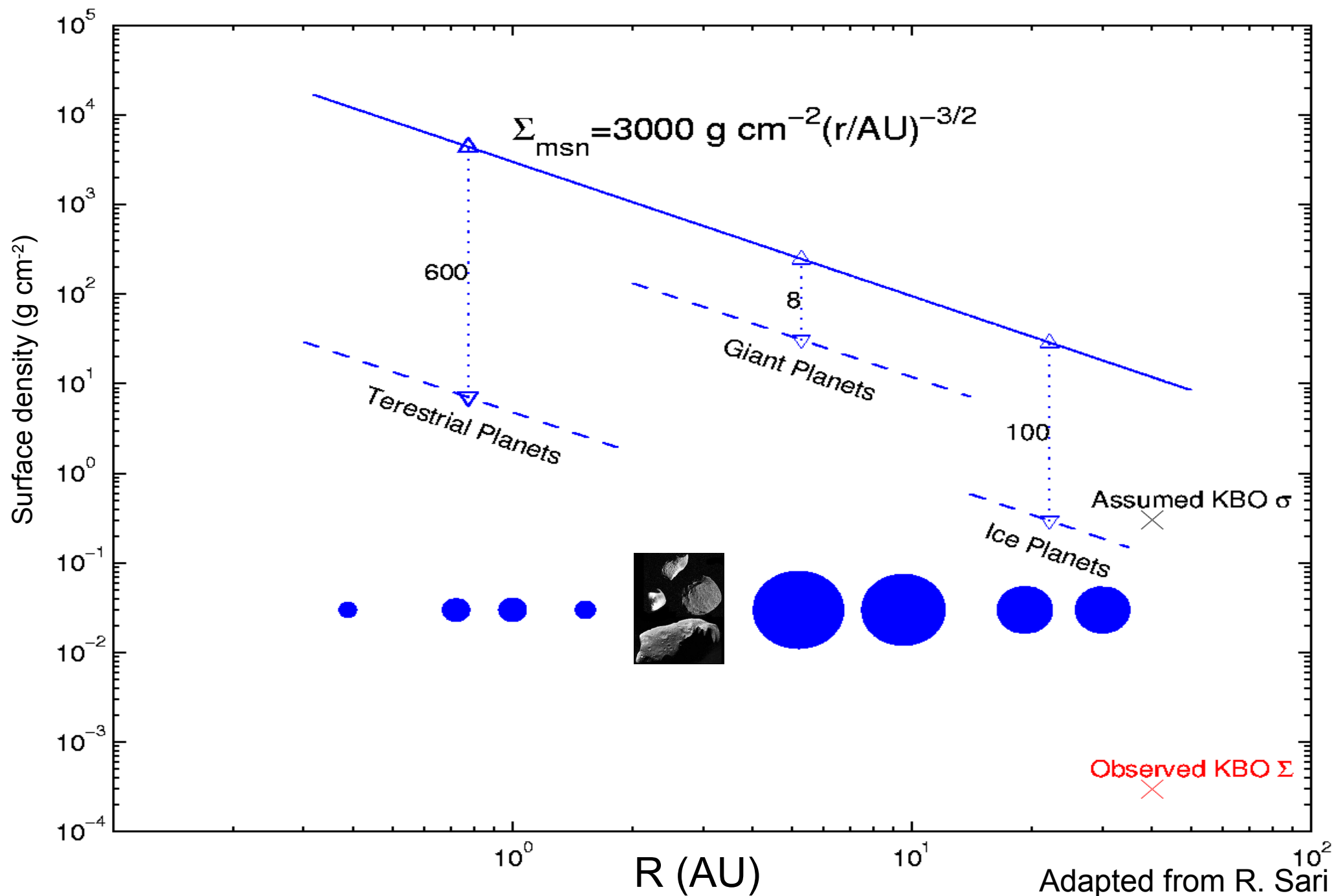
- Planetesimals susceptible to very rapid inward migration.
- Collisions need to result in net accretion.
- Cores susceptible to rapid inward migration
- Giant planets must form before gas dissipates
- Uranus & Neptune must form in less than age of solar system



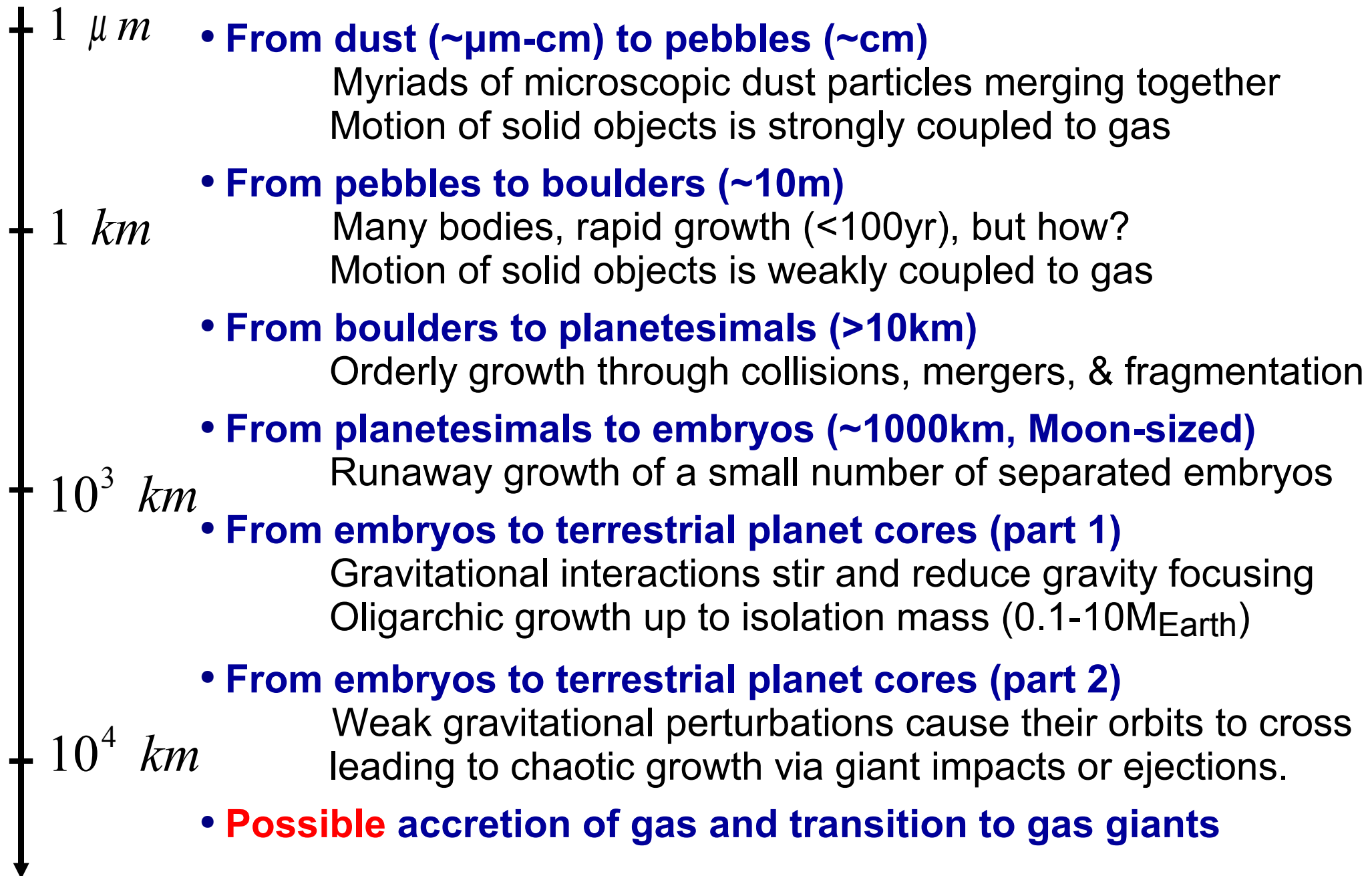
# Processes in Planet Formation

- Condensation of grains from Solar nebular (complicated physics & chemistry)
- Planetesimal Formation (highly uncertain)
- Migration (Type I, II, III)
- “Simple” Accretion
  - Chaotic Growth
  - Oligarchic Growth
  - Orderly Growth
  - Runaway Growth

# Minimum Mass Solar Nebula



# Stages of Planet Formation by Core Accretion



## From pebbles to boulders

Very poorly understood! Potential planetesimal formation mechanisms:

- **Gravitational instability** (Goldreich & Ward 1973; Youdin & Shu 2002)

Dust sediments towards midplane, forms dense layer, becomes gravitationally unstable.

1-10 km size bodies form on dynamical (about 100 yr) timescale.

??? Can dust really sediment? What is the role of turbulence in the disk?

- **Coagulation of dust particles** (Weidenschilling & Cuzzi 1993)

Dust particles collide with each other and stick ensuring growth.

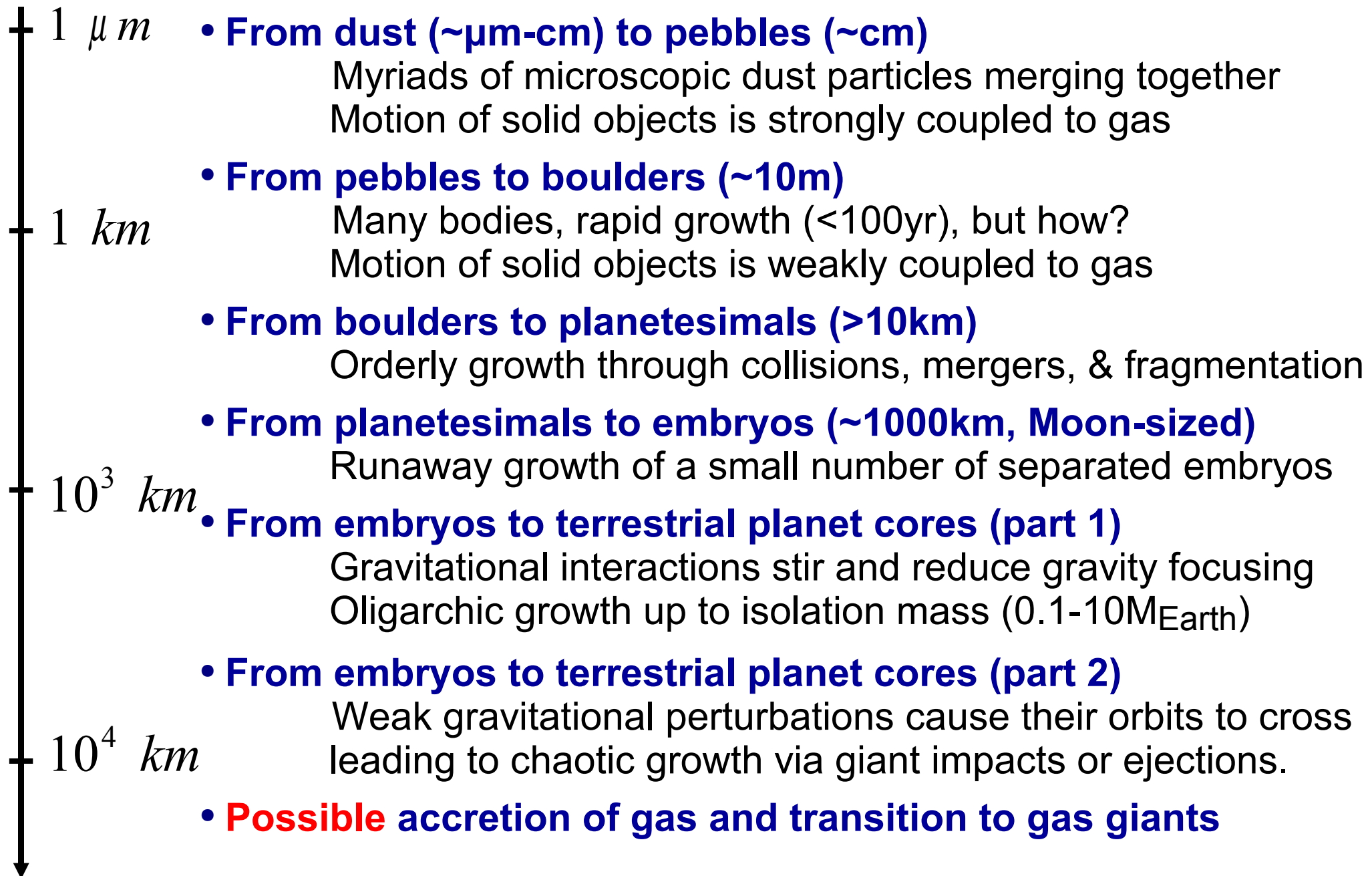
1 m bodies grow in less than 10,000 yr **if** 100% sticking probability.

??? Sticking mechanism is **very** unclear. Collisions may occur at high velocities leading to dust fission rather than fusion.

- **“Exotic” mechanisms: vortices, turbulent concentration, etc.**

??? Do these work at all?

# Stages of Planet Formation by Core Accretion



## From planetesimals to Moon-size “embryos”

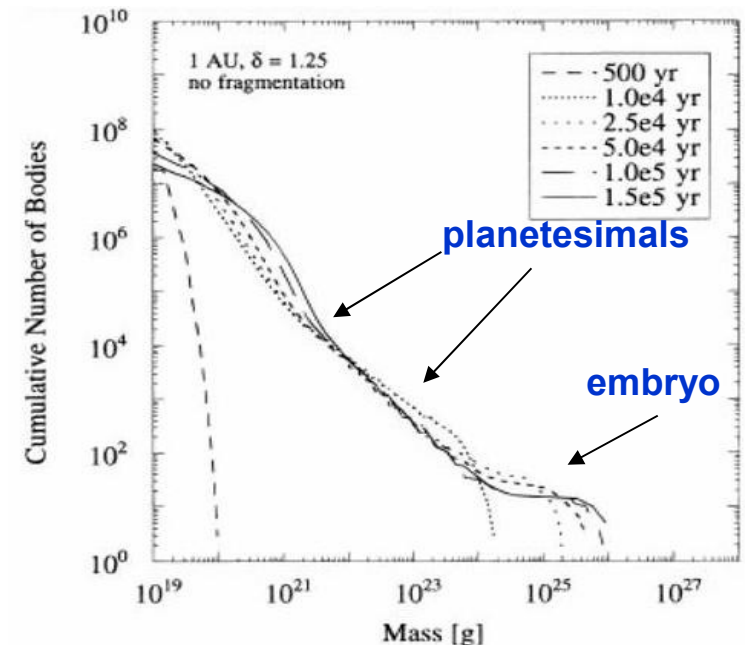
### Features of this evolutionary stage:

- Many planetesimals ( $\approx 10^{12}$  within 1 AU); orbits overlap.
- Mutual gravitational perturbations excite their eccentricities and inclinations -energy gets pumped from circular orbital motion into random motion.
- Low-velocity collisions lead to mergers and planetesimal grows, high velocity collisions cause erosion and fragmentation
- System evolves under simultaneous action of all these processes

Because of the huge number of bodies involved, **kinetic theory** should be employed to study planetesimal agglomeration, including both **mass** and **velocity** evolution.

**Direct N-body simulations** can also probe **spatial** evolution but they are very limited.

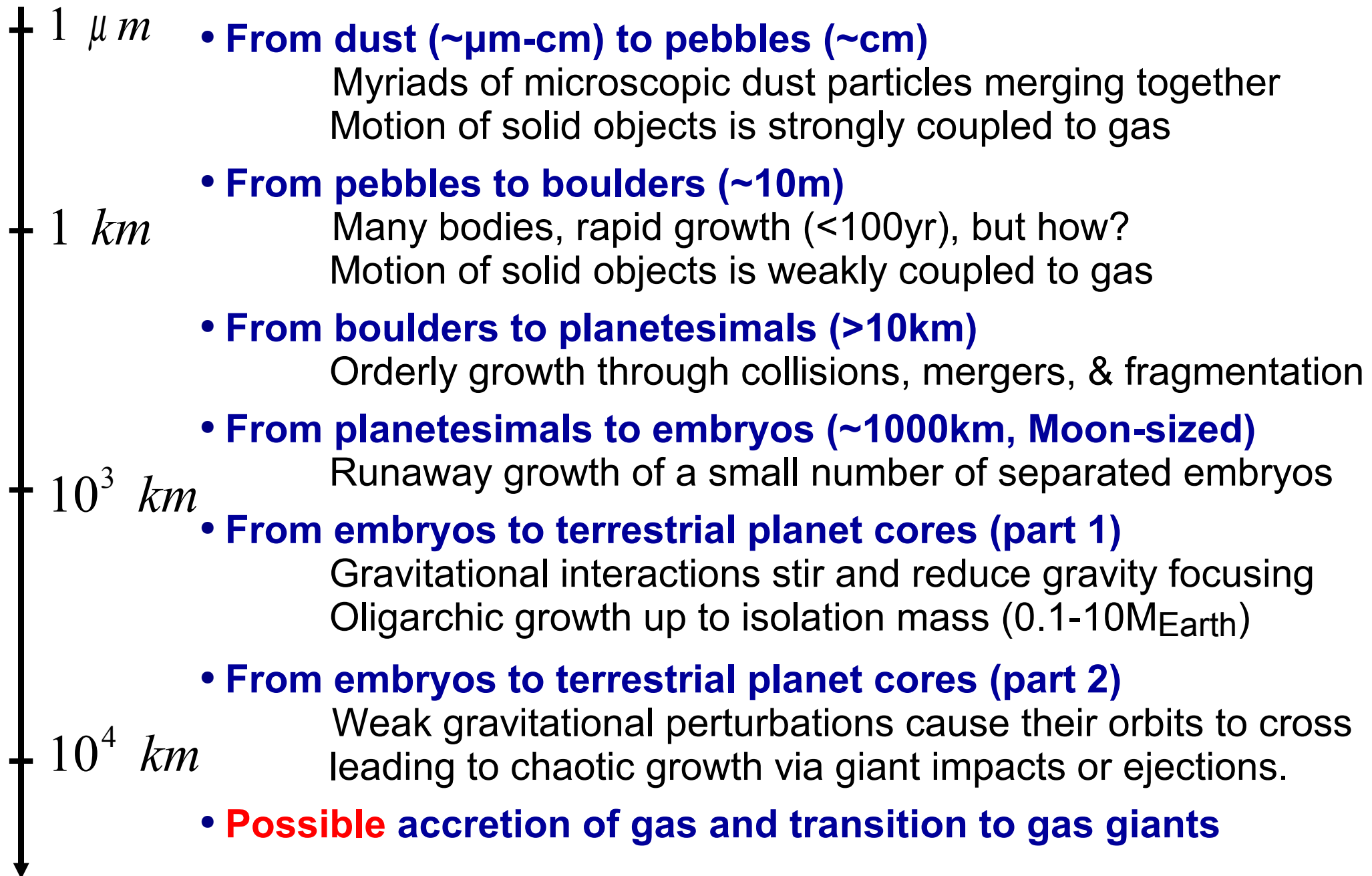
**Particle-in-a-box simulations** (modeling disk as a “gas” of gravitating particles) demonstrate growth up to  $10^{26}$  g in  $10^5$  yr at 1 AU – **Moon-size embryos in the terrestrial region.**



(Kenyon & Luu 1998)

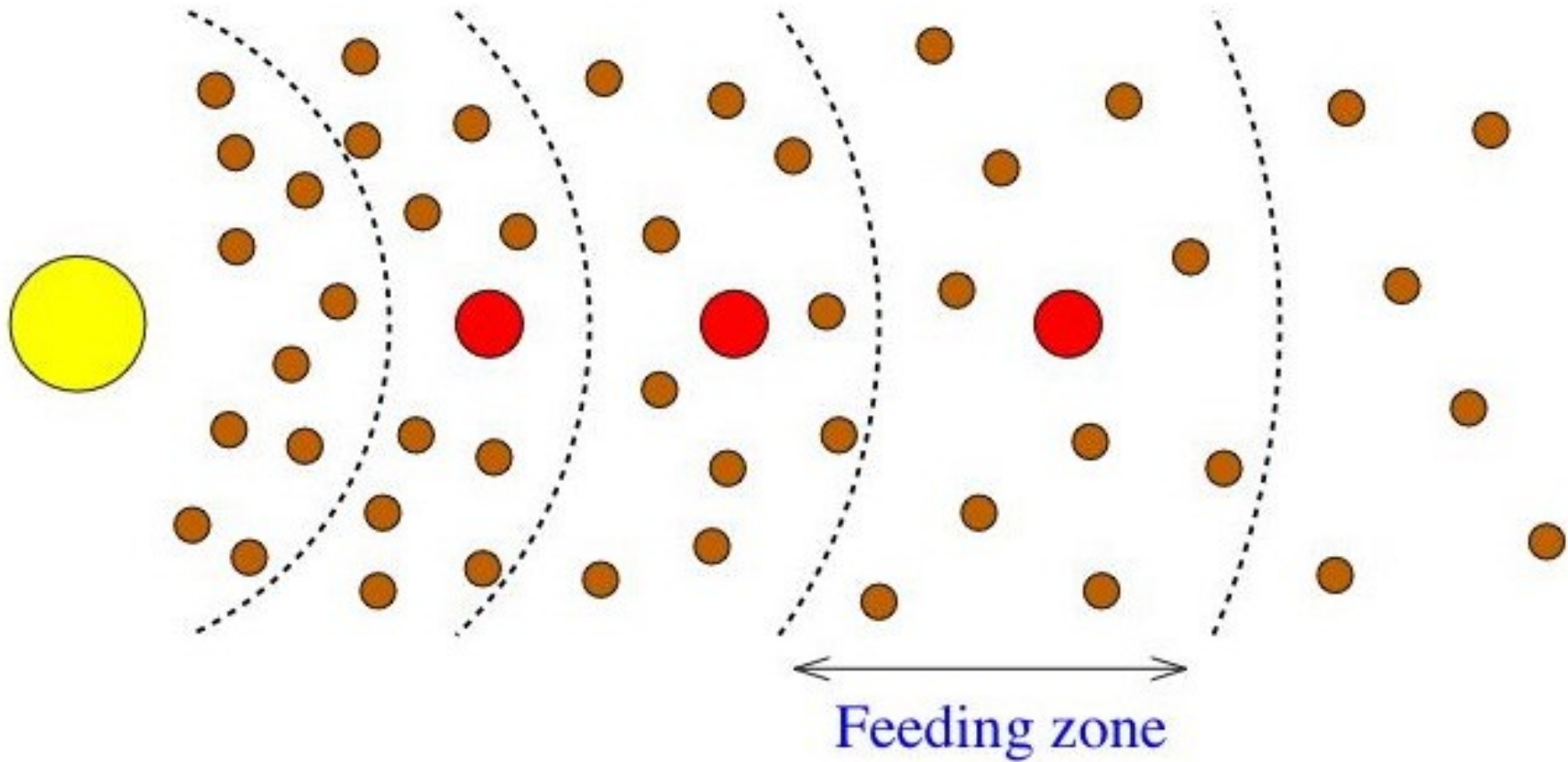
Adapted from R. Rafikov

# Stages of Planet Formation by Core Accretion

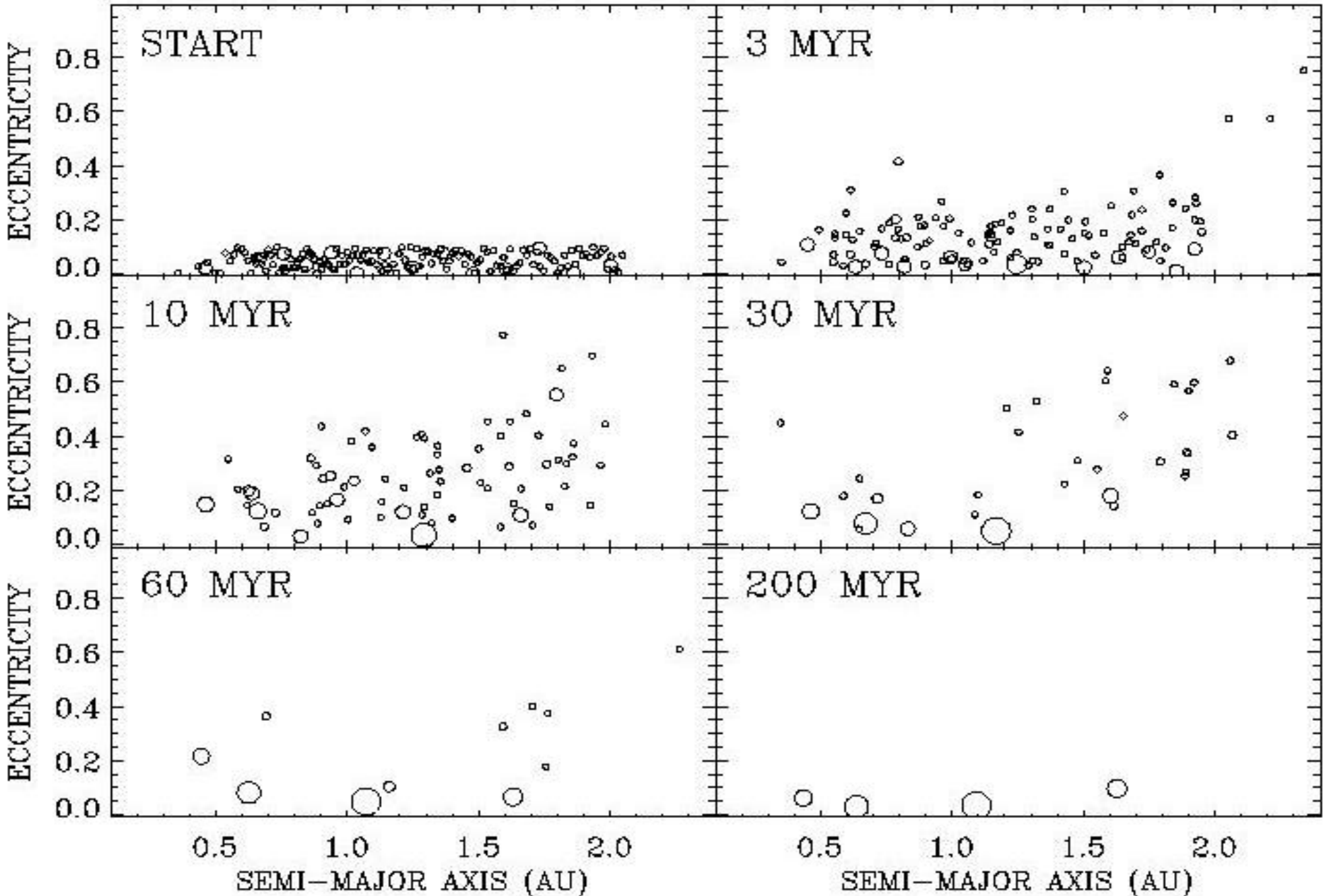




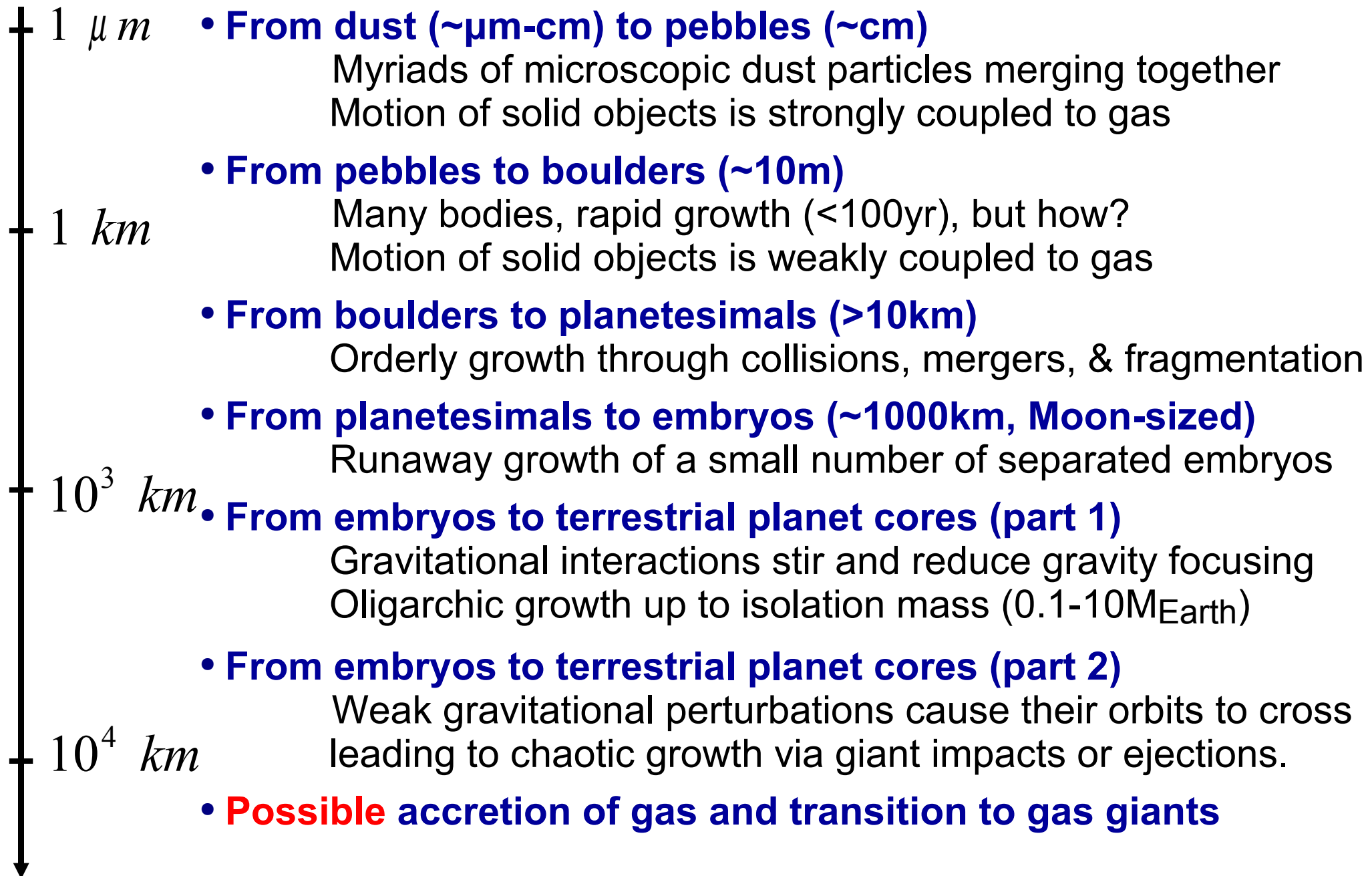
# Oligarchic Growth



# Embryos to Terrestrial Planets (Sun-Jupiter-Saturn)

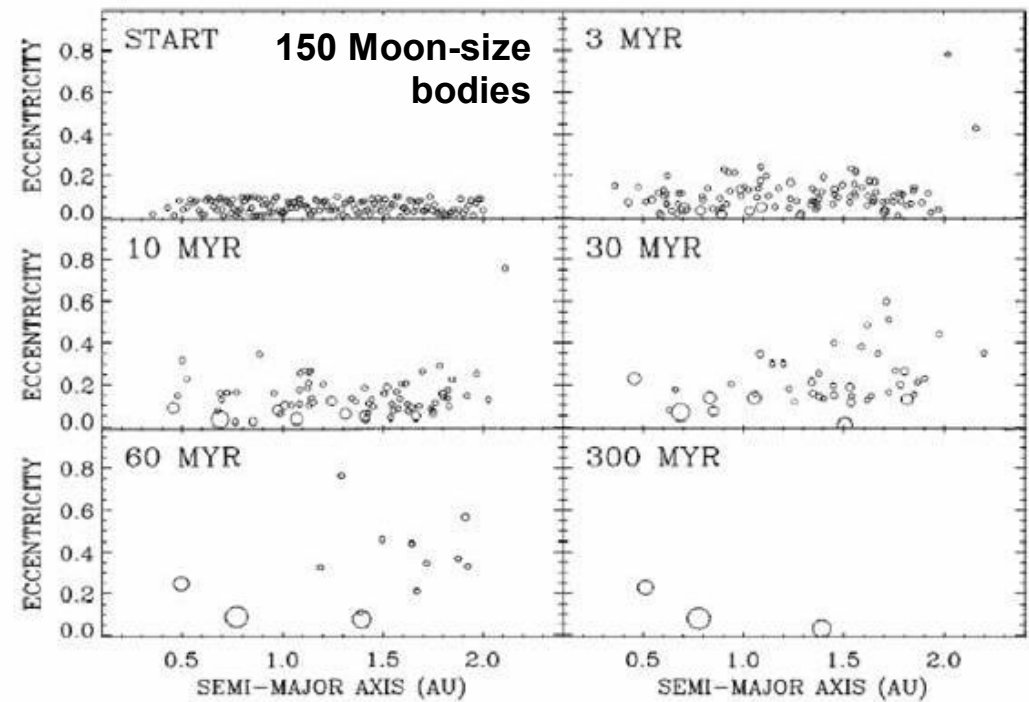


# Stages of Planet Formation by Core Accretion



## From Moon-size embryos to fully-grown planets

- Spatially widely separated embryos gravitationally excite each other into **crossing orbits**
- Bigger bodies form in **catastrophic collisions** in about  $10^8$  years in the inner Solar System



**Evidence:**

**Chambers 2001**

- **Earth-Moon system**: giant impact about 30 million yrs after Earth formed.
- Planetary **obliquities**

**???** Final dynamical state?

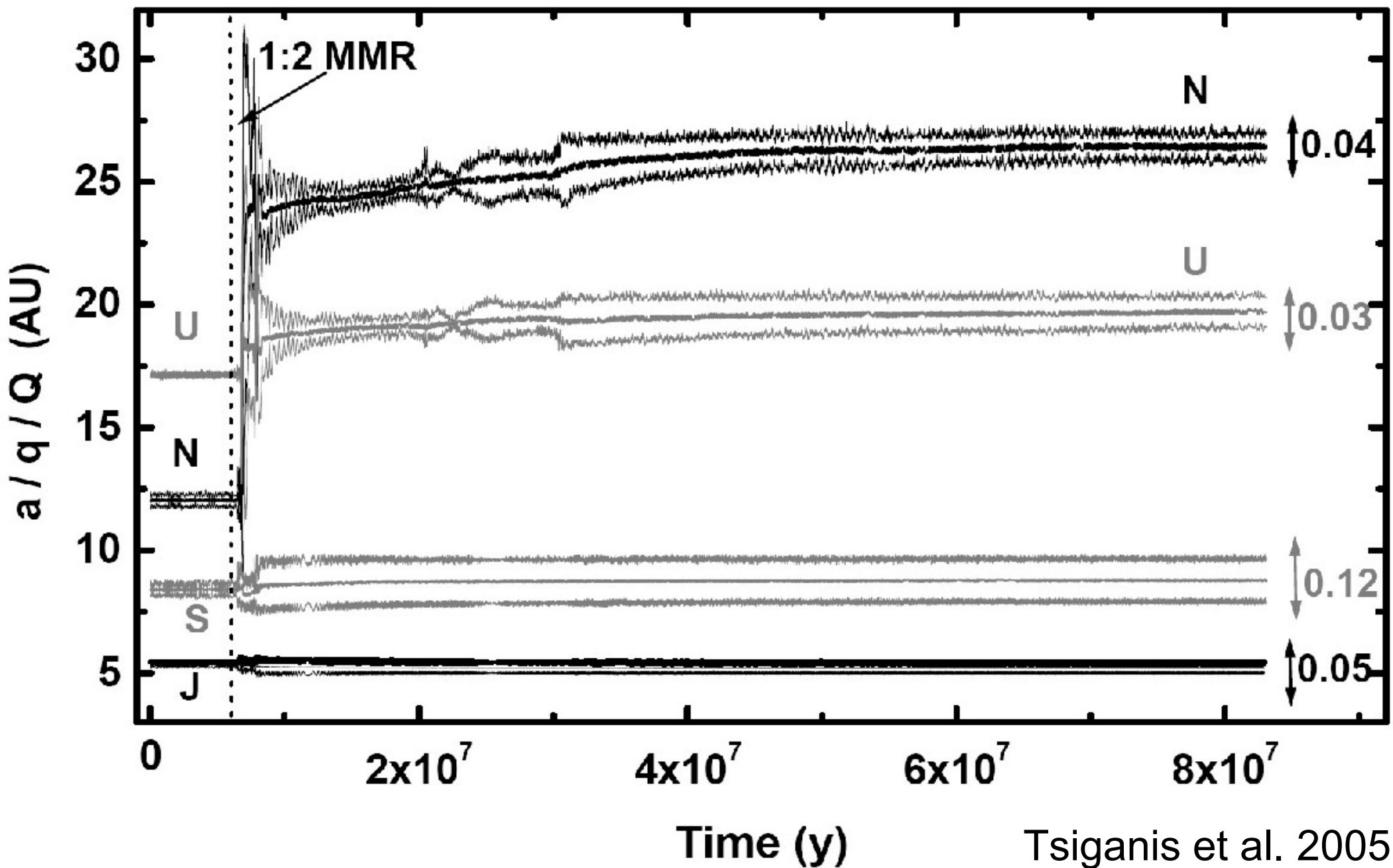
# Violence in the Solar System

- Mercury large density
- Mars-sized Earth-impactor created the Moon
- Giant planet's irregular satellites
- Saturn's large ring system
- Uranus's obliquity
- Neptune's retrograde moon Triton
- Excitation of Kuiper Belt

# Formation of Uranus & Neptune

- Problem: Standard timescale to accrete Neptune *in situ* at  $\sim 30$  AU exceeds 4 Gyr
- Possible Solutions:
  - a) Form Uranus and Neptune closer to Sun (Thommes et al. 1999; Tsiganis et al. 2005)
  - b) Majority of disk mass in small bodies, leading to more effective gravitational focusing and increased accretion rates (GLS = Goldreich et al. 2004)

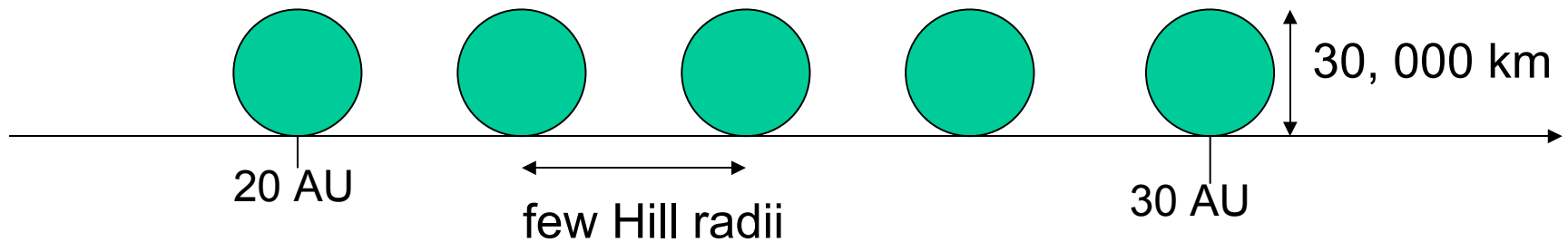
# Jupiter, Saturn, 2 Ice Giants + small bodies



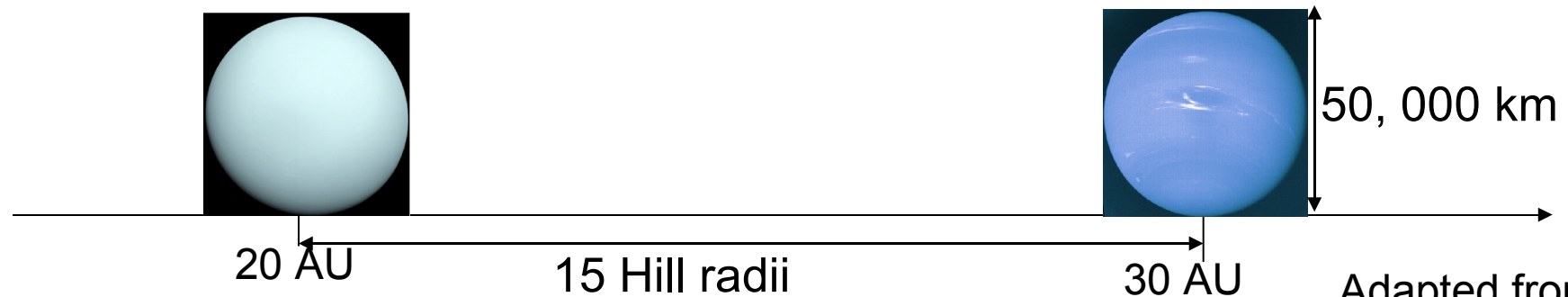


# Uranus & Neptune = End of Oligarchy?

- Formation time of Uranus & Neptune fast enough (10 Myr) if small bodies are very small ( $< 1\text{ m}$ ) and very cold ( $e < 0.05$ )
- In cold (sub Hill) accretion, might expect:



Observe:

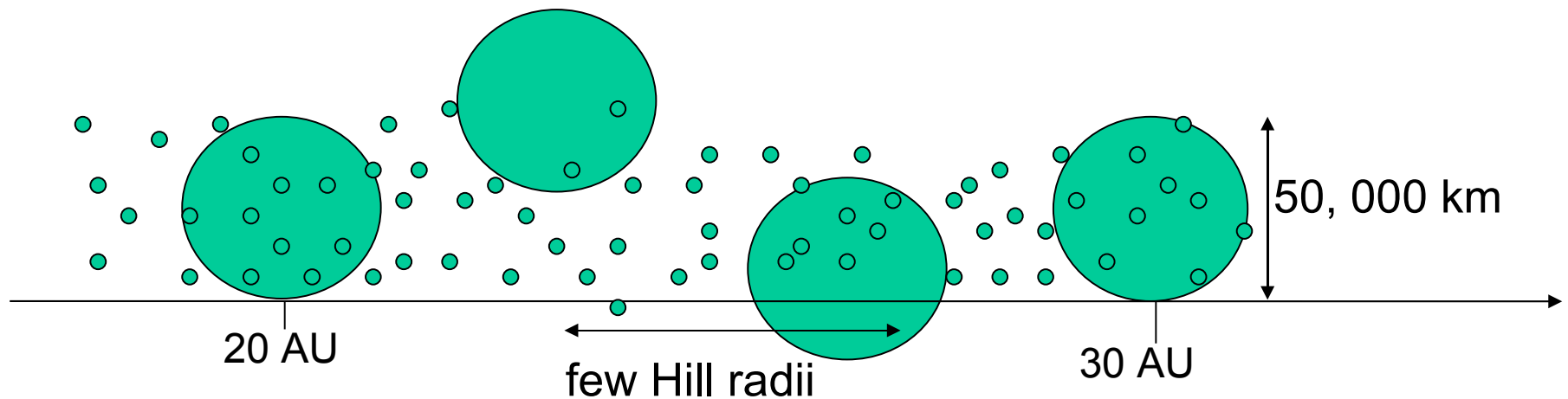


Adapted from R. Sari

# Uranus & Neptune: Beyond Isolation

- Isolation when  $\Sigma \sim \sigma$ .
- we assume  $u \sim v_H$

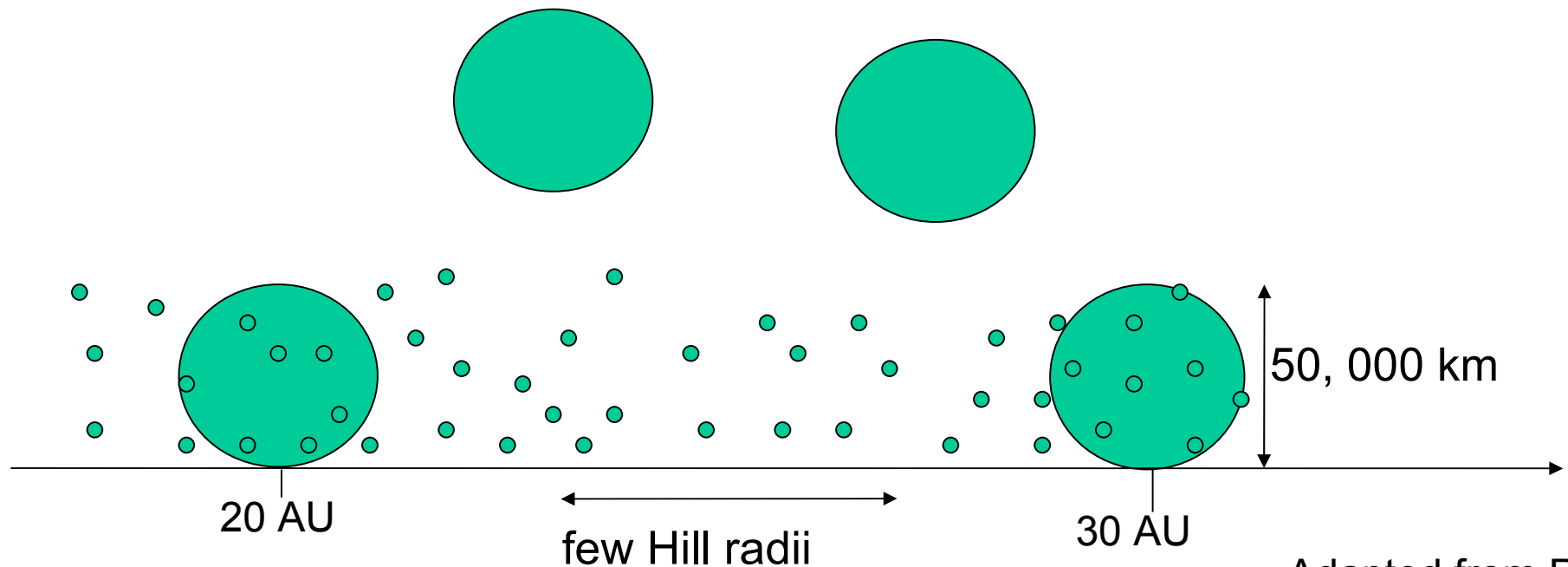
$$T_{\text{isolation}} \sim \Omega^{-1} \frac{\alpha \rho R}{\sigma} \sim 10 \text{ million years}$$



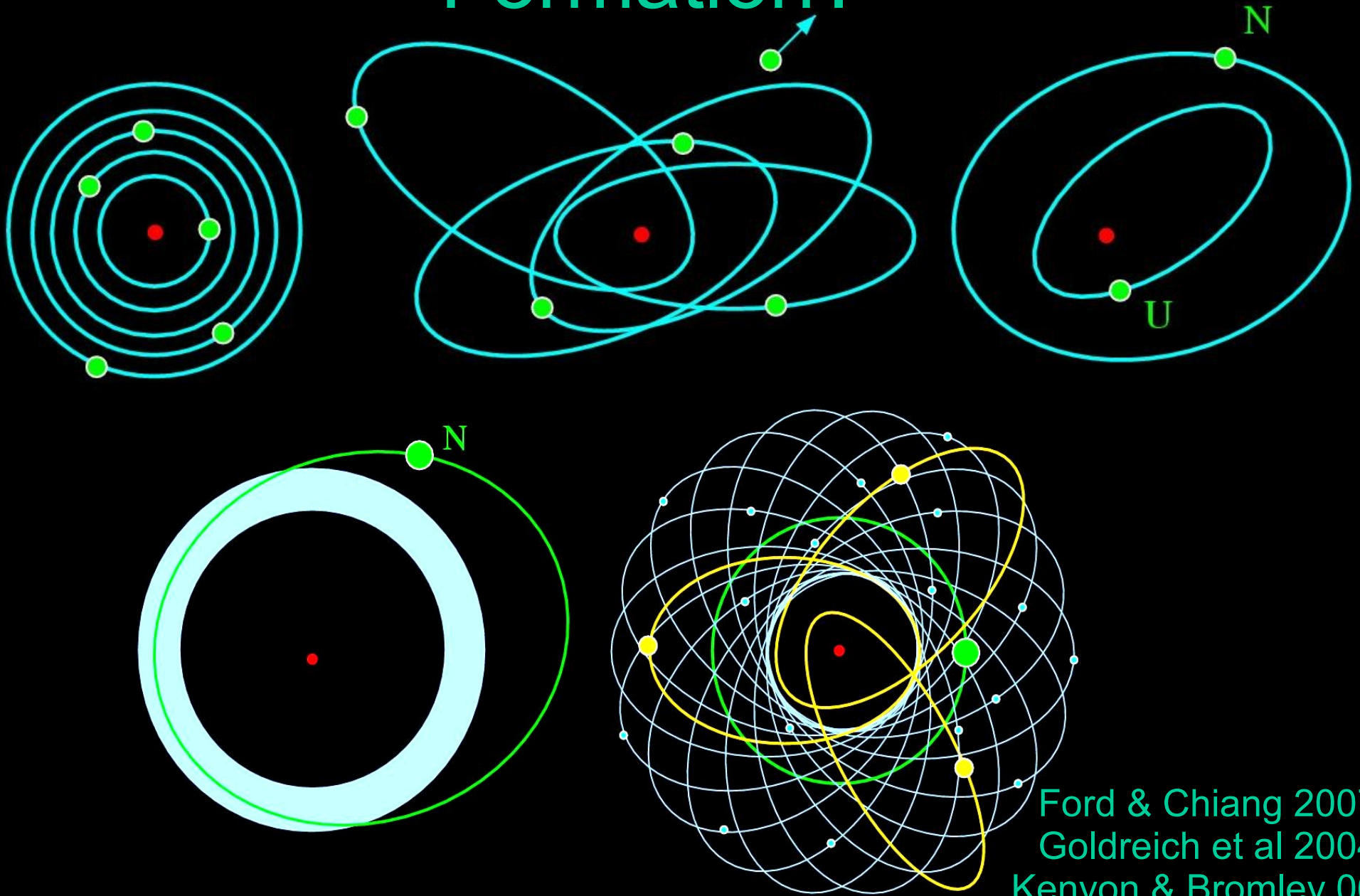
# Uranus & Neptune: Ejection

- After 10 million years,  $\Sigma > \sigma$
- Heating > Cooling  $\Rightarrow$  **runaway heating**
- Planets are ejected in time

$$T_{\text{eject}} \sim \frac{1}{10} \Omega^{-1} \left( \frac{M_{\odot}}{M_{\text{Neptune}}} \right)^2 \sim \text{billion years}$$



# Very Late Stages of Planet Formation?



Ford & Chiang 2007  
Goldreich et al 2004  
Kenyon & Bromley 06  
Thommes et al. 99, 02

# Sculpting of the Kuiper Belt

- Problem 2: How to excite Scattered Disk?
- Possible Solutions:
  - a) Migration & sweeping resonances (secular, Kozai & high-order mean-motion; Gomes et al. 2003ab)...  
But has very low efficiency,  $\sim 10^{-3}$
  - b) Stirring of scattered disk by oligarchs during chaotic stage (Chiang et al. 2006)...  
We will test this with simulations (Ford & Chiang 2007)

# Goals

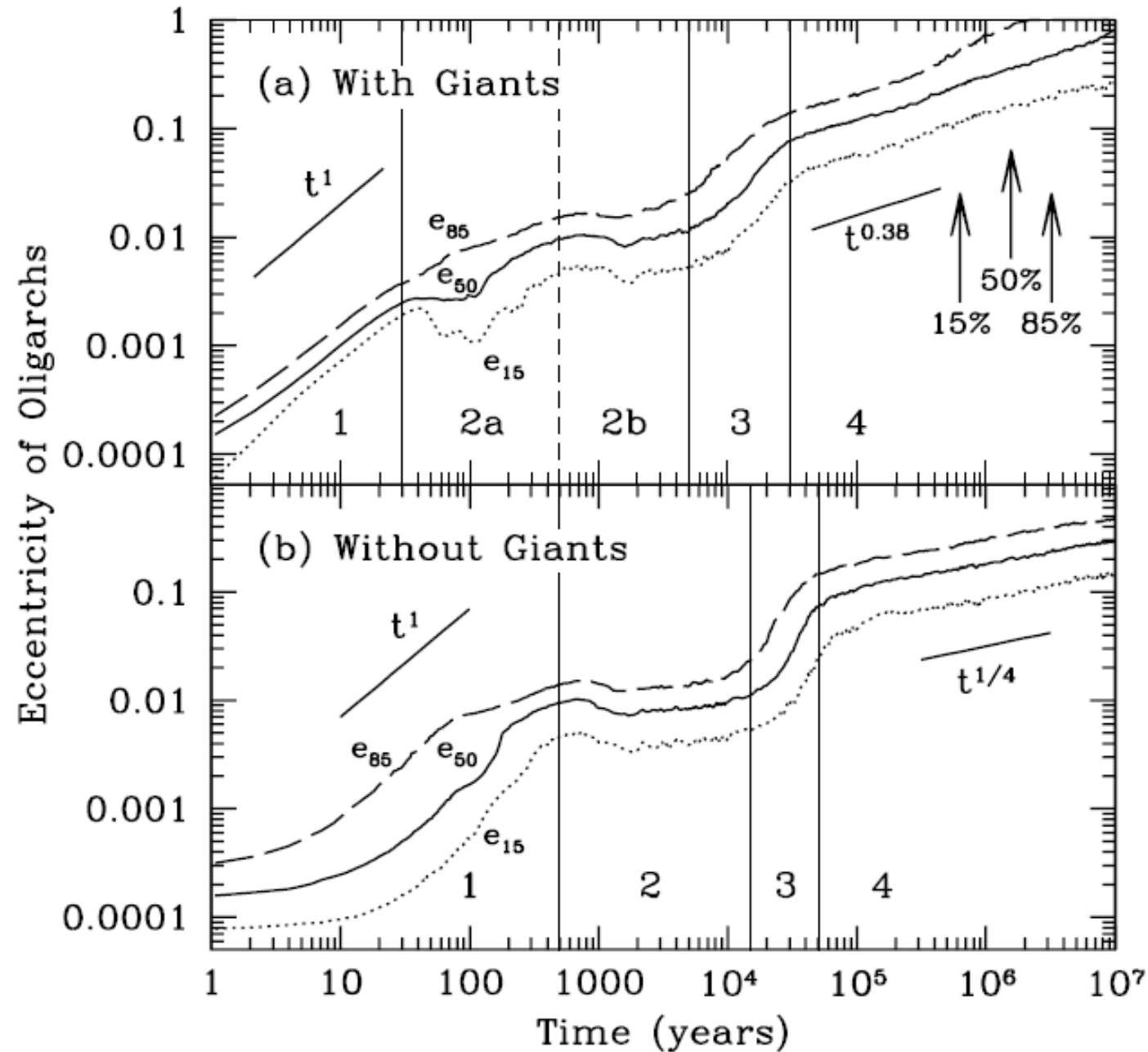
Test analytic predictions of GLS & C06 with numerical simulations. Will outcomes resembling our Solar System be common?

- Can 3 of 5 oligarchs be ejected?
- Where will remaining oligarchs be?
- Can their eccentricity/inclination be damped to observed values?
- Can scattered disk be created in the process?

# Our Model: Initial Conditions

- Jupiter & Saturn on current orbits:  $a_{\text{init}} = 5.18, 9.54$  AU
- 5 Neptune-mass Oligarchs:
  - $a_{\text{init}} = 15, 20, 25, 30, 35$  AU
  - $e_{\text{init}} = \sin(i_{\text{init}}) = 0.0001$

# Eccentricity Growth w/o Dissipation

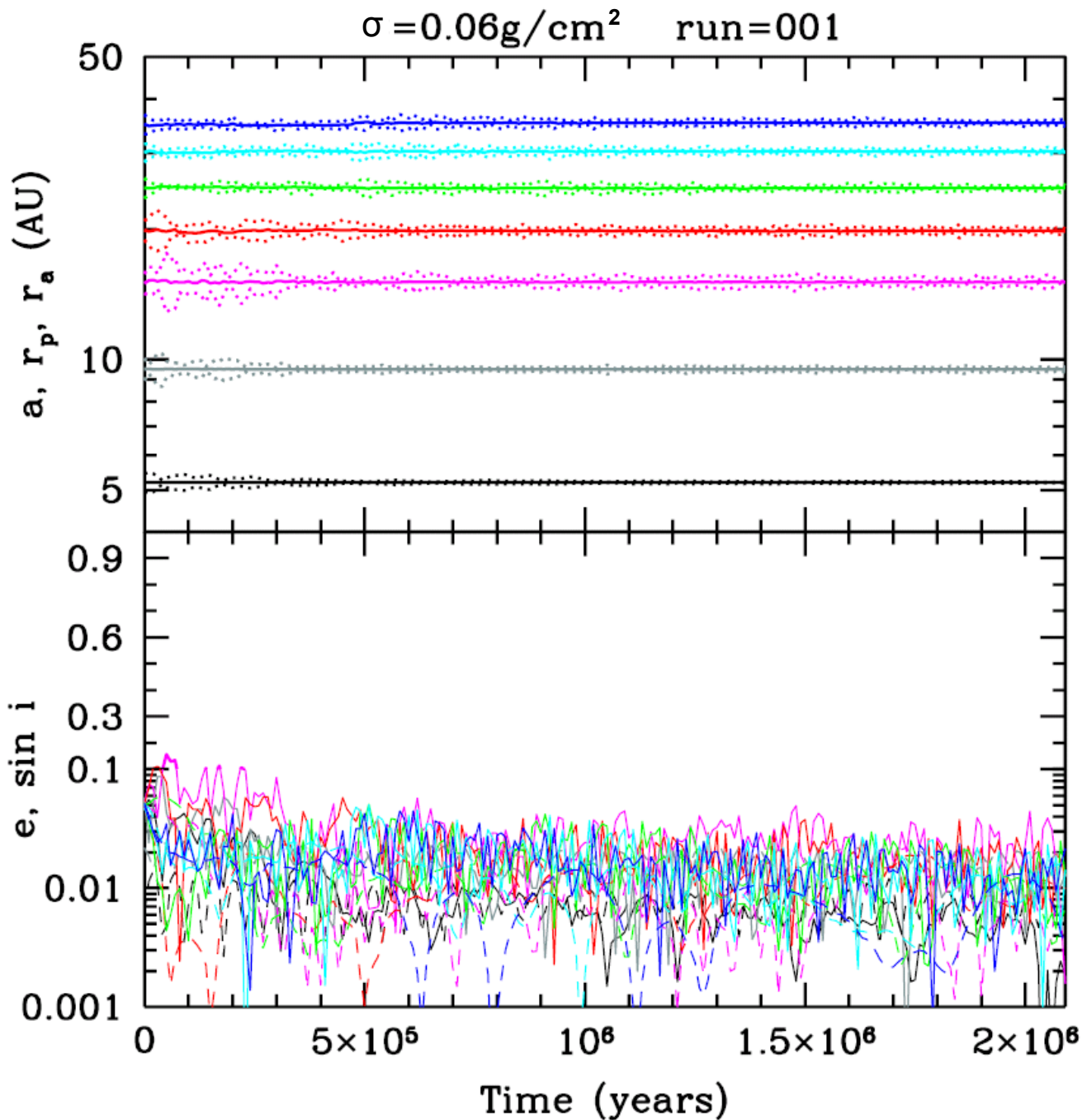




# Our Model: Initial Conditions

- Jupiter & Saturn on current orbits:  $a_{\text{init}} = 5.18, 9.54$  AU
- 5 Neptune-mass Oligarchs:
  - $a_{\text{init}} = 15, 20, 25, 30, 35$  AU
  - $e_{\text{init}} = \sin(i_{\text{init}}) = 0.05$
- Small bodies (static, constant  $\sigma$  disk):
  - $12.5 \text{ AU} < a < 45 \text{ AU}$
  - Interact with oligarchs only via dynamical friction
- Large ( $\sim 100\text{km}$ ) Kuiper Belt Objects
  - 400 test particles
  - $a_{\text{init}} = 40\text{-}45$  AU
  - $e_{\text{init}} = \sin(i_{\text{init}}) = 0.01$

# Full Simulations: $\sigma > 0.06 \text{ g/cm}^2$



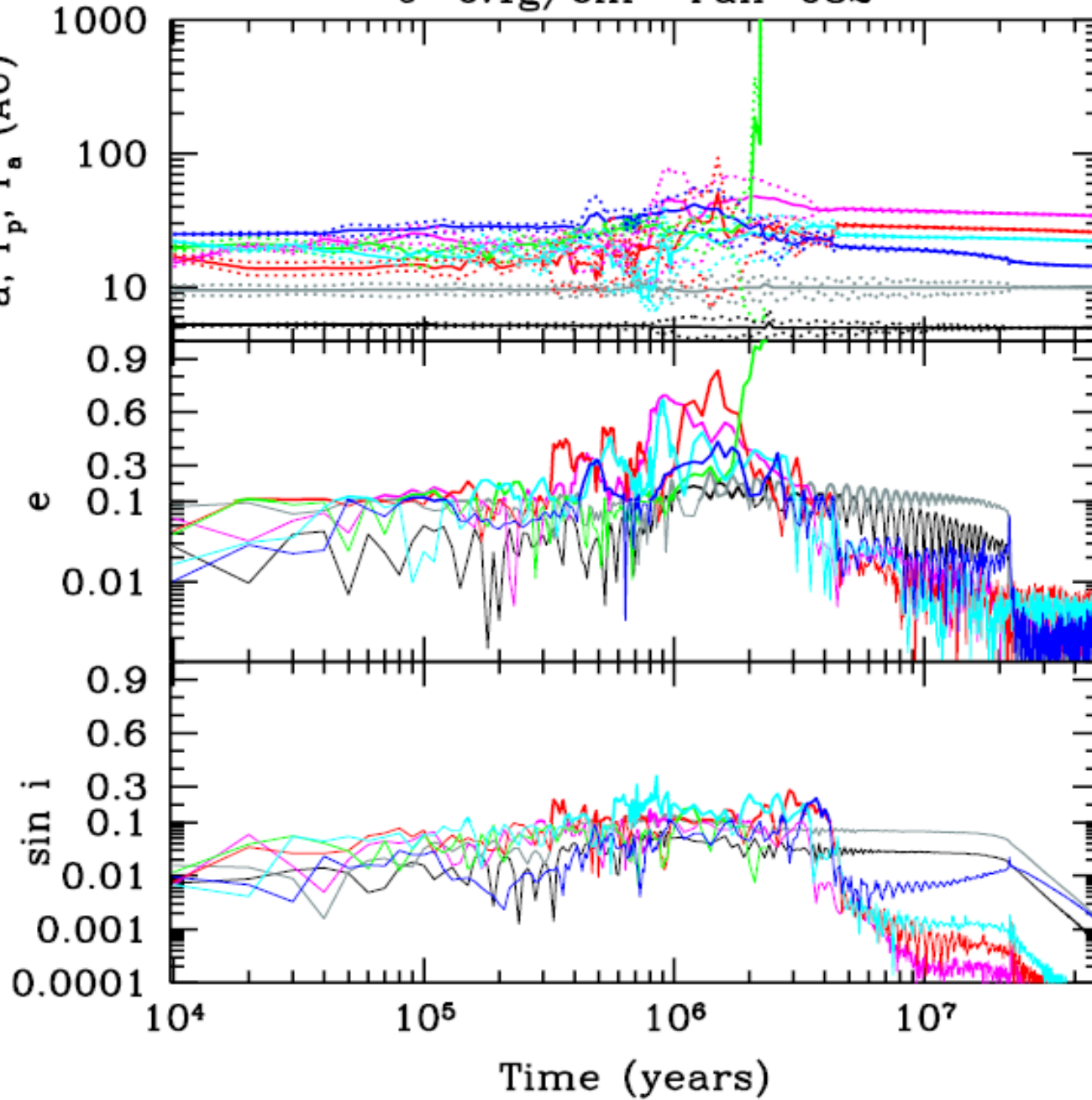
vs  $\Sigma \sim 0.7 \text{ g/cm}^2$

- Dynamical friction prevents close encounters
- Systems retain 5 oligarchs

# Full Simulations: $\sigma \sim 0.1 \text{ g/cm}^2$

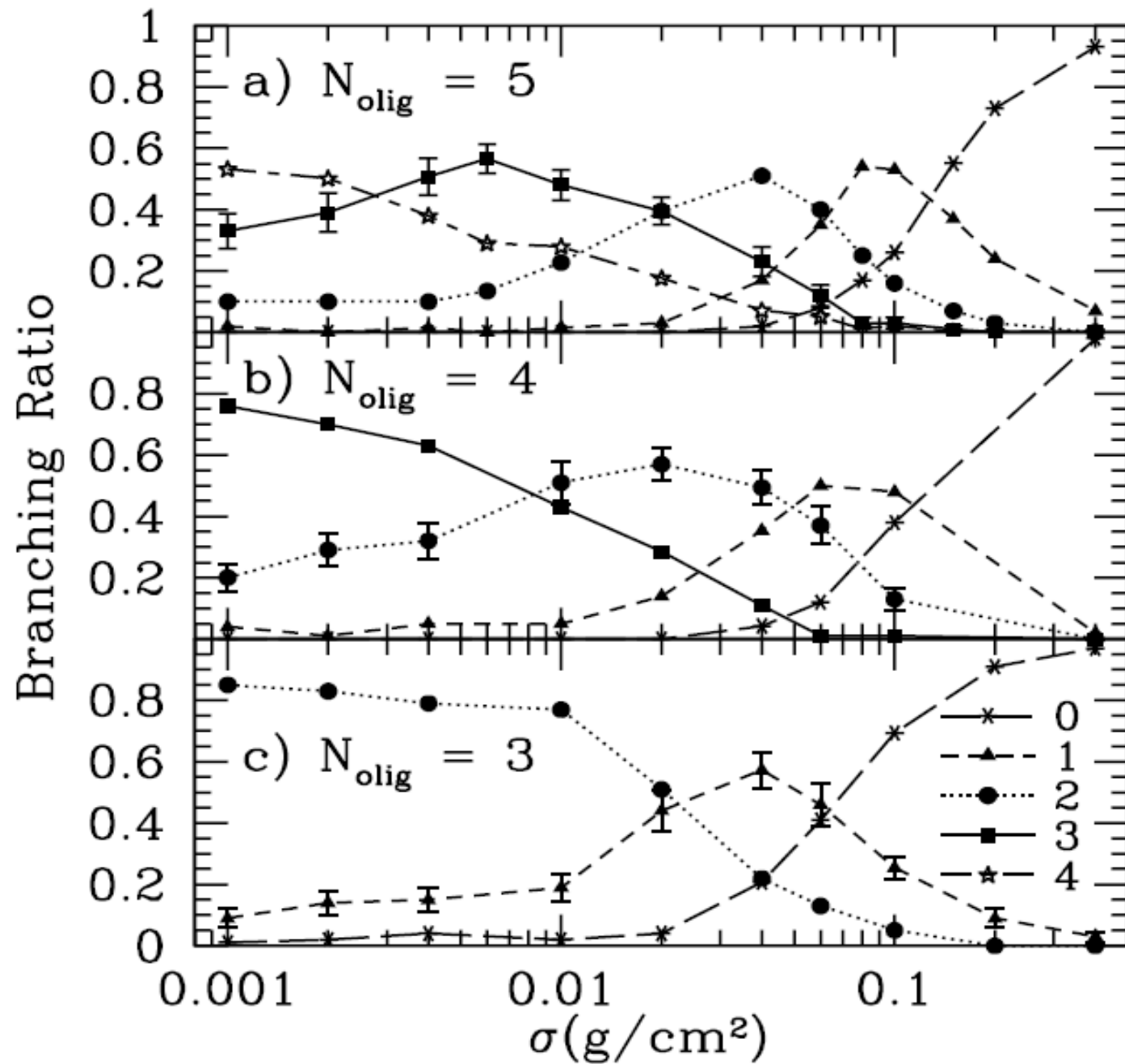
$\sigma = 0.1 \text{ g/cm}^2$  run=082

vs  $\Sigma \sim 0.7 \text{ g/cm}^2$



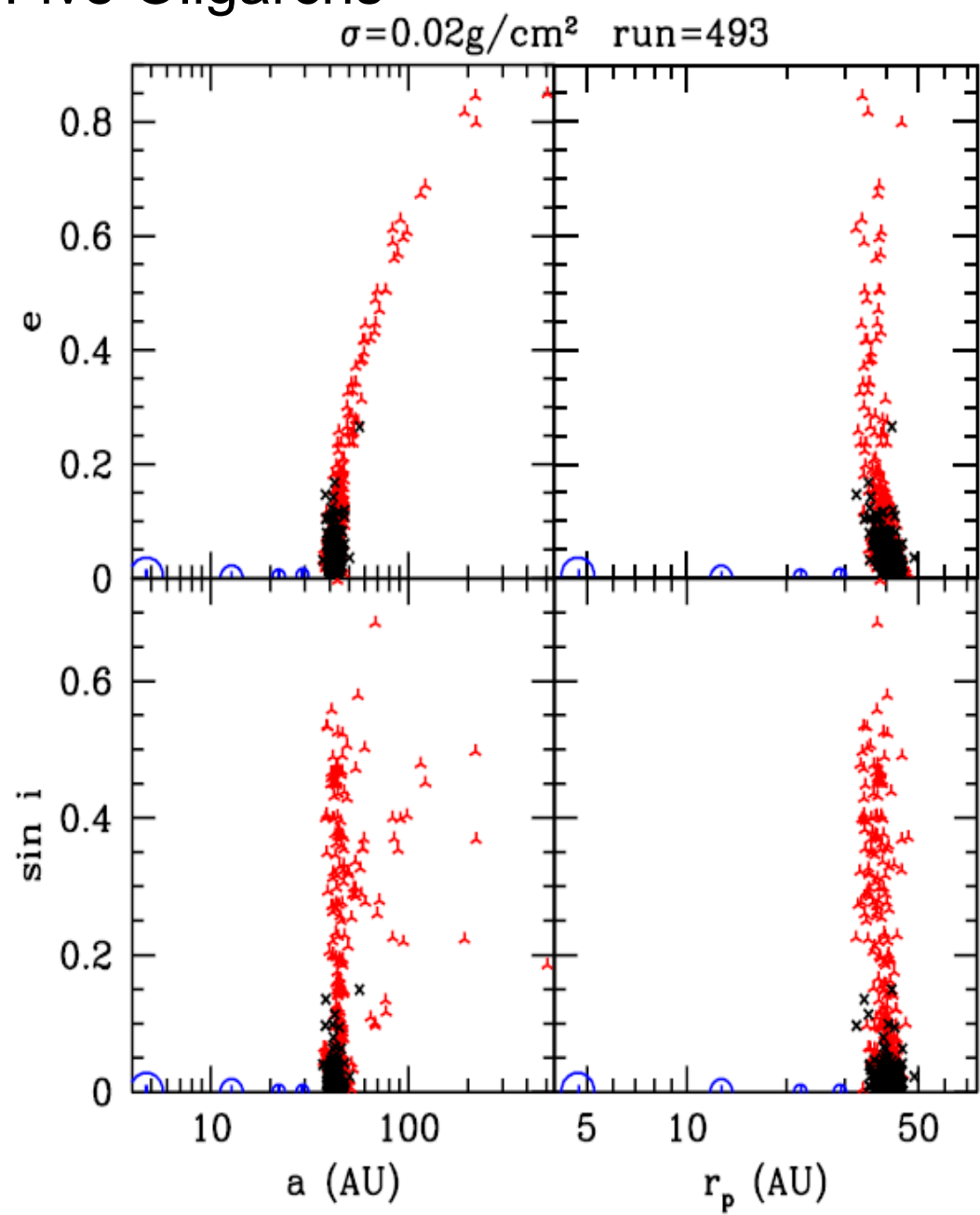
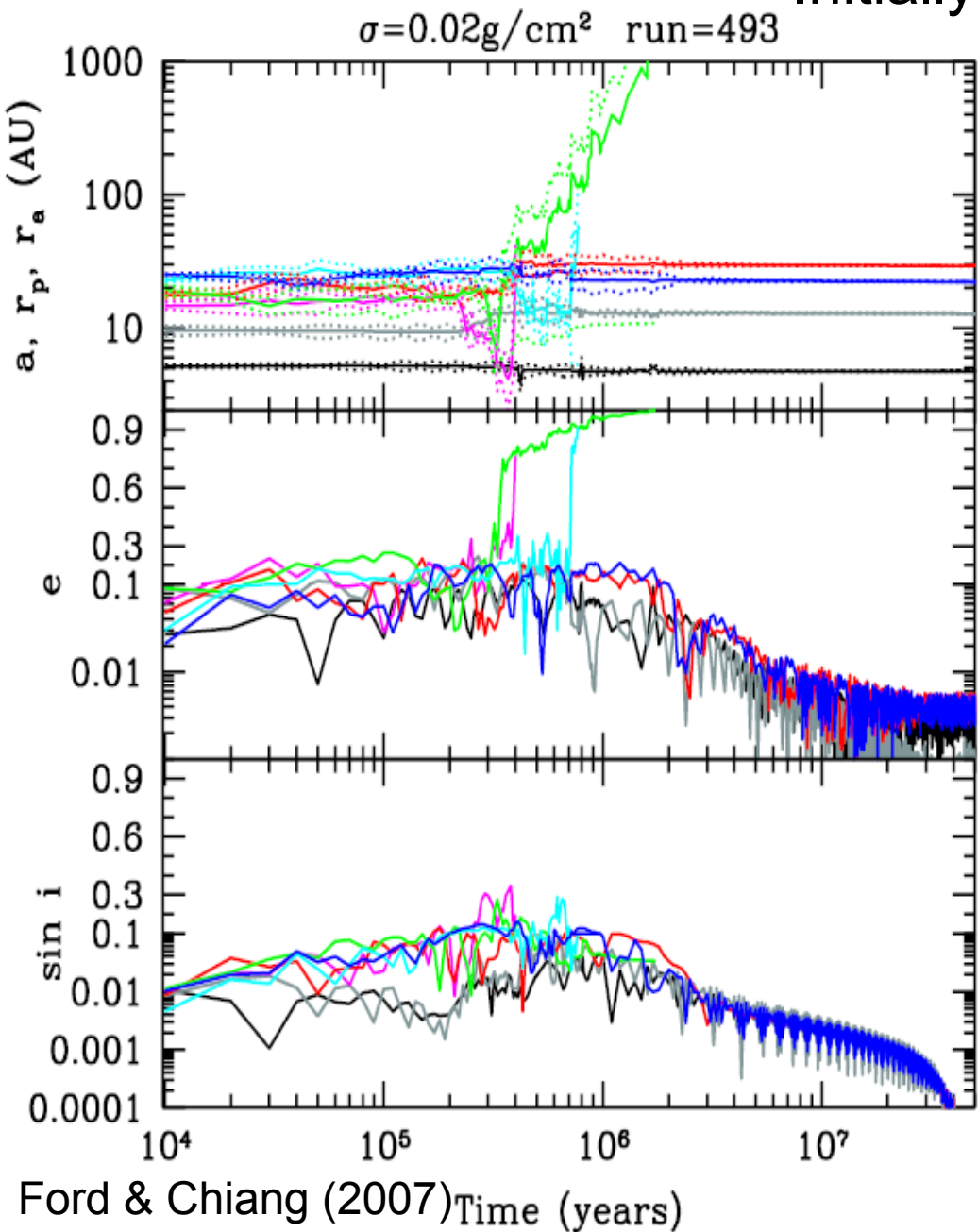
- Near threshold of instability
- One oligarch ejected
- Remaining planets recircularize
- Results in outward migration

# Outcome of Instability

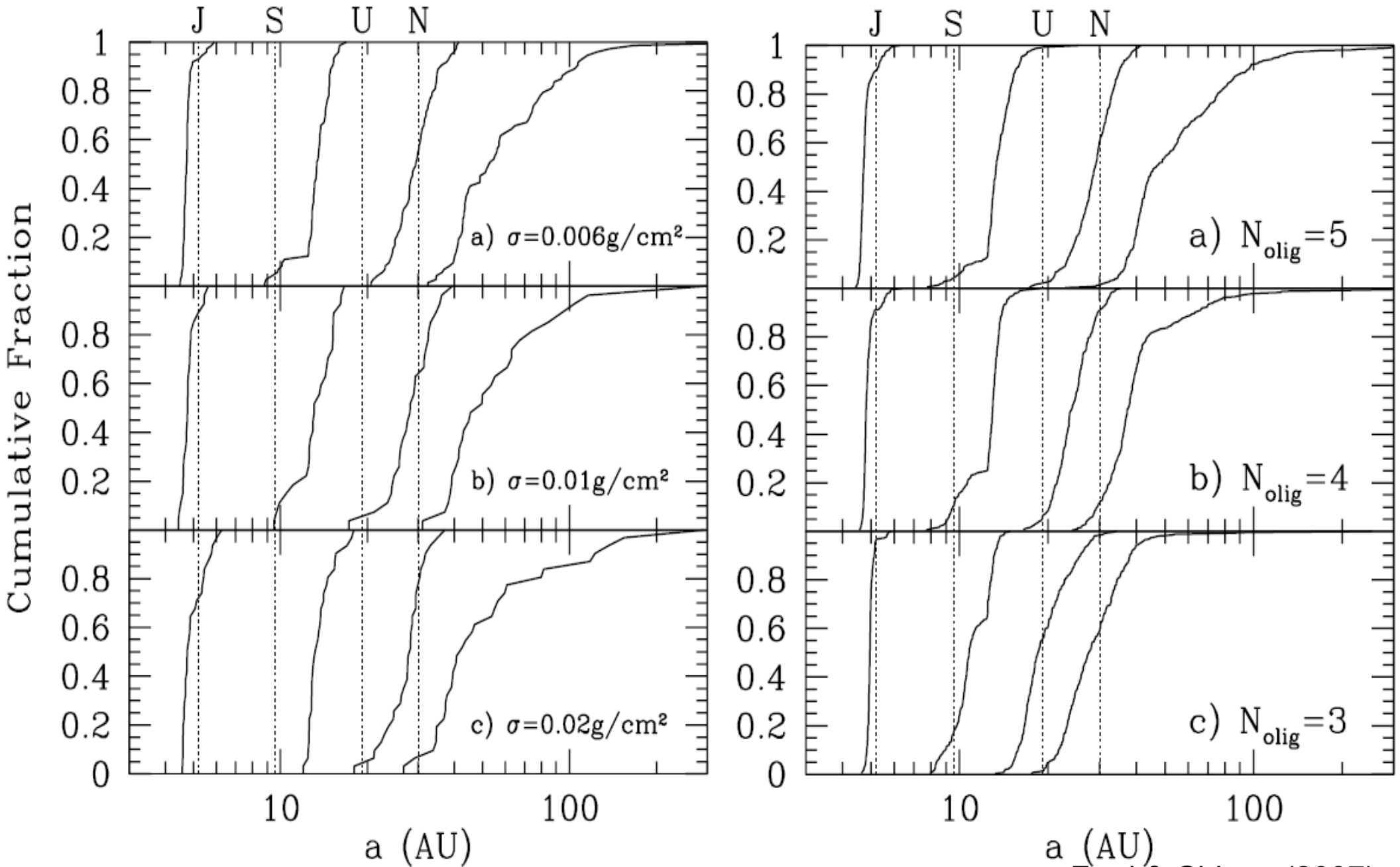


# Full Simulations: $\sigma \sim 0.02 \text{ g/cm}^2$ vs $\Sigma \sim 0.7 \text{ g/cm}^2$

Initially Five Oligarchs

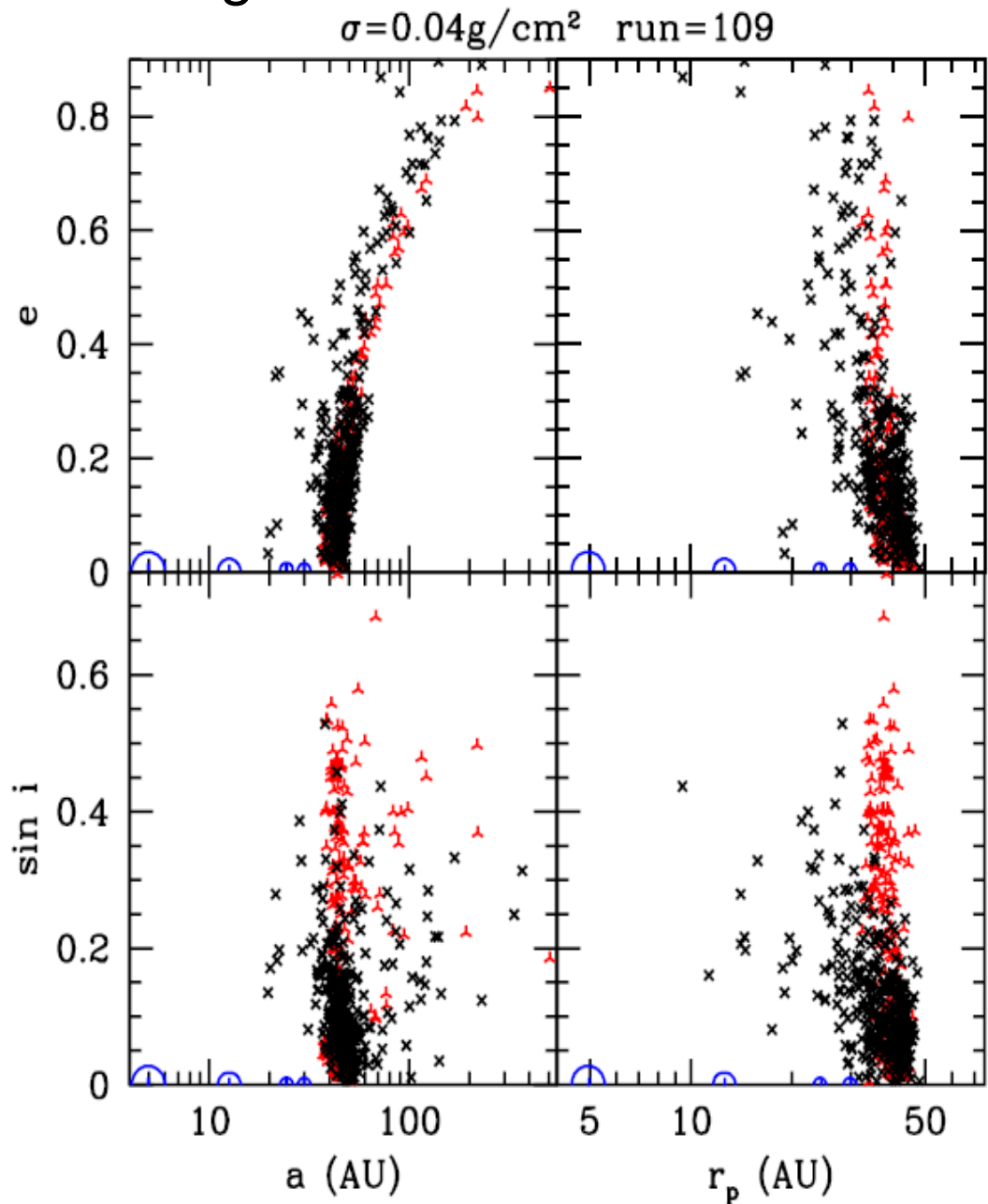
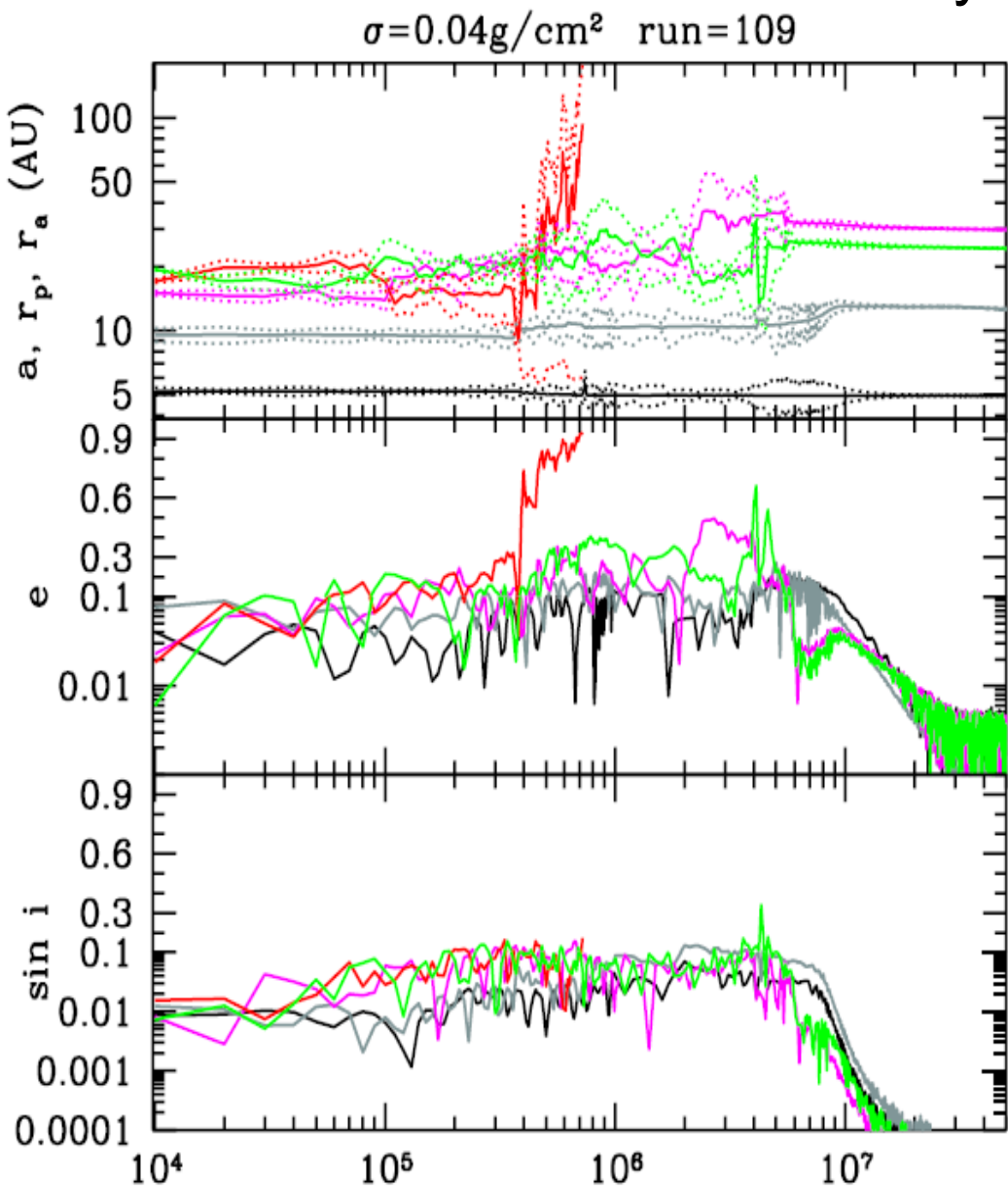


# Outward Spreading of Oligarchs



# Full Simulations: $\sigma \sim 0.04 \text{ g/cm}^2$ vs $\Sigma \sim 0.7 \text{ g/cm}^2$

Initially Three Oligarchs



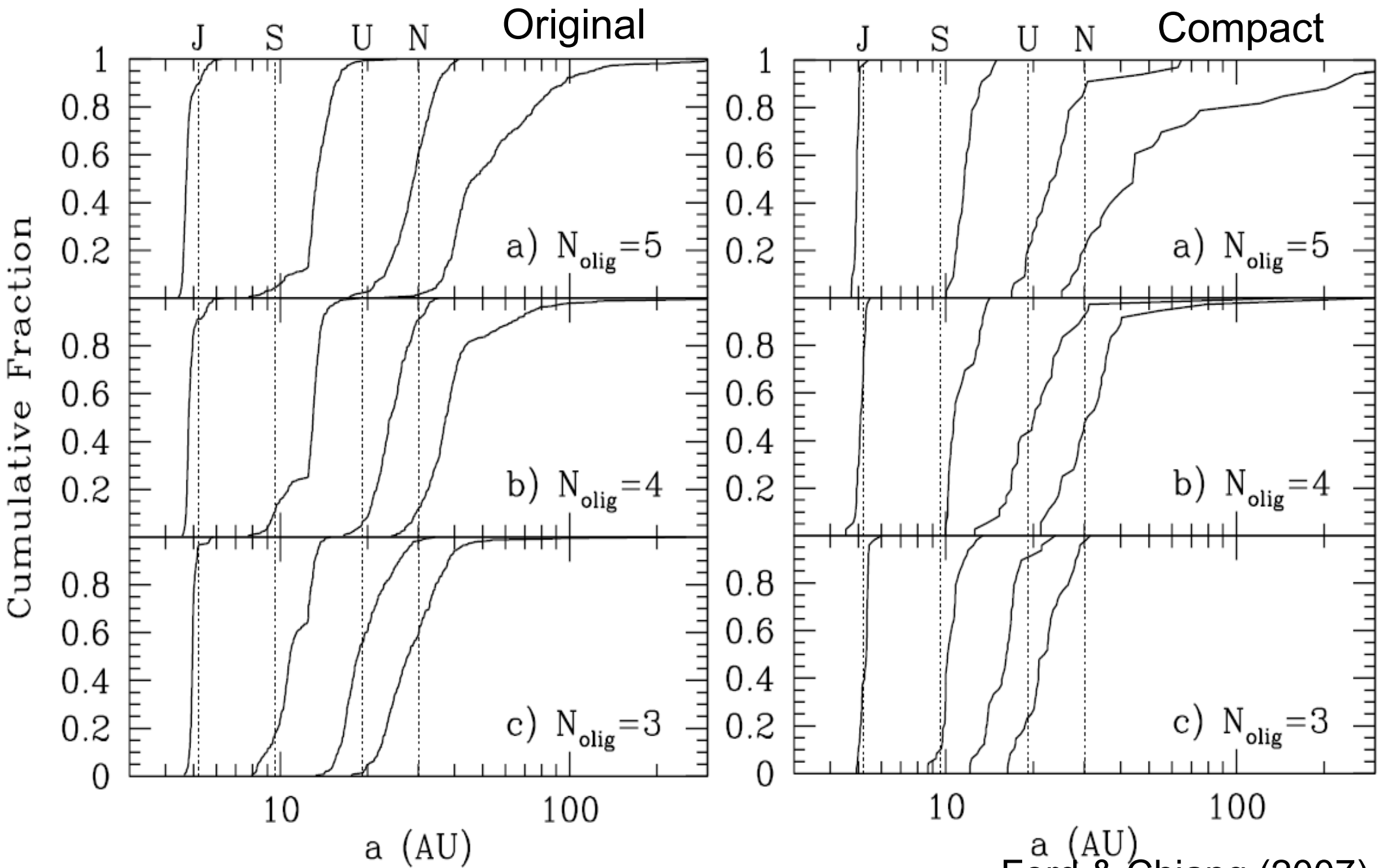


# Our Model: Initial Conditions

- Consider more compact initial conditions
- Jupiter & Saturn:  $a_{\text{init}} = 5.7, 8 \text{ AU}$
- 5 Neptune-mass Oligarchs:
  - $a_{\text{init}} = 13.17, 15.5, 17.7, 20.1 \text{ AU}$
  - $e_{\text{init}} = \sin(i_{\text{init}}) = 0.05$
- Small bodies (static, constant  $\sigma$  disk):
  - $10 \text{ AU} < a < 45 \text{ AU}$
  - Interact with oligarchs only via dynamical friction
- Large ( $\sim 100 \text{ km}$ ) Kuiper Belt Objects
  - 400 test particles
  - $a_{\text{init}} = 40\text{-}45 \text{ AU}$
  - $e_{\text{init}} = \sin(i_{\text{init}}) = 0.01$



# Outward Spreading of Oligarchs

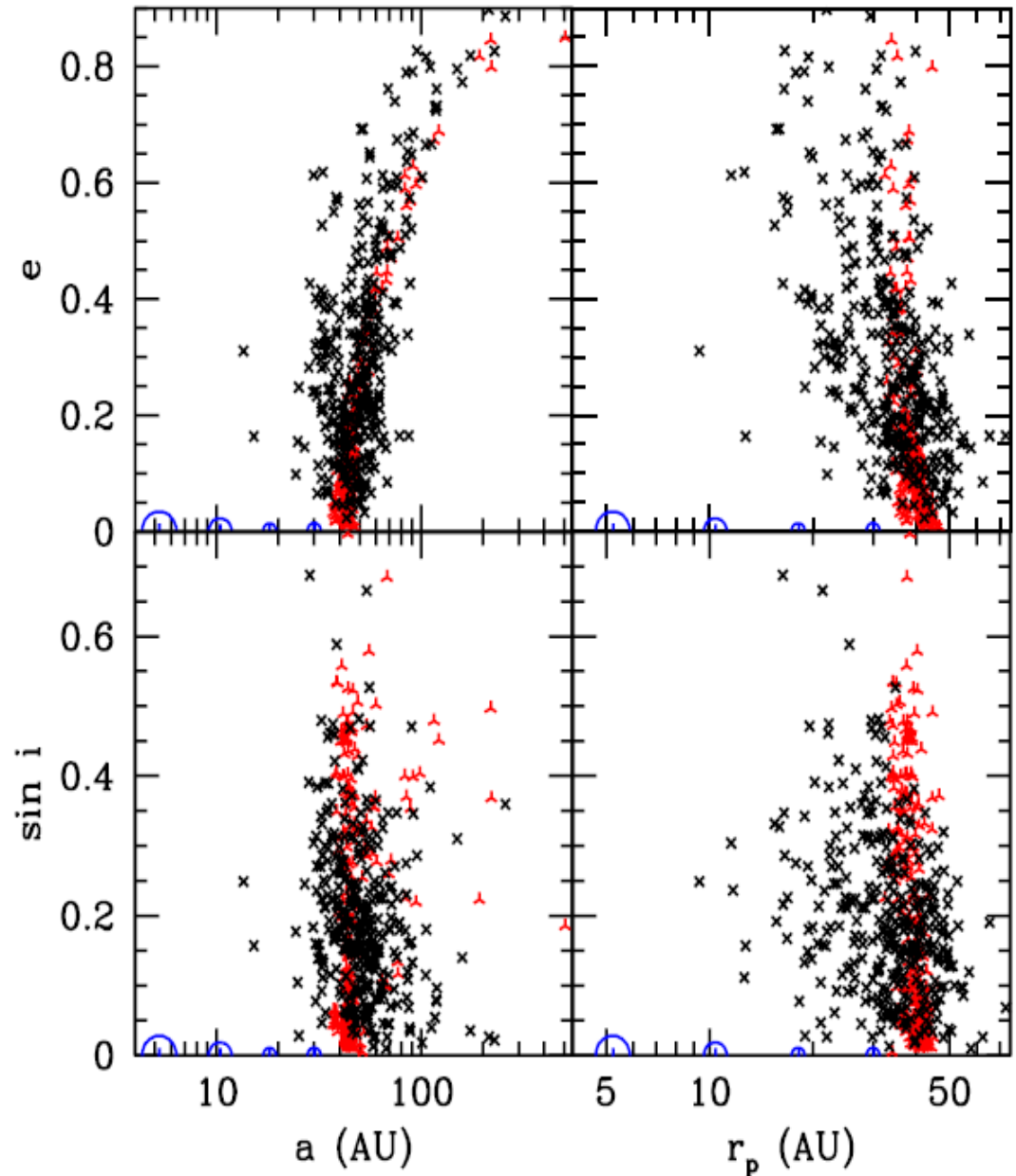
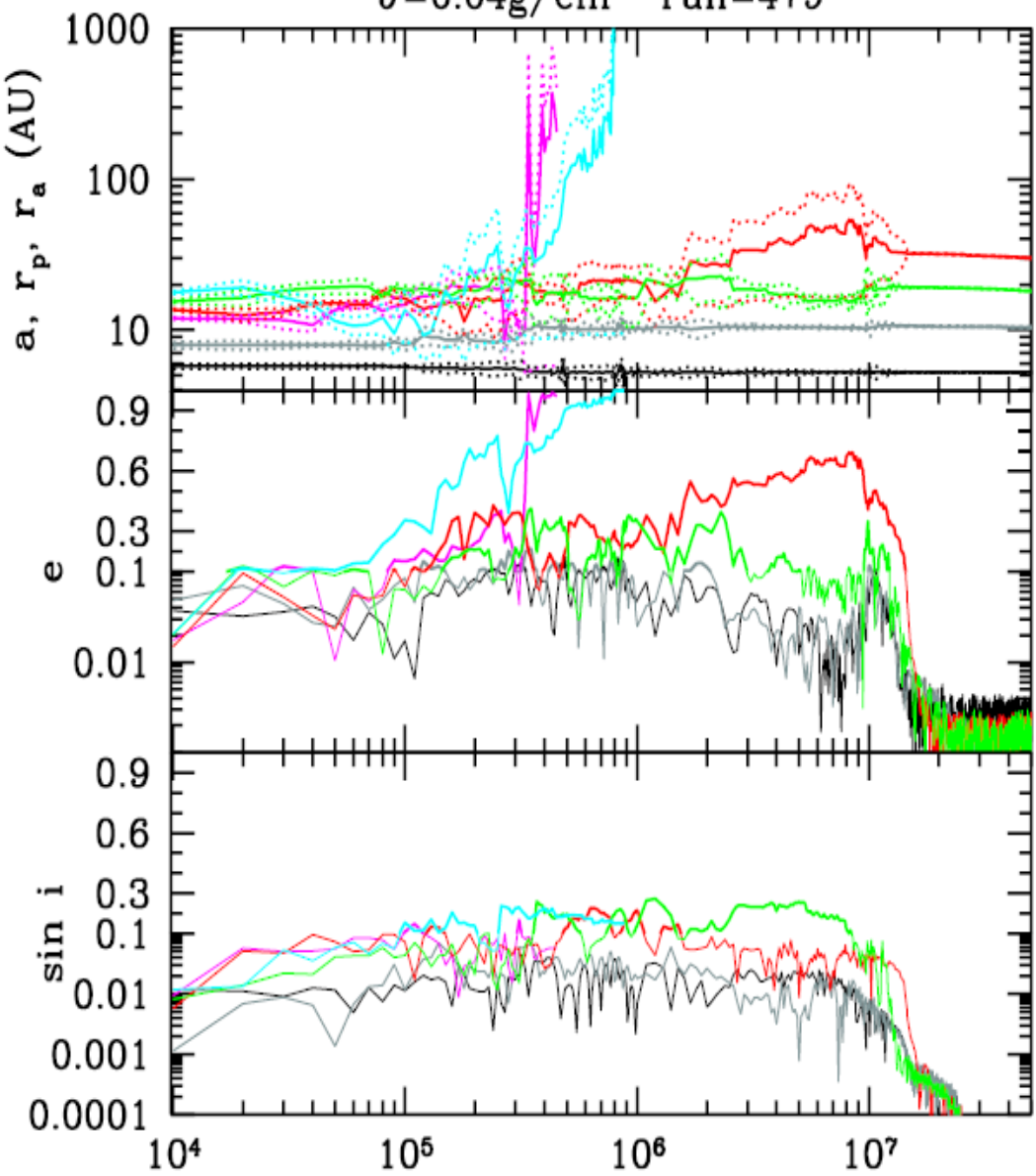


# Full Simulations: $\sigma \sim 0.04 \text{ g/cm}^2$ vs $\Sigma \sim 1.8 \text{ g/cm}^2$

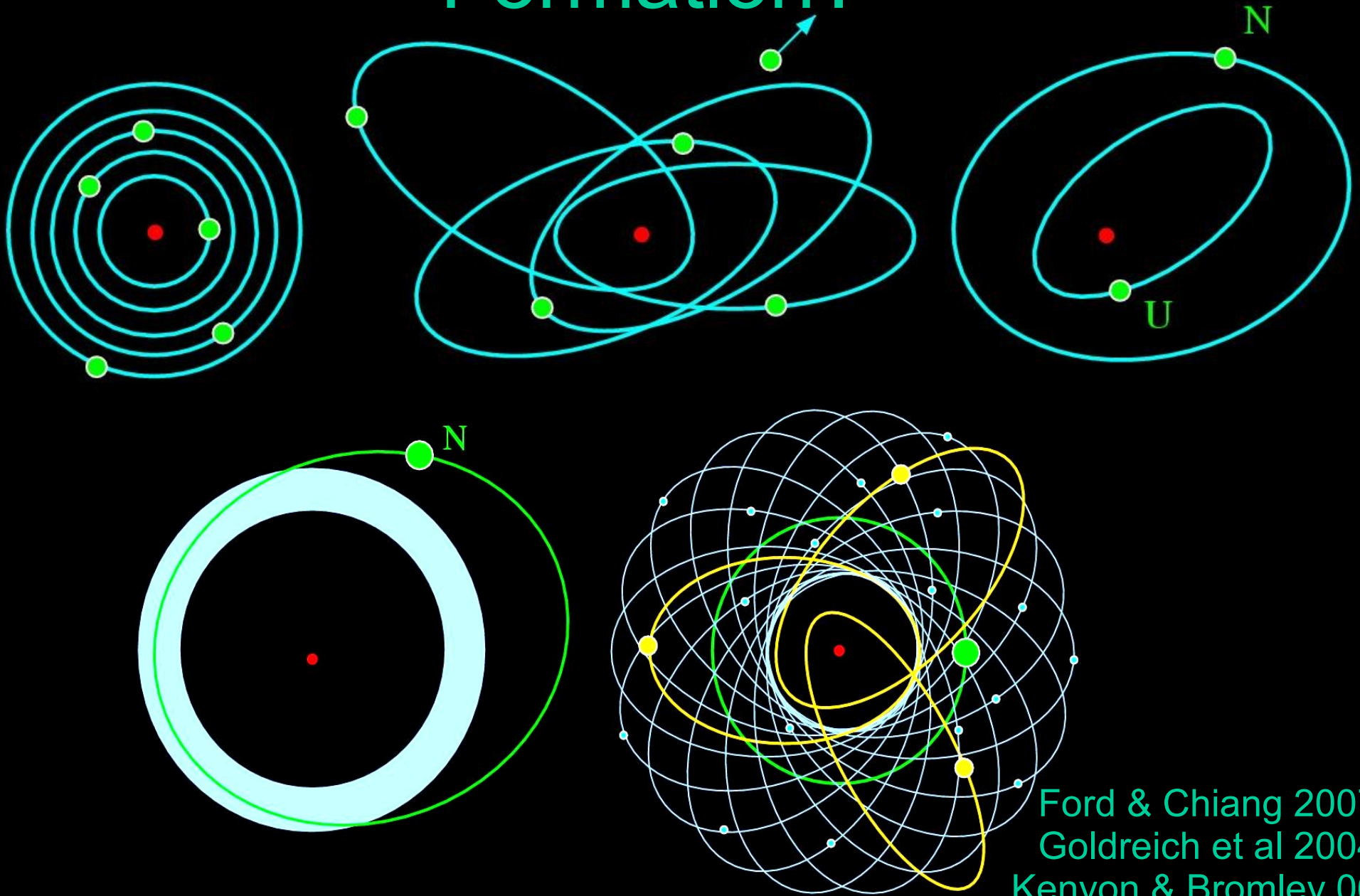
Initially Four Oligarchs, Compact Spacing

$\sigma = 0.04 \text{ g/cm}^2$  run=479

$\sigma = 0.04 \text{ g/cm}^2$  run=479



# Very Late Stages of Planet Formation?



Ford & Chiang 2007  
Goldreich et al 2004  
Kenyon & Bromley 06  
Thommes et al. 99, 02

# Conclusions

- Early stages of planet formation are highly uncertain due to complicated physics
- Oligarchic growth may regulate growth, enforcing a similar intermediate state
- Late stages of planet formation have simple physics, but can produce a wide variety of outcomes due to chaotic evolution
- Final state of planetary systems is determined by long-term chaotic orbital evolution

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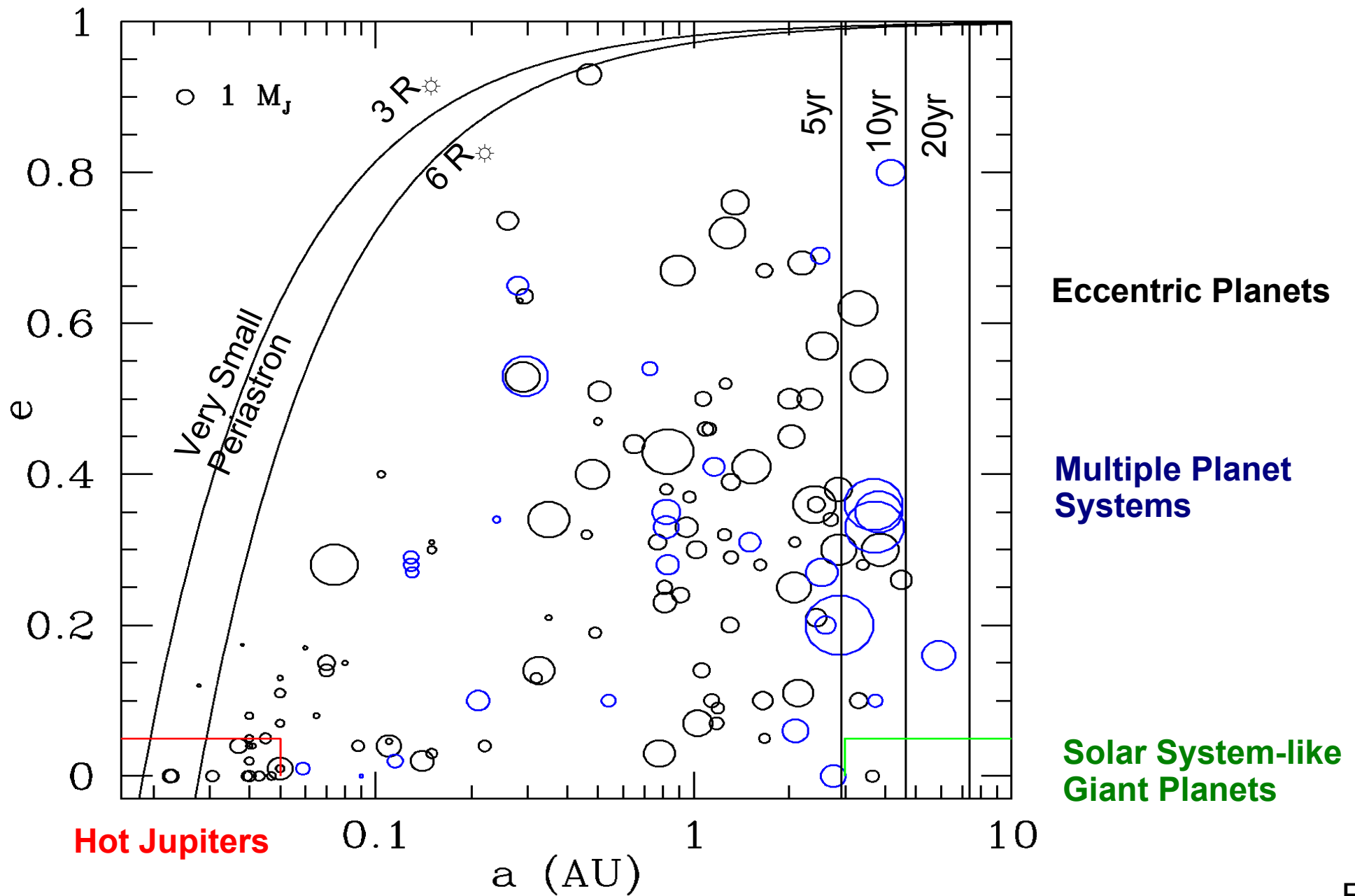
University of Florida (starting in August, 2007)

May 30, 2007

Extrasolar Planets: detection, formation, evolution, and dynamics of planetary systems  
Sabhal Mor Ostaig, Isle of Skye, United Kingdom

Collaborators: Sourav Chatterjee<sup>G</sup>, Eugene Chiang, Scott Gaudi, Matt Holman,  
Kris Joshi<sup>G</sup>, Mario Juric, Boris Kozinsky<sup>U</sup>, Verene Lystad<sup>U</sup>, Fred Rasio,  
Boris Zbarsky<sup>U</sup>

# Diversity of Extrasolar Planets



# How to Excite Eccentricities?

- **Gas Disk** (Artymowicz 1992, Chiang & Murray 2002, Goldreich & Sari 2003, Papalouizou et al. 2001, Ogilvie & Lubow 2003)
- **Planetesimal Disk** (Murray et al. 1998)
- **Planet-Planet Scattering**
- **Resonant Interactions** (Chiang & Murray 2002, Kley et al. 2004, 2005, Lee & Peale 2002, Nagasawa et al. 2003, Tsiganis et al. 2005, Adams & Laughlin 2006)
- **Secular Perturbations from Hierarchical Triple Systems** (Holman et al. 1997, Ford et al. 2000, Takeda & Rasio 2005)
- **Passing Stars** (Laughlin & Adams 1998, Ford et al. 2000, Hurley & Shara 2002, Zakamska & Tremaine 2004)
- **Asymmetric Stellar Jets** (Namouni 2005, 2006)
- **Hybrid Scenarios** (Marzari et al. 2005, Sandor & Kley 2006)

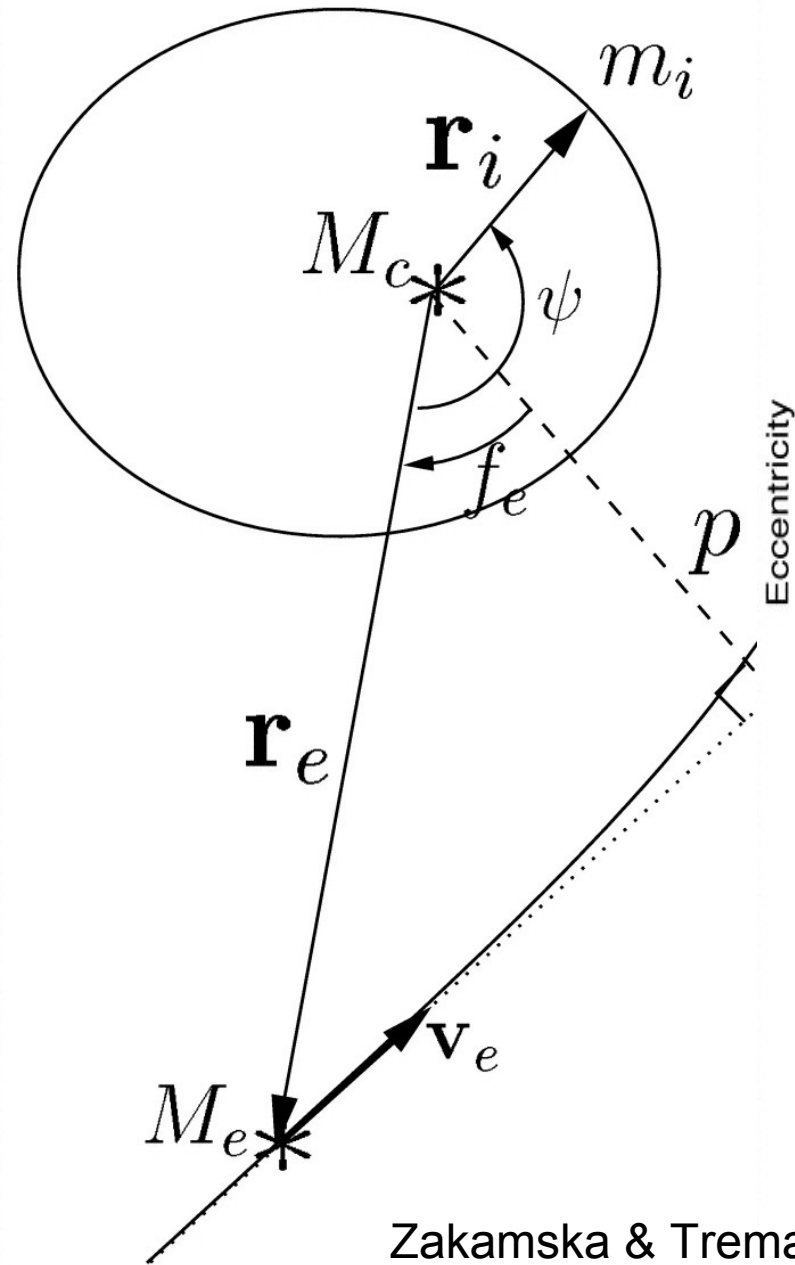


# How to Excite Eccentricities?

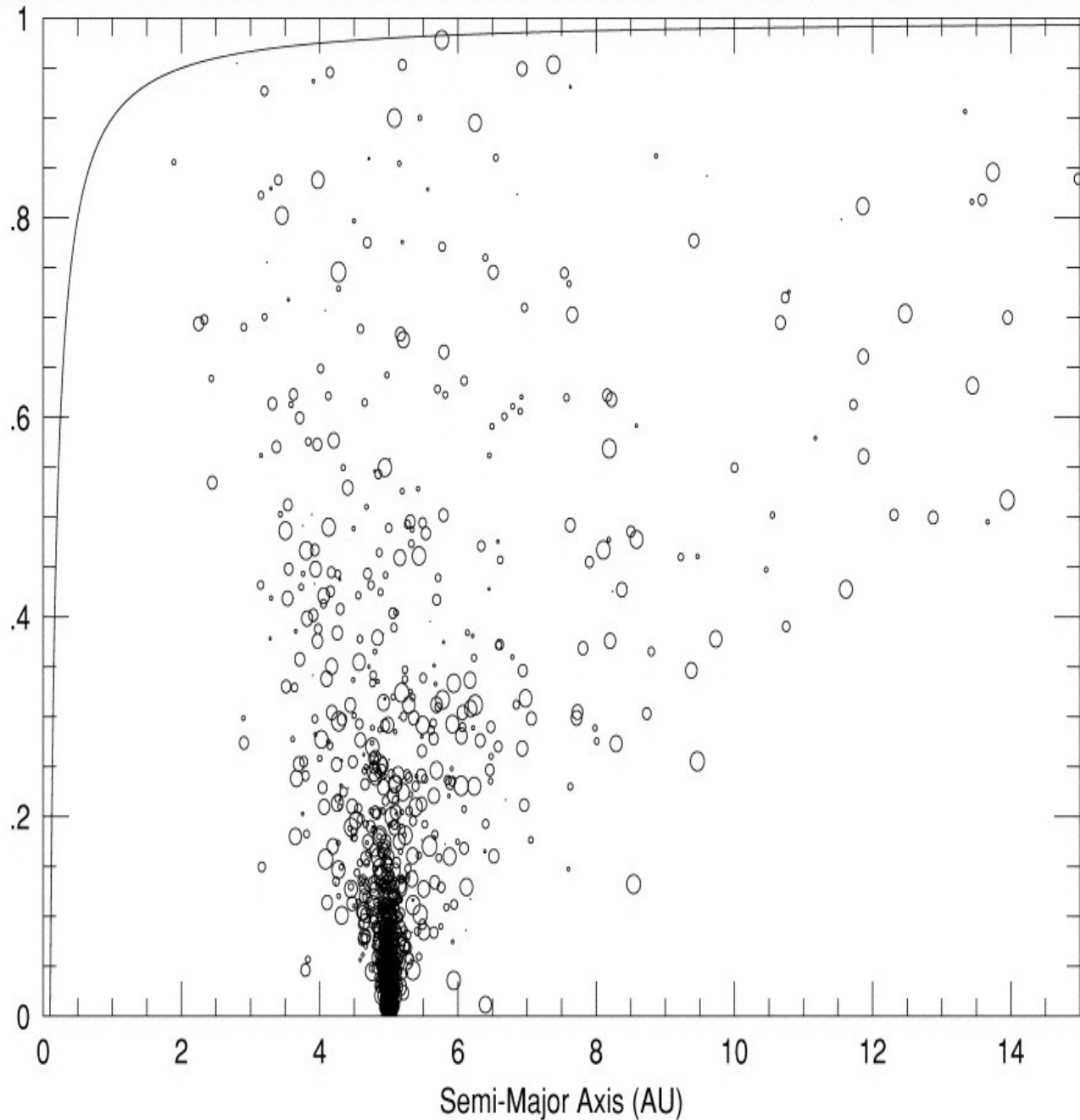
- **Gas Disk** (Artymowicz 1992, Chiang & Murray 2002, Goldreich & Sari 2003, Papalouizou et al. 2001, Ogilvie & Lubow 2003)
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- **Asymmetric Stellar Jets** (Namouni 2005, 2006)
- **Hybrid Scenarios** (Marzari et al. 2005, Sandor & Kley 2006)



# Eccentricity from Stellar Encounters

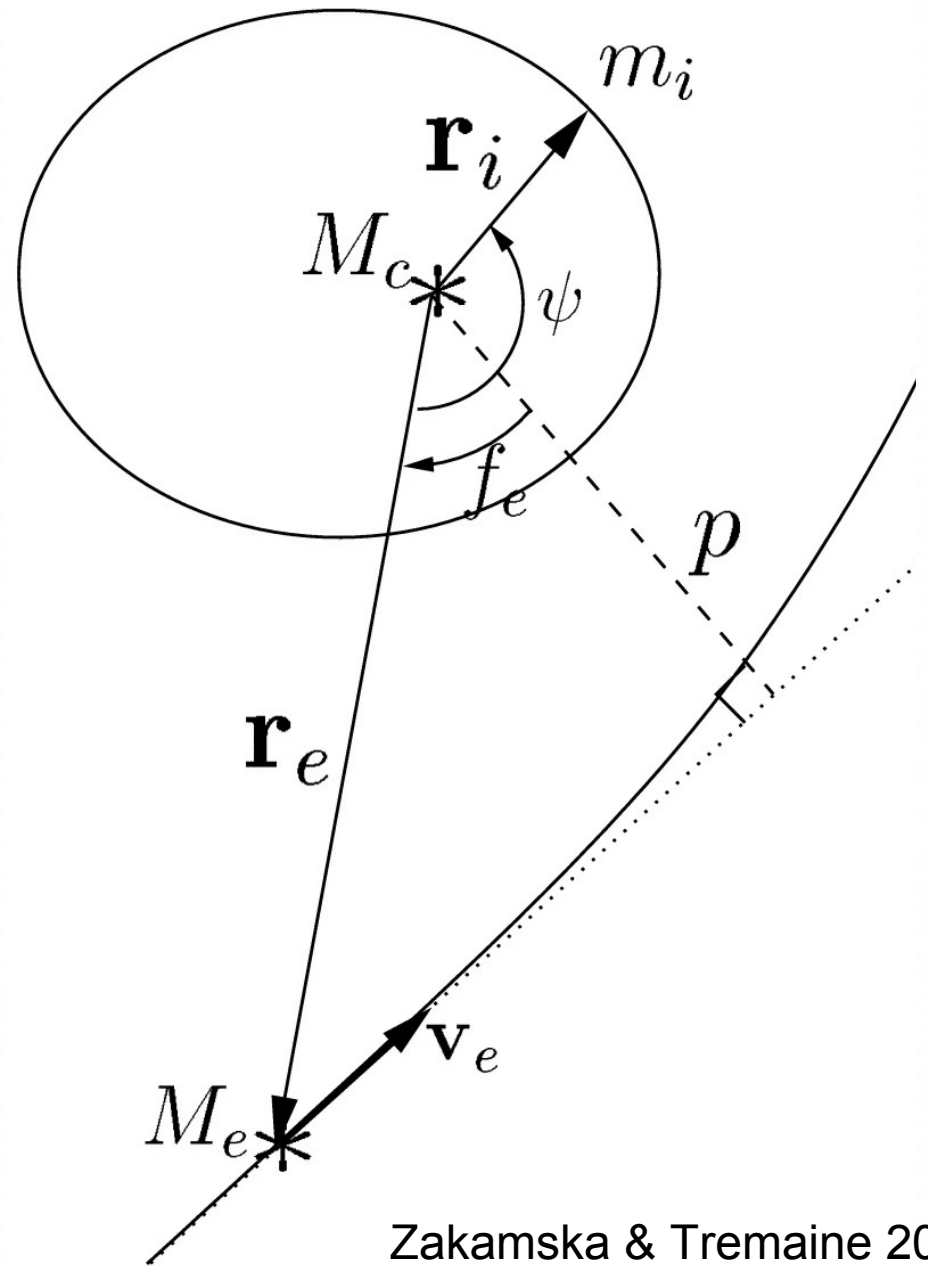


Zakamska & Tremaine 2004

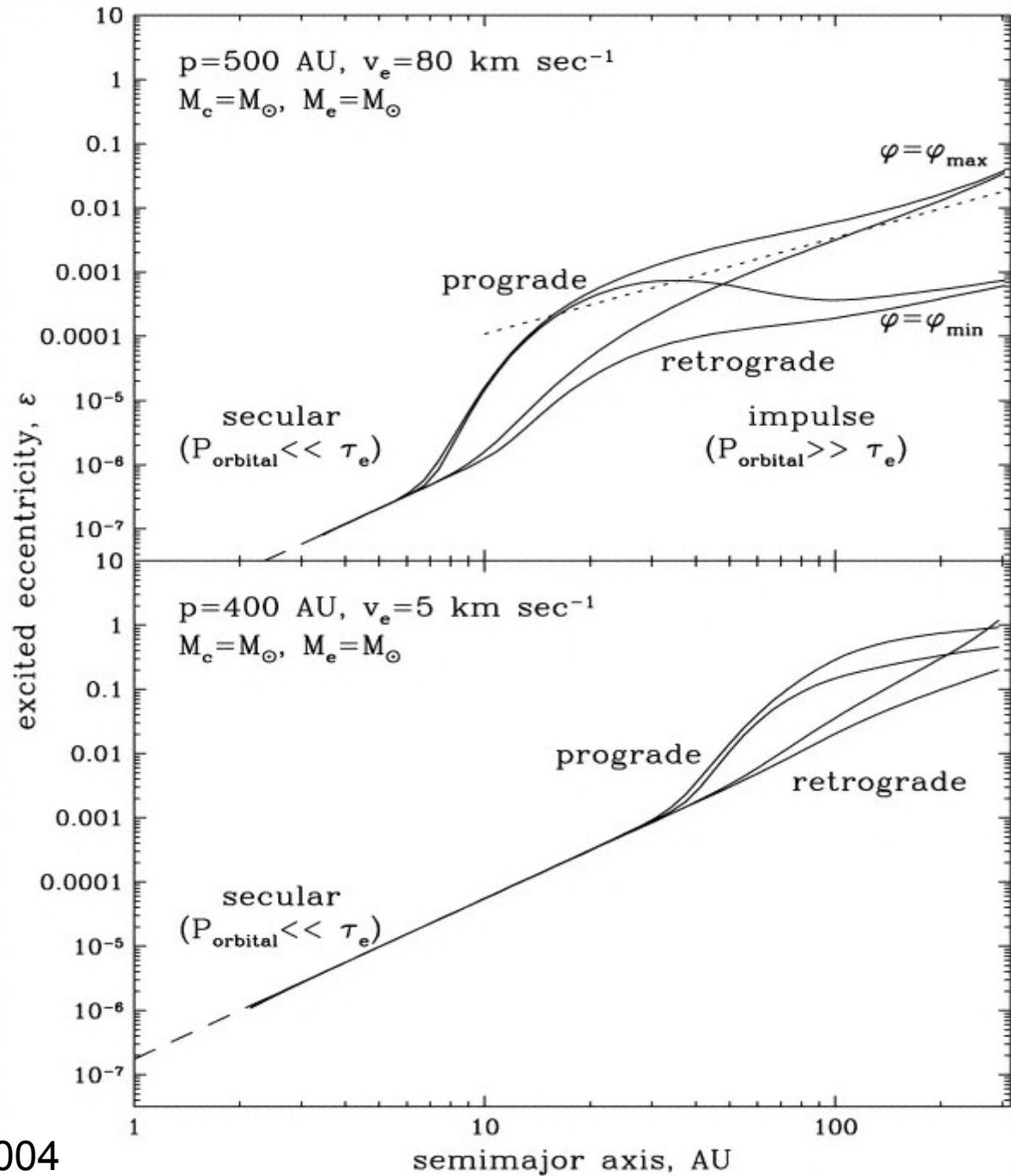


Laughlin & Adams 1998

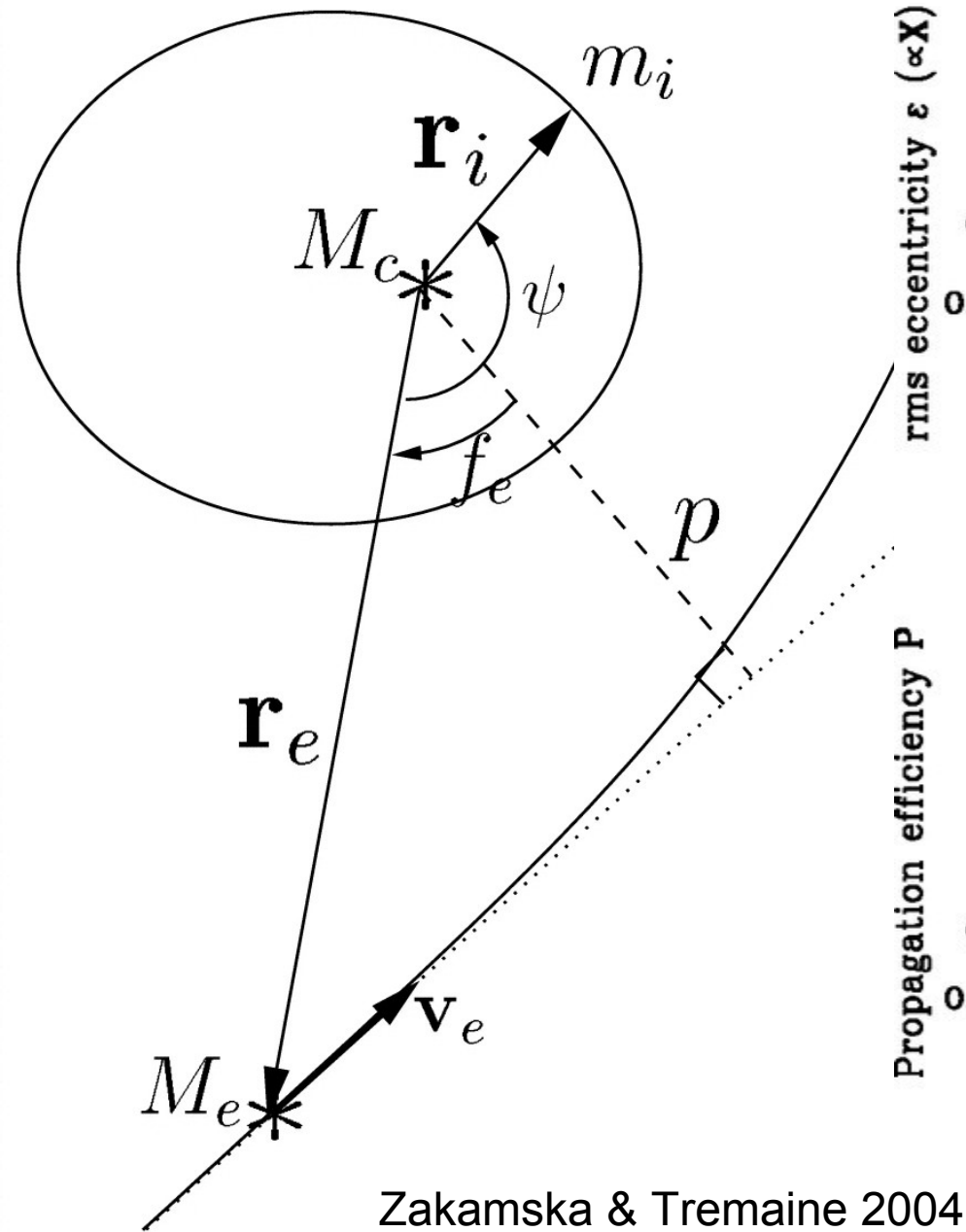
# Eccentricity from Stellar Encounters



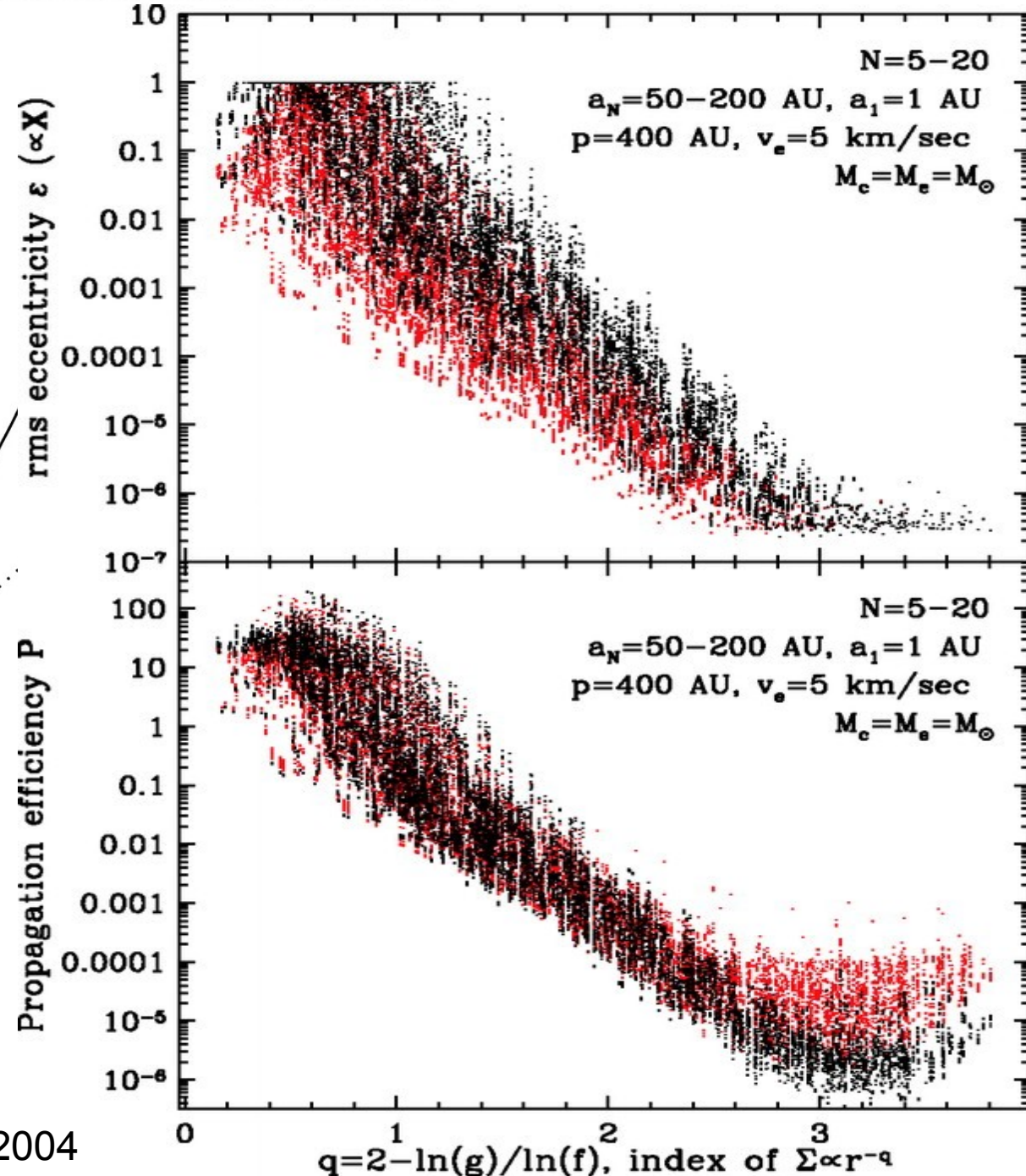
Zakamska & Tremaine 2004

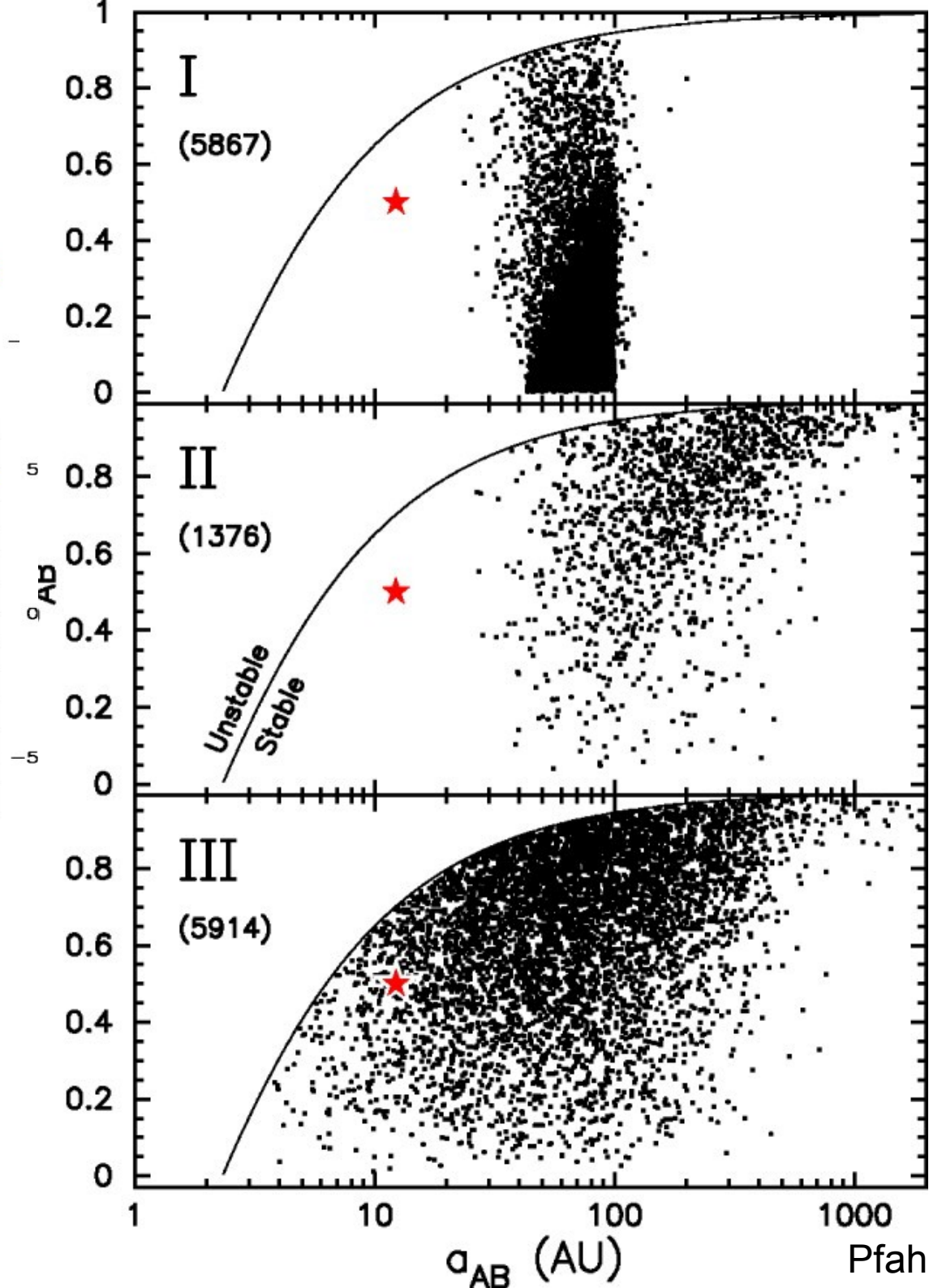
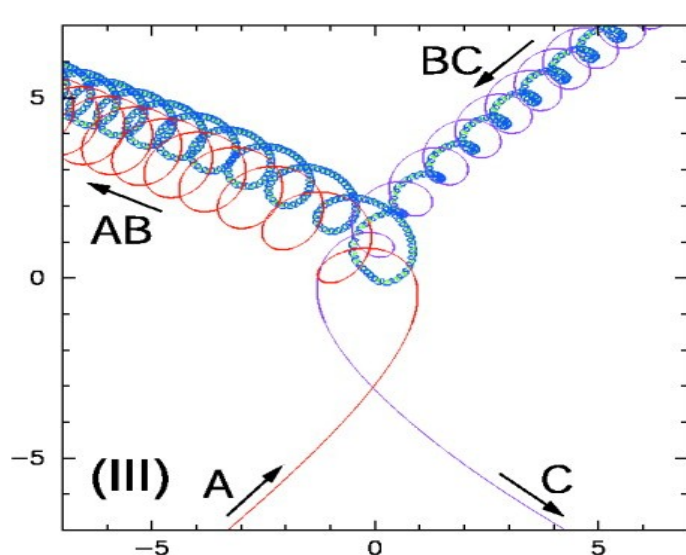
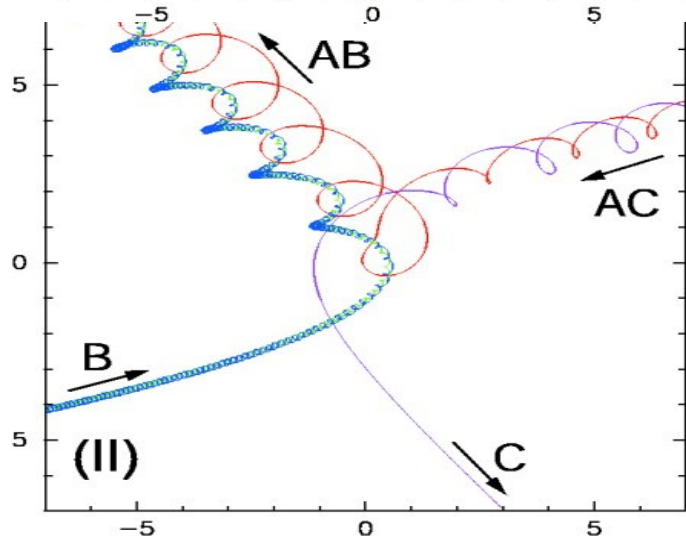
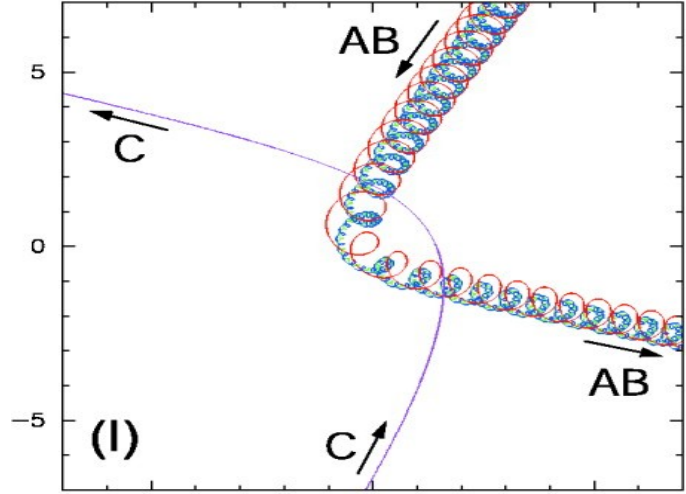


# Eccentricity from Stellar Encounters

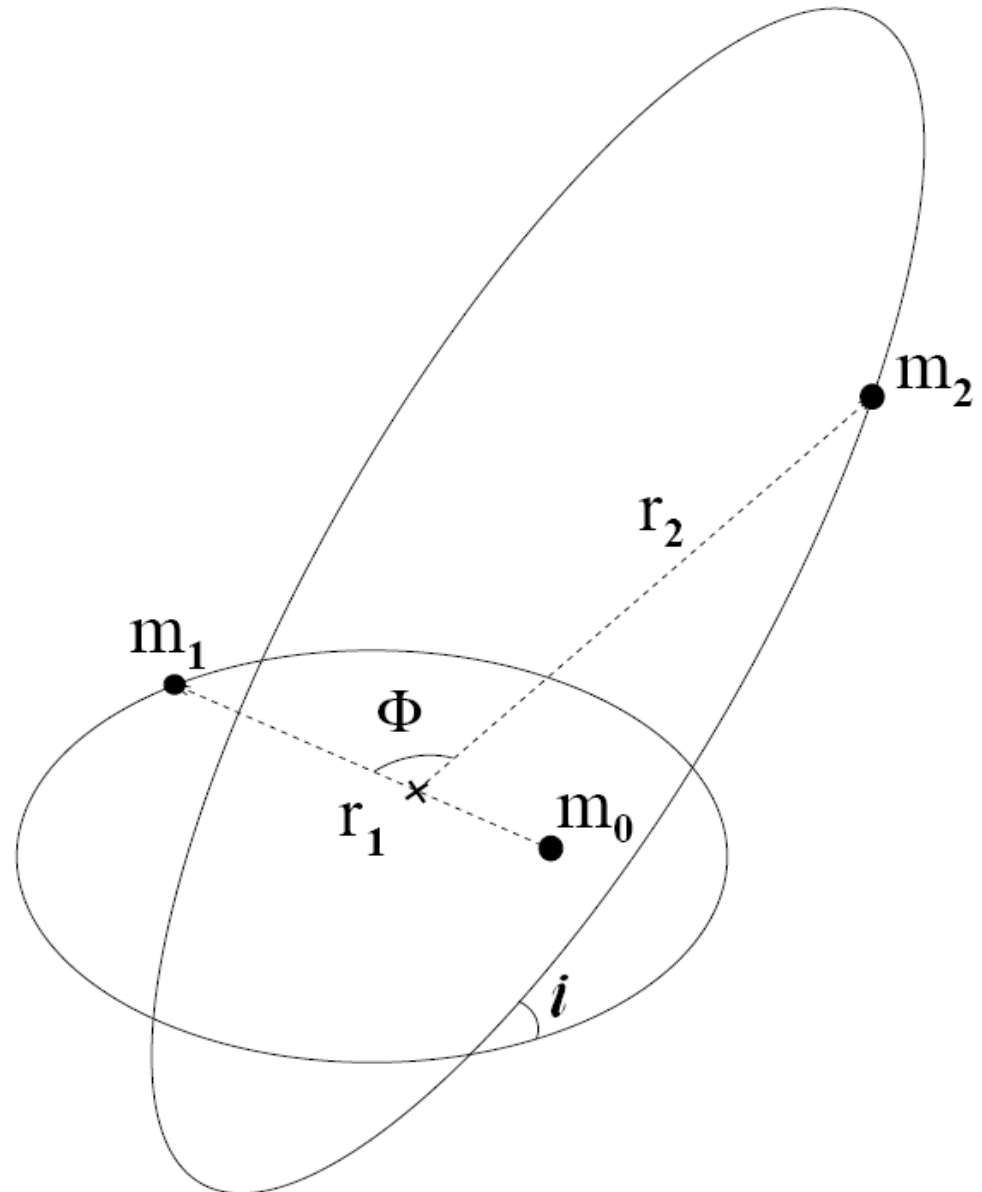
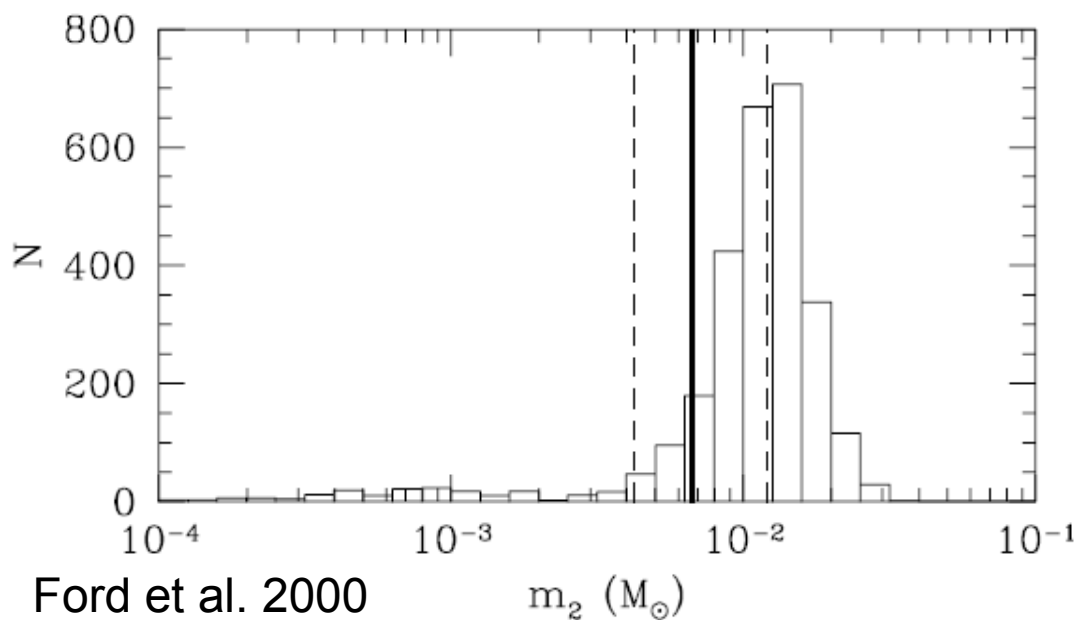
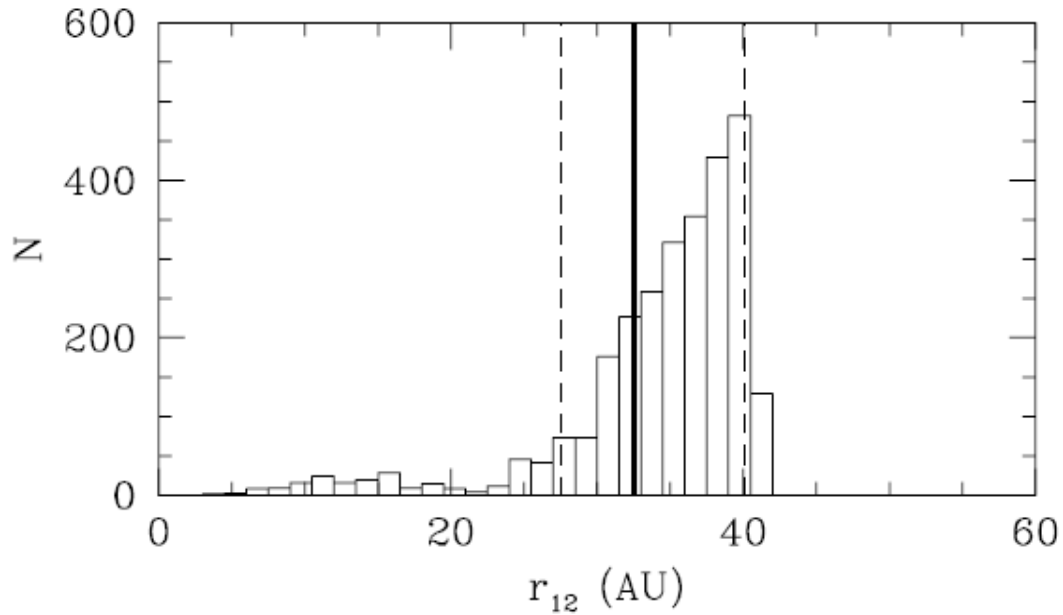


Zakamska & Tremaine 2004

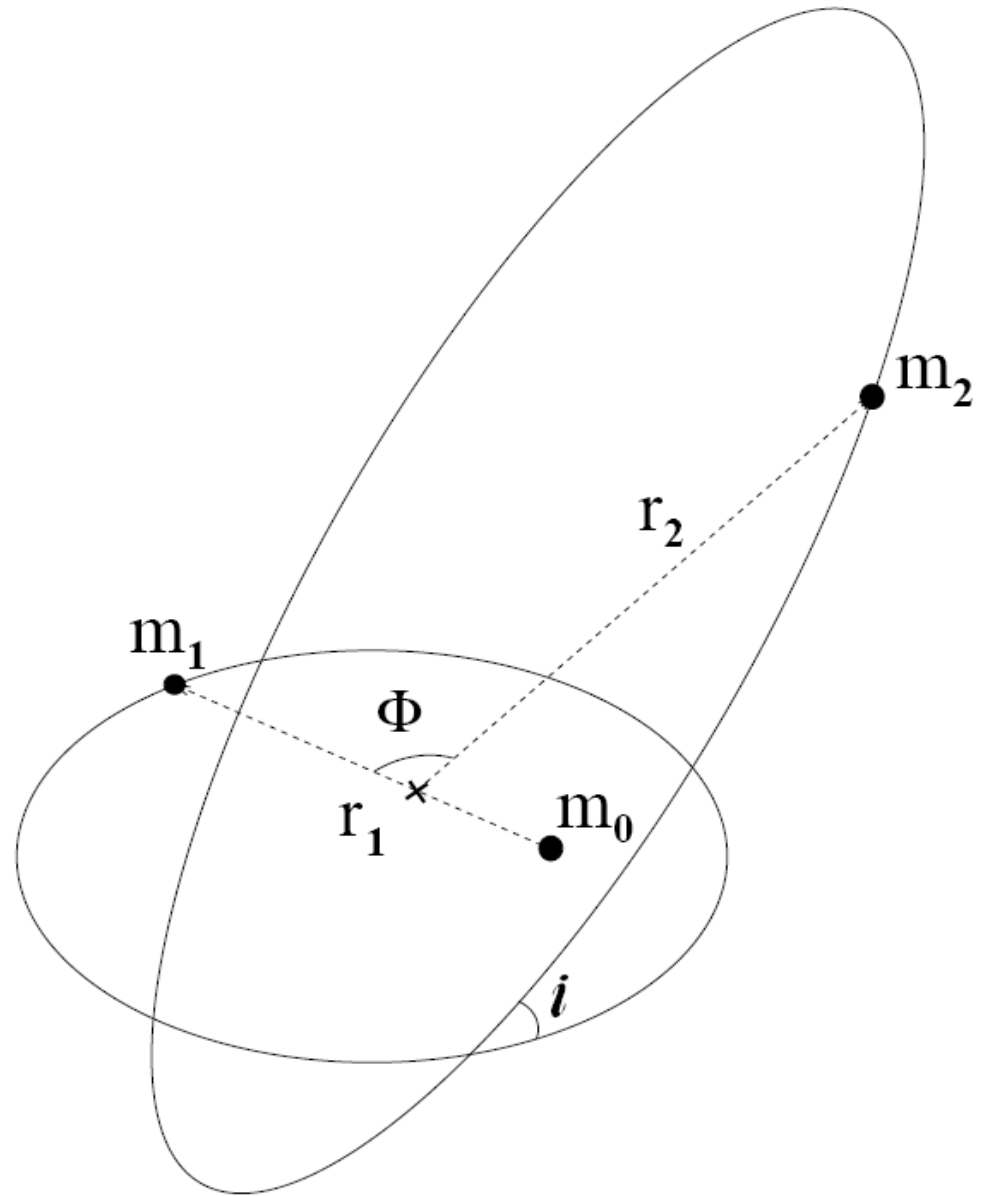
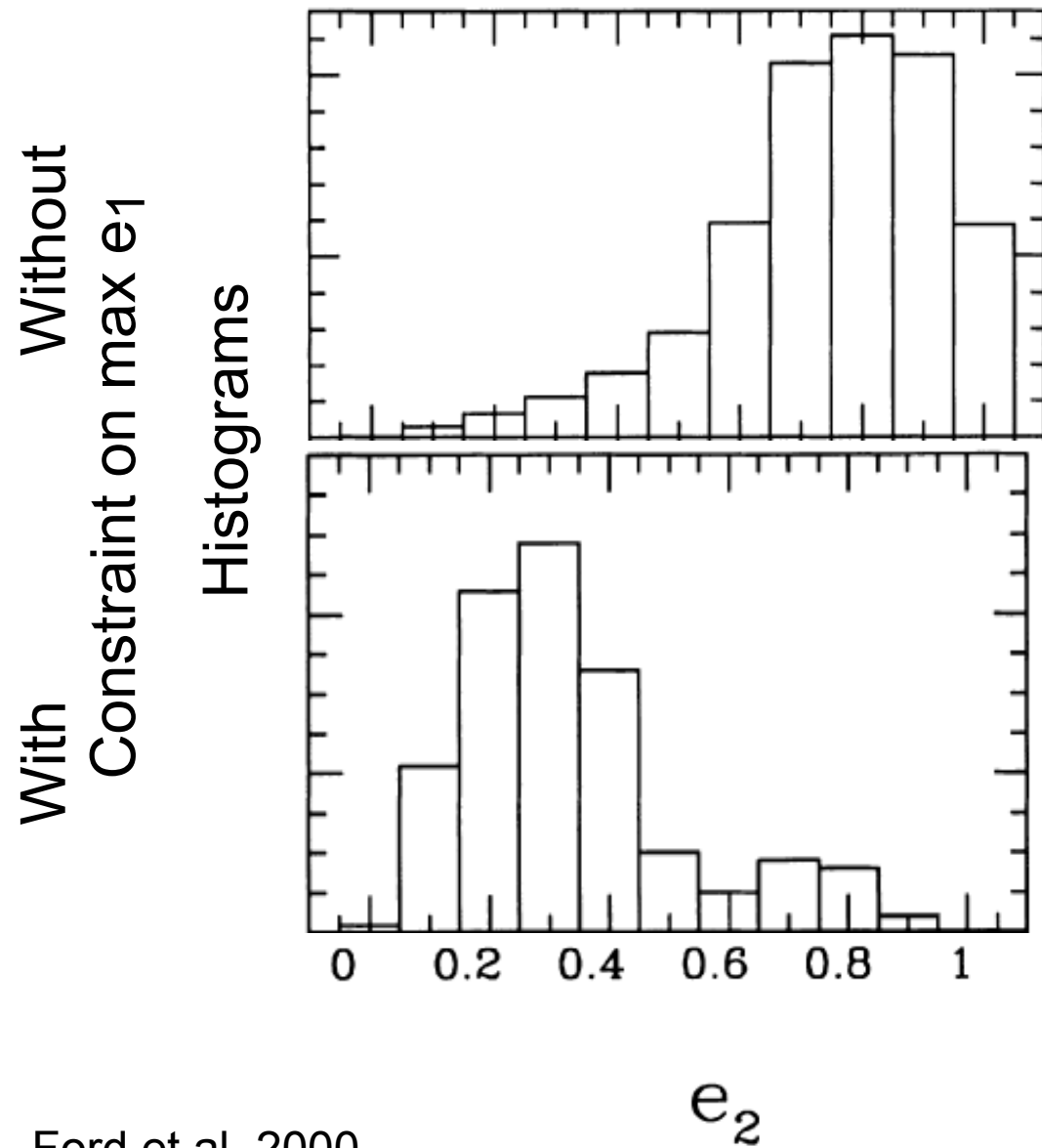




# A Captured Planet in PSR 1620+26?



# A Captured Planet in PSR 1620+26?

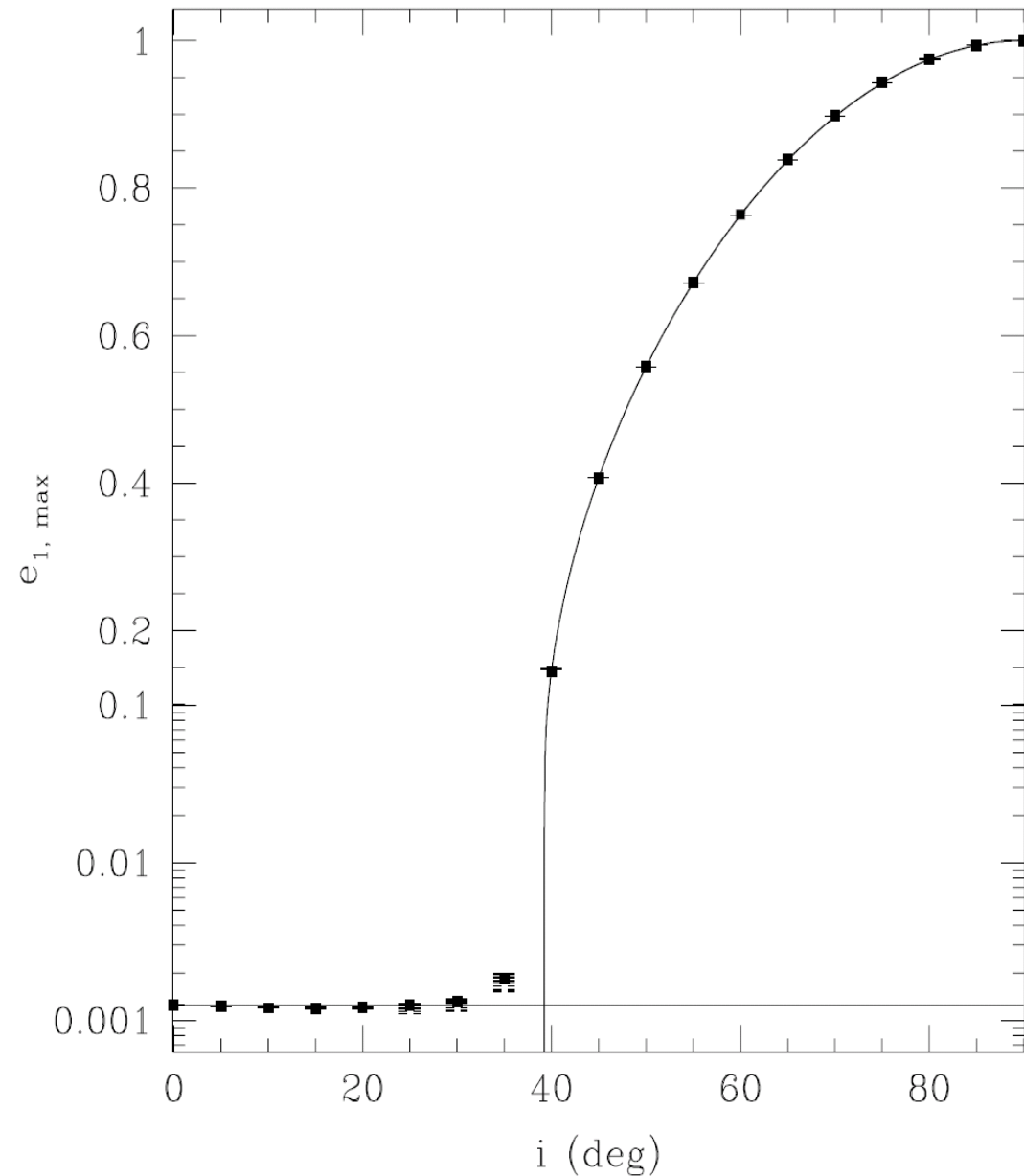




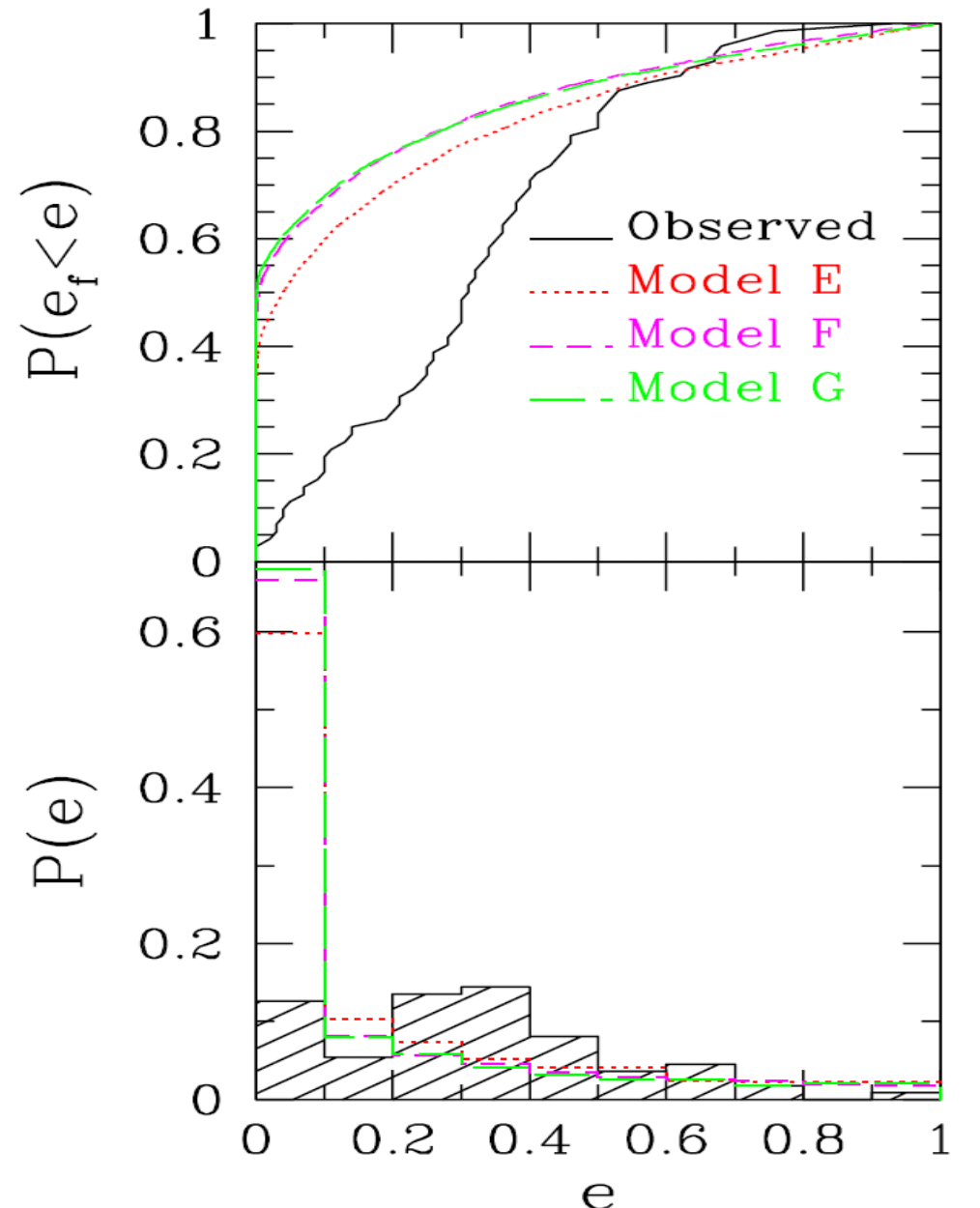
# How to Excite Eccentricities?

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- **Hybrid Scenarios** (Marzari et al. 2005, Sandor & Kley 2006)

# Binaries Exciting Eccentricities



Ford et al. 2000



Takeda & Rasio 2005



# How to Excite Eccentricities?

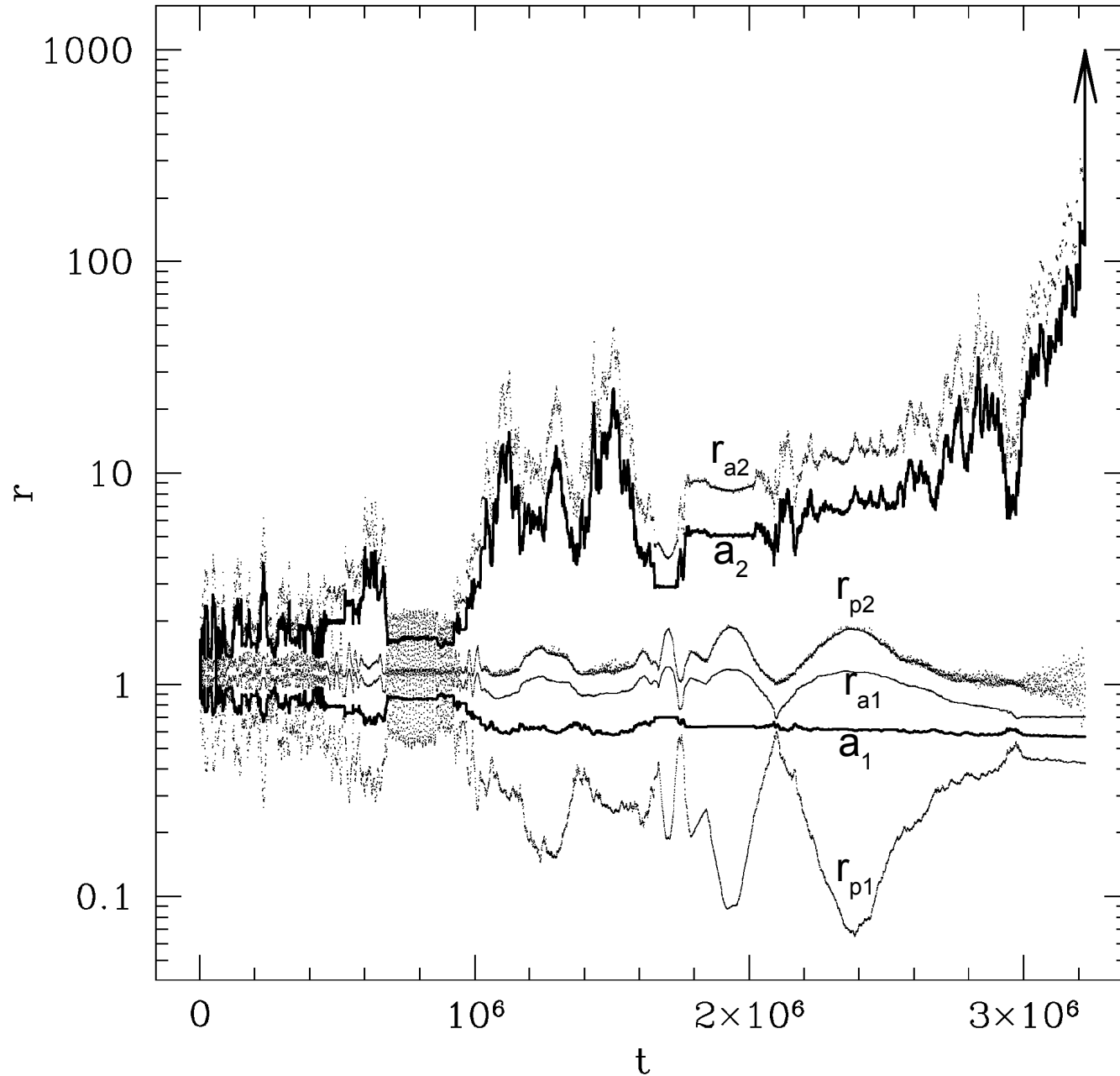
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- **Hybrid Scenarios** (Marzari et al. 2005, Sandor & Kley 2006)

# How to Excite Eccentricities?

- Planet-Planet Scattering

- Two Planets, Equal Mass (Rasio & Ford 1996, Ford et al 2000)
- Two Planets, Unequal Masses (Ford et al. 2003, Veras & Armitage 2003, Ford & Rasio 2007)
- Three Planets (Weidenschilling & Marzari 1996, Marzari & Weidenschilling 2002, Ford et al. 2003, Veras & Armitage 2004, Chatterjee et al. 2007)
- Many Planets (Lin & Ida 1997, Papaloizou & Terquem 2001, Adams & Laughlin 2003, Goldreich et al. 2005, Ford & Chiang 2007, Juric & Tremaine 2007)
- Convergent Migration & Resonant Capture (Lee & Peale 2003; Sandor et al. 2006)
- Three Planets in Binary Star (Marzari et al. 2005)

# Planet-Planet Scattering



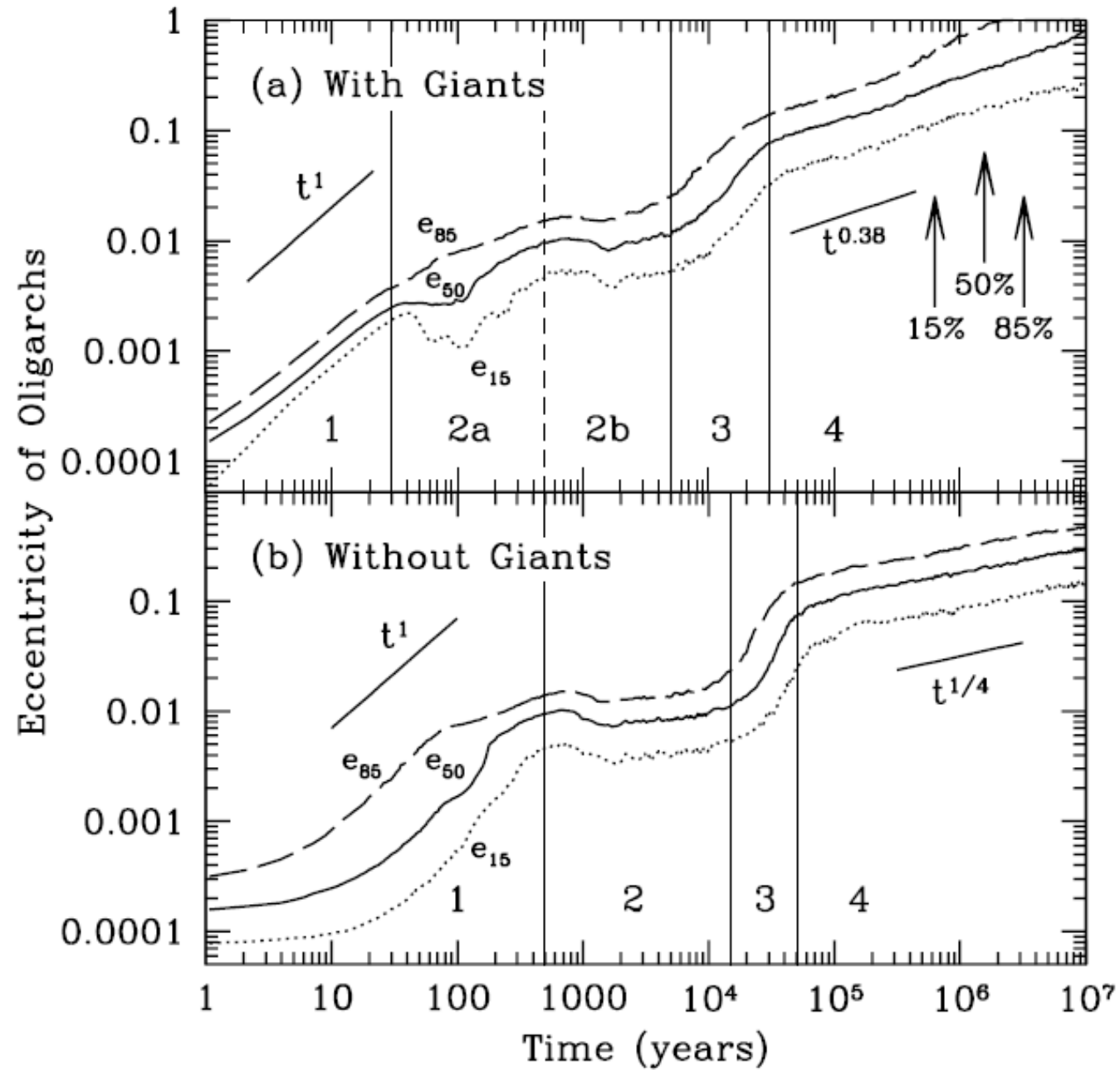
- Two giant planets initially on nearly circular orbits
- Dynamical instability leads to close encounters
- Typically results in planets colliding or one being ejected
- Sometimes planet acquires small pericenter distance

Rasio & Ford 1996

# Triggers for Dynamical Instability

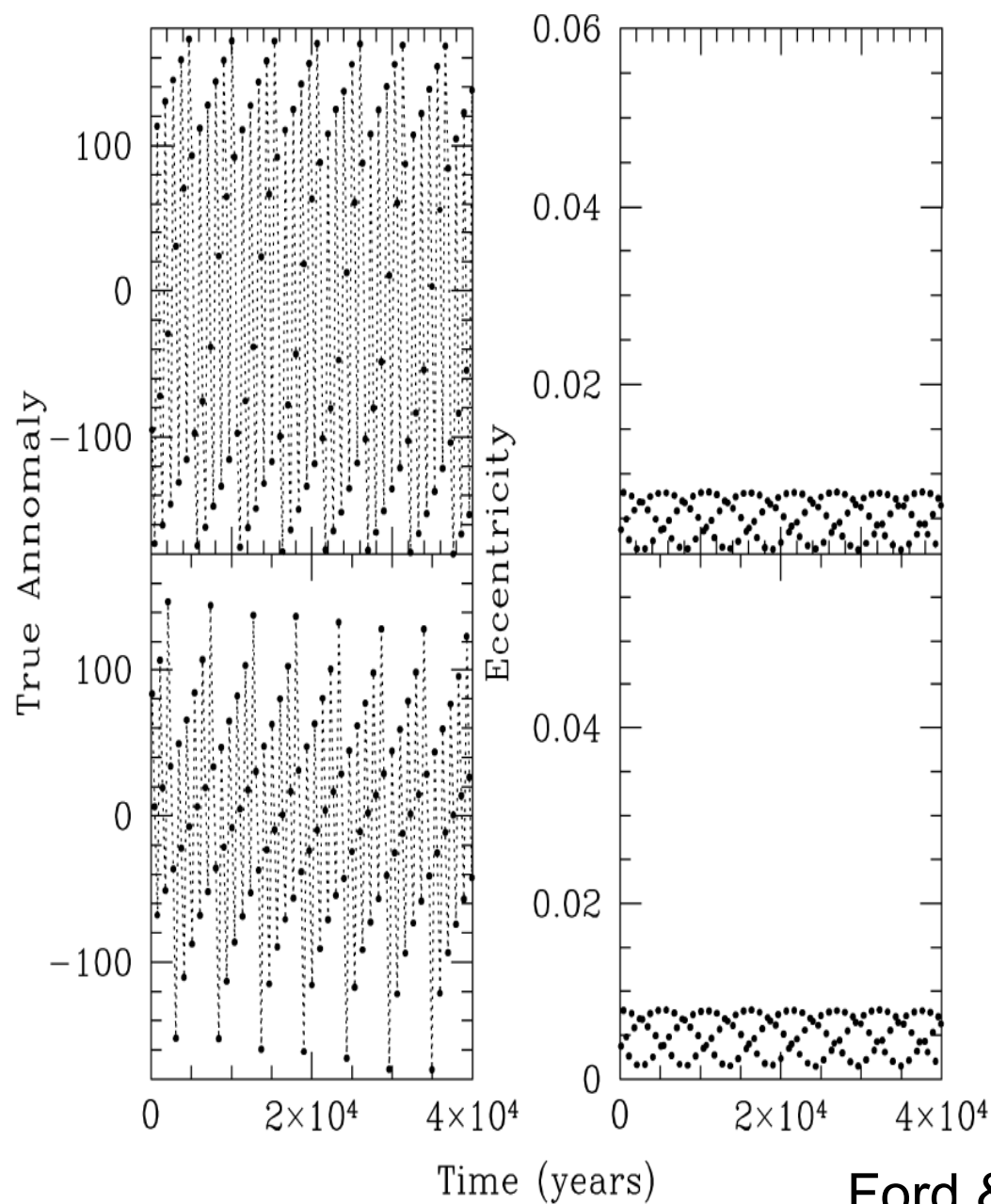
- Dissipation of Protoplanetary Disk
- Mass Growth
- Secular Evolution
  - Multiple Planet Systems
  - Wide Stellar Binary Companions
- Migration
  - Convergent
  - Divergent crossing of Mean Motion resonances
- Distant Stellar Encounters

# Eccentricity Growth

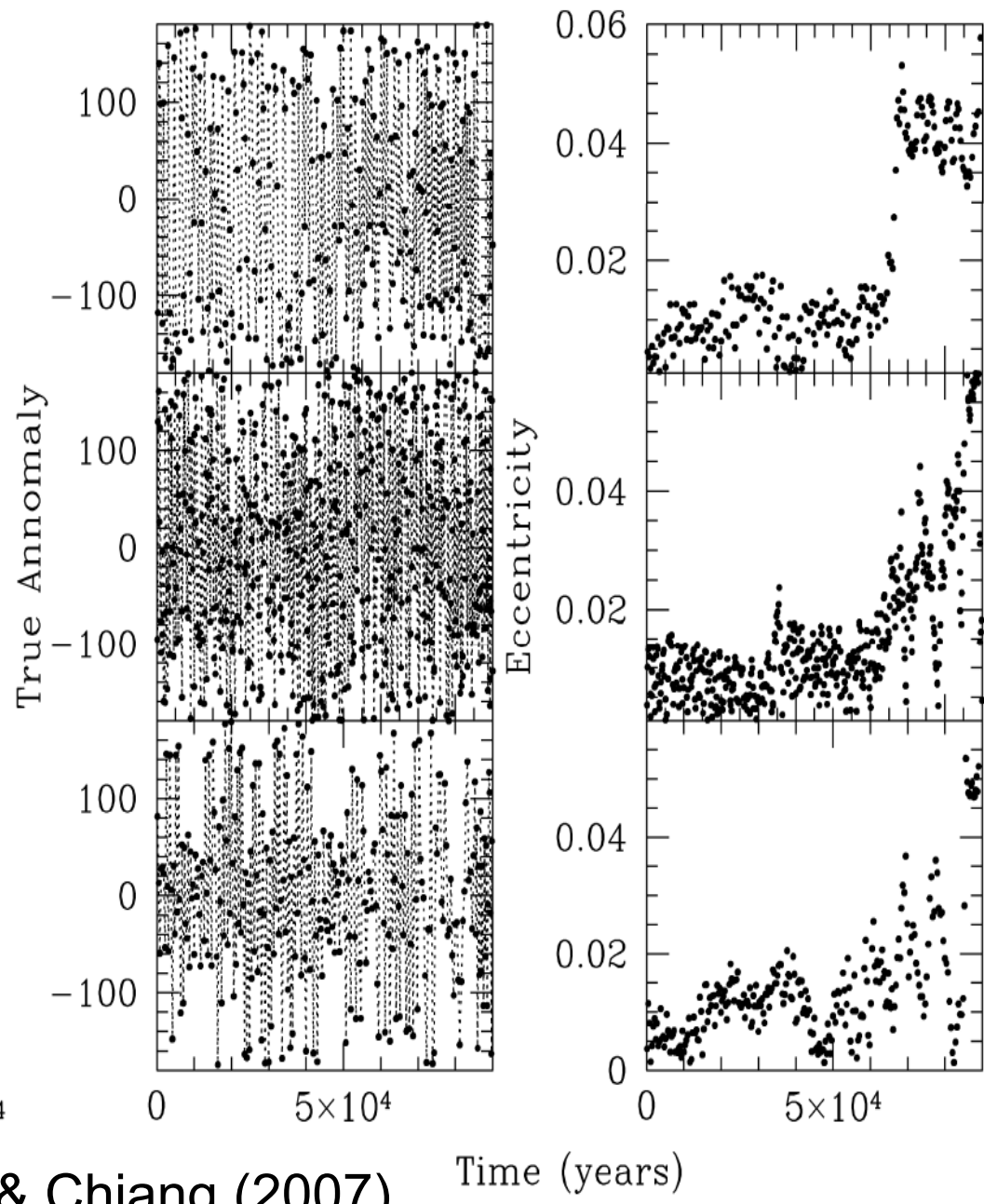


# Route to Chaos

## Two Planets

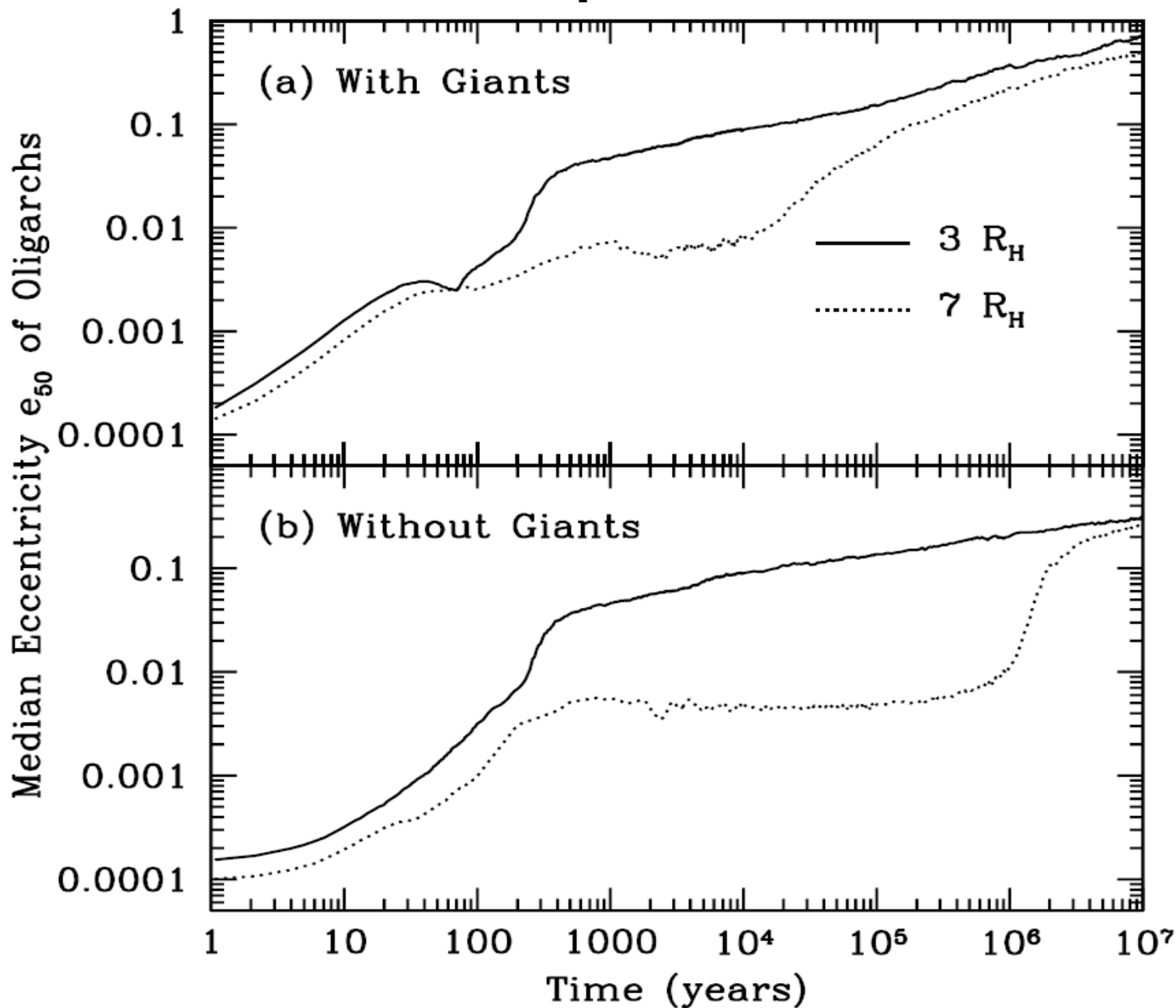


## Three Planets

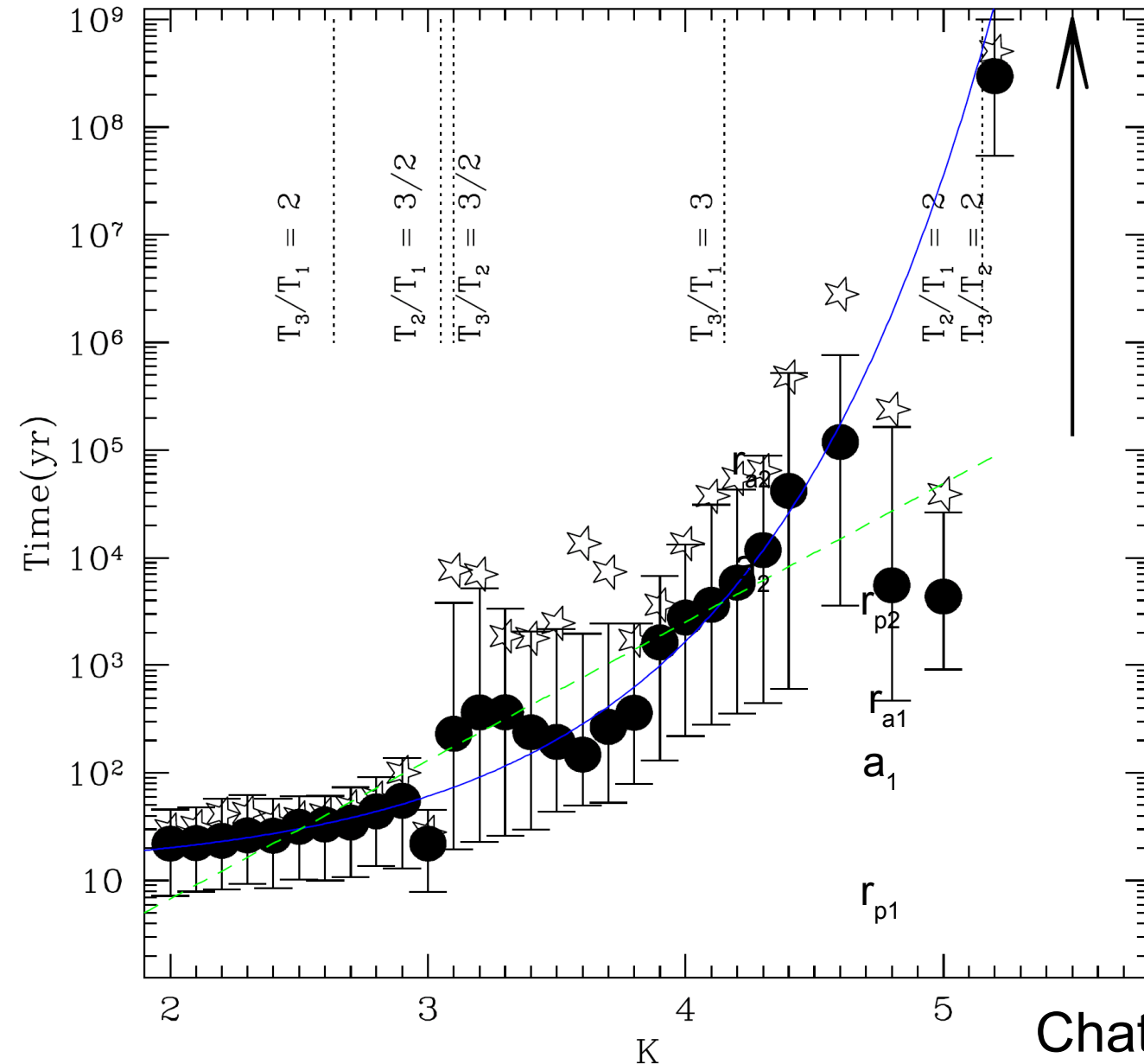


Ford & Chiang (2007)

# Eccentricity Growth of Five Neptune Mass Planets



# Timescale Until Instability for Three Giant Planets



- Three giant planets initially on *well-separated* nearly circular orbits
- Timescale until dynamical instability depends on the masses and spacing
- Timescale until a dynamical instability is manifest can be arbitrarily long

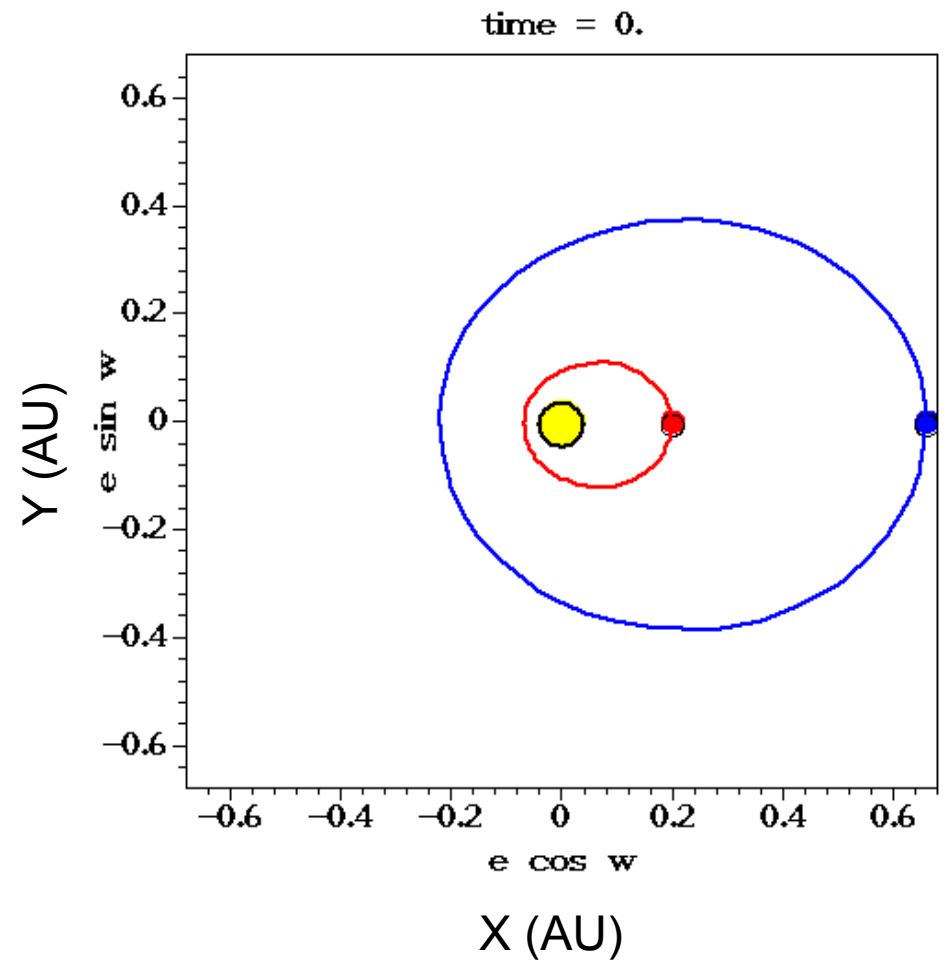
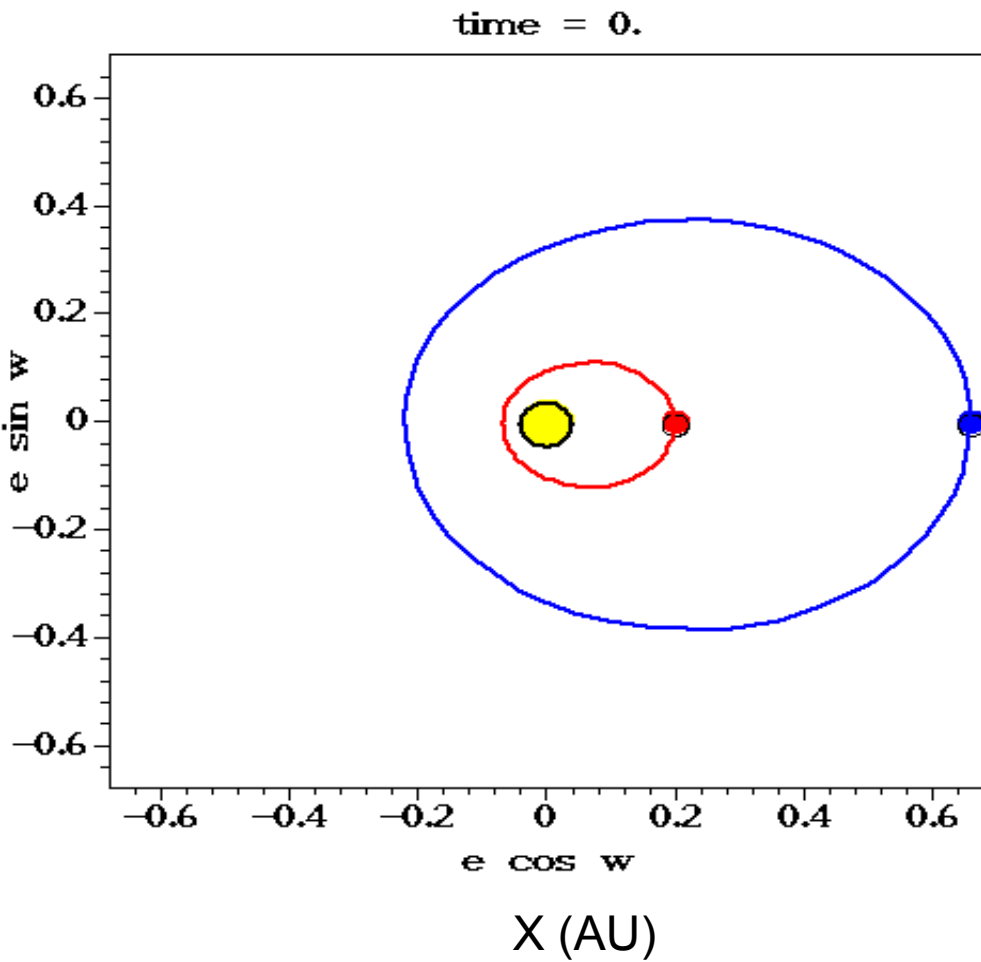
Chatterjee et al. 2007 see also Marzari & Weidenschilling 2003



# u Andromedae

- First multiple planet system discovered around main sequence (F8V,  $1.3 M_{\odot}$ , 3Gyr) star in 1999.
- Now have  $\sim 450$  radial velocity observations with precision limited by stellar jitter of  $\sim 7.5\text{m/s}$
- u And c & d have significant eccentricities ( $\sim 0.26$  &  $0.28 \pm 0.02$ )
- Significant secular eccentricity evolution
- What is the origin of these eccentricities?

# Circulation vs Libration



# How to Excite Eccentricities?

- Adiabatic Torque on  $u$  And  $d$
- Impulsive Perturbation to  $u$  And  $d$

# How to Excite Eccentricities?

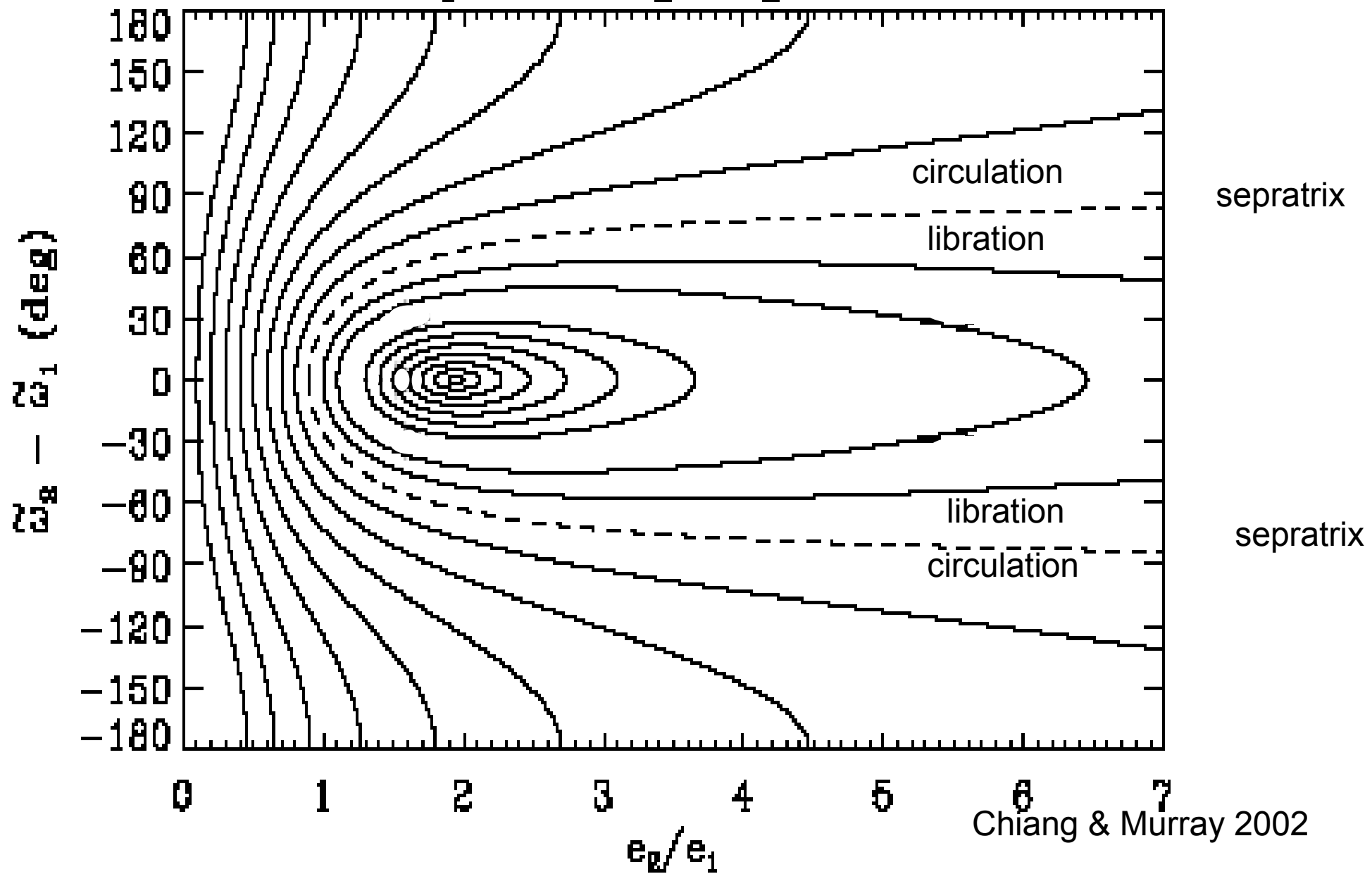
- Adiabatic Torque on  $u$  And  $d$ 
  - Gas disk beyond  $u$  And  $d$
  - Excites Eccentricity of  $u$  And  $d$
  - Drives System from Circulating to Librating Regime
  - Damps Libration Amplitude about Aligned Configuration
  - Predicts: Small Libration Amplitude & Small Eccentricity Oscillations

# How to Excite Eccentricities?

- Impulsive Perturbation to u And d
  - Additional Massive Planet (u And e,  $\sim 1.9 M_{\text{Jup}}$ )
  - Chaotic Evolution ( $\sim 1,000$  yrs)
    - u And e *Ejected*
    - u And d remains on *Eccentric Orbit*
    - u And c remains on orbit which may be circular *or* eccentric
    - Secular Interactions between c & d lead to current orbits
  - Predicts either Circulation or Large Amplitude Libration and Significant Eccentricity Evolution

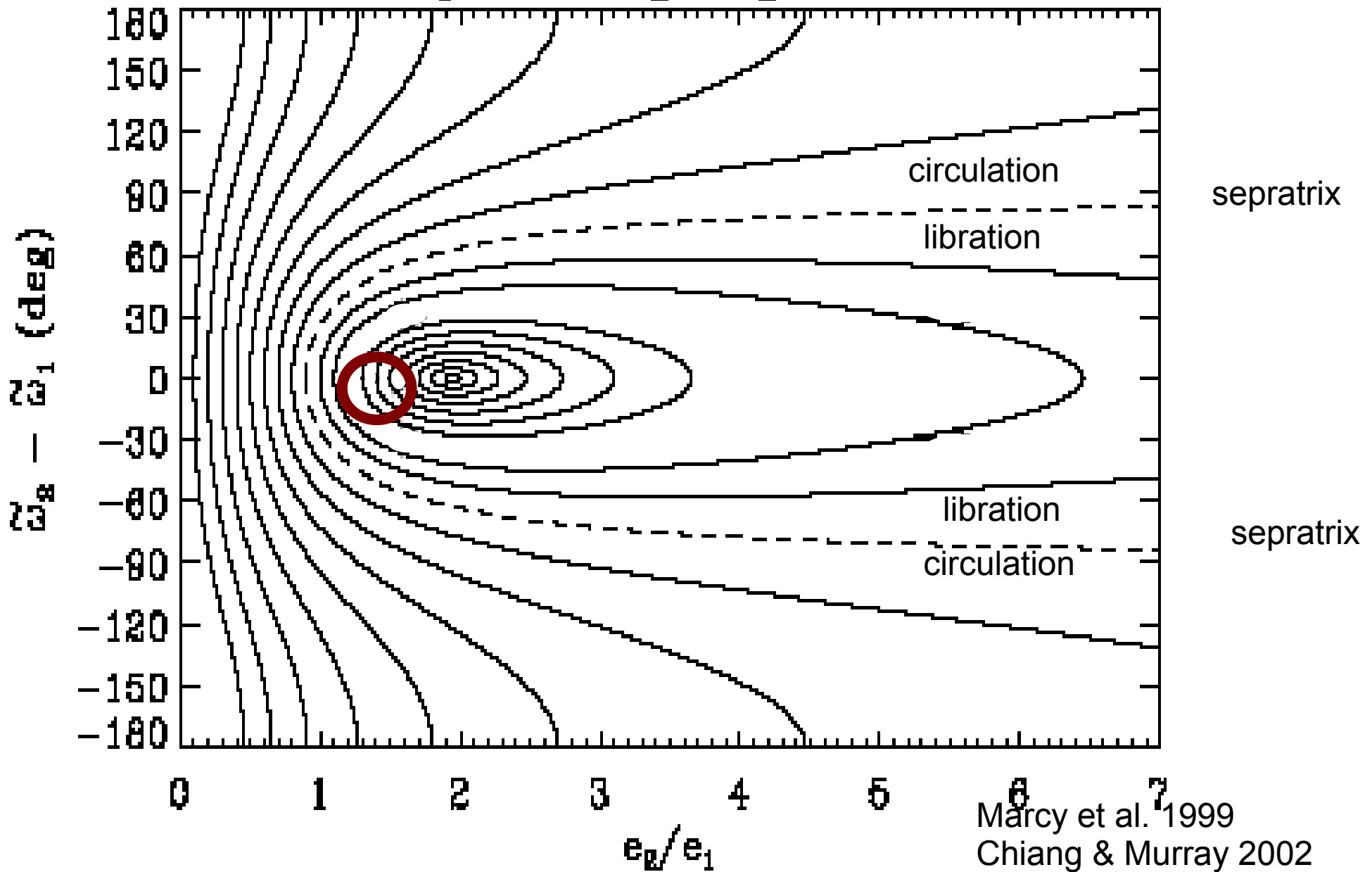
# Secular Eccentricity Evolution

## Laplace-Lagrange Contours



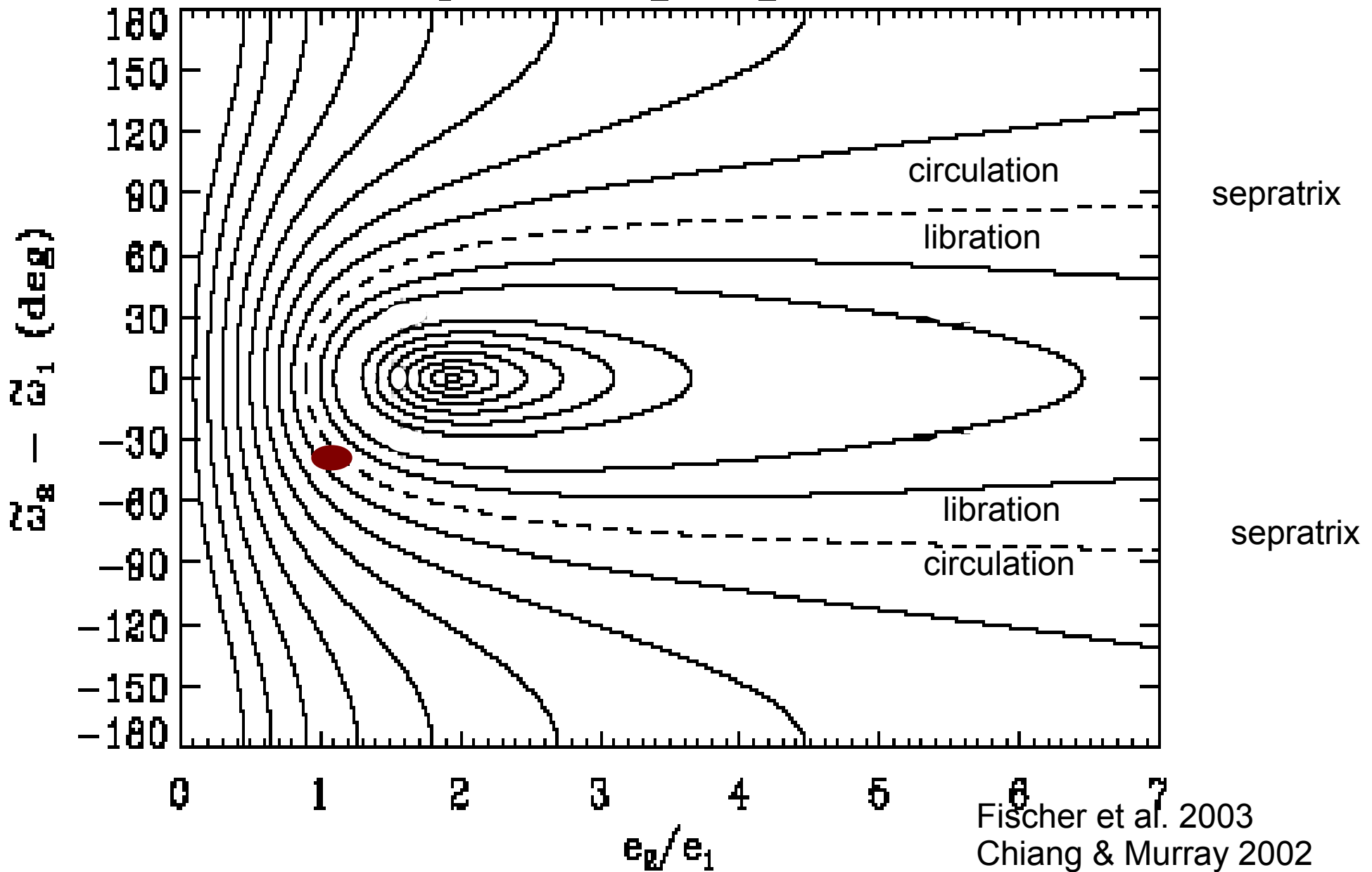
# Secular Eccentricity Evolution

## Laplace-Lagrange Contours



# Secular Eccentricity Evolution

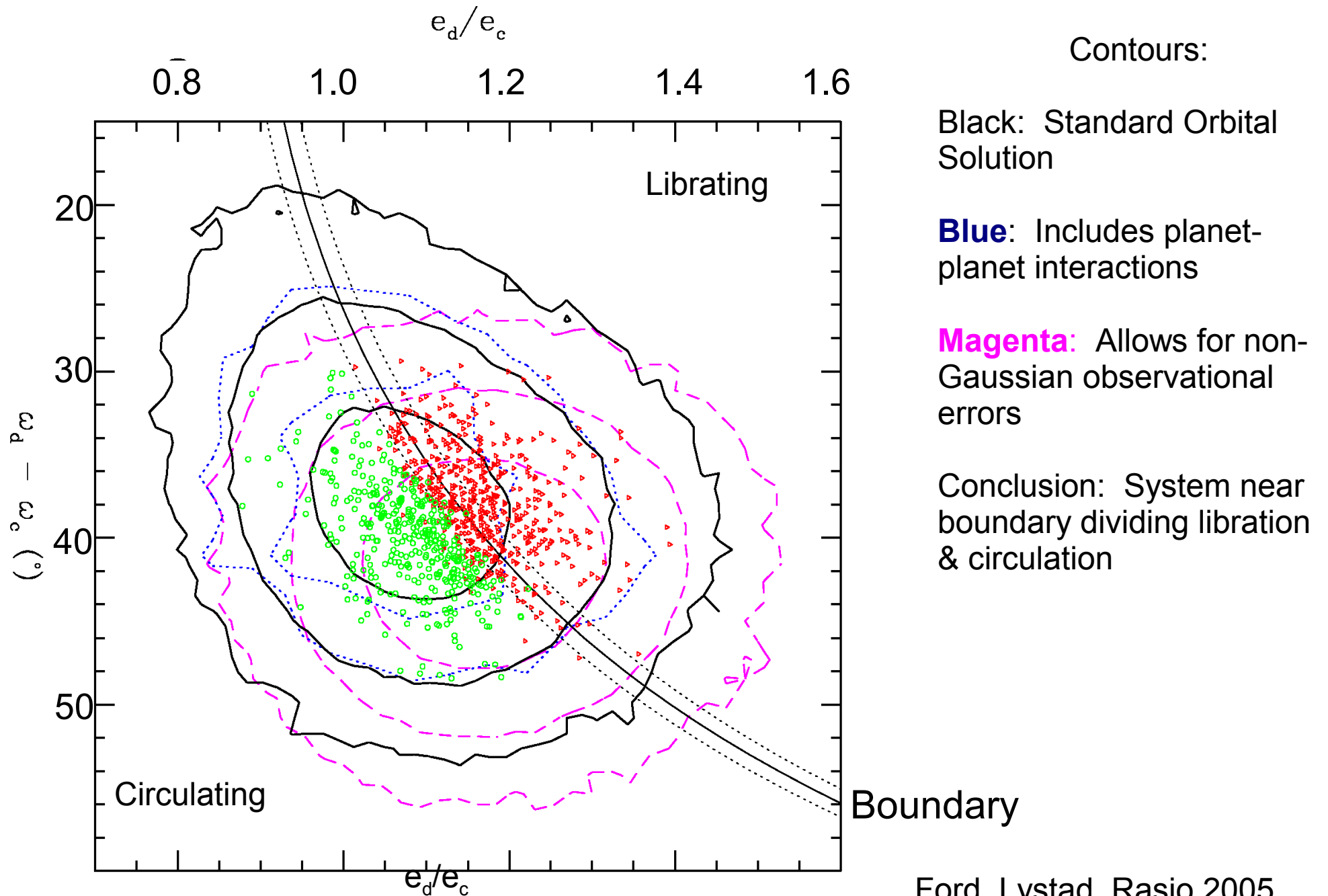
## Laplace-Lagrange Contours



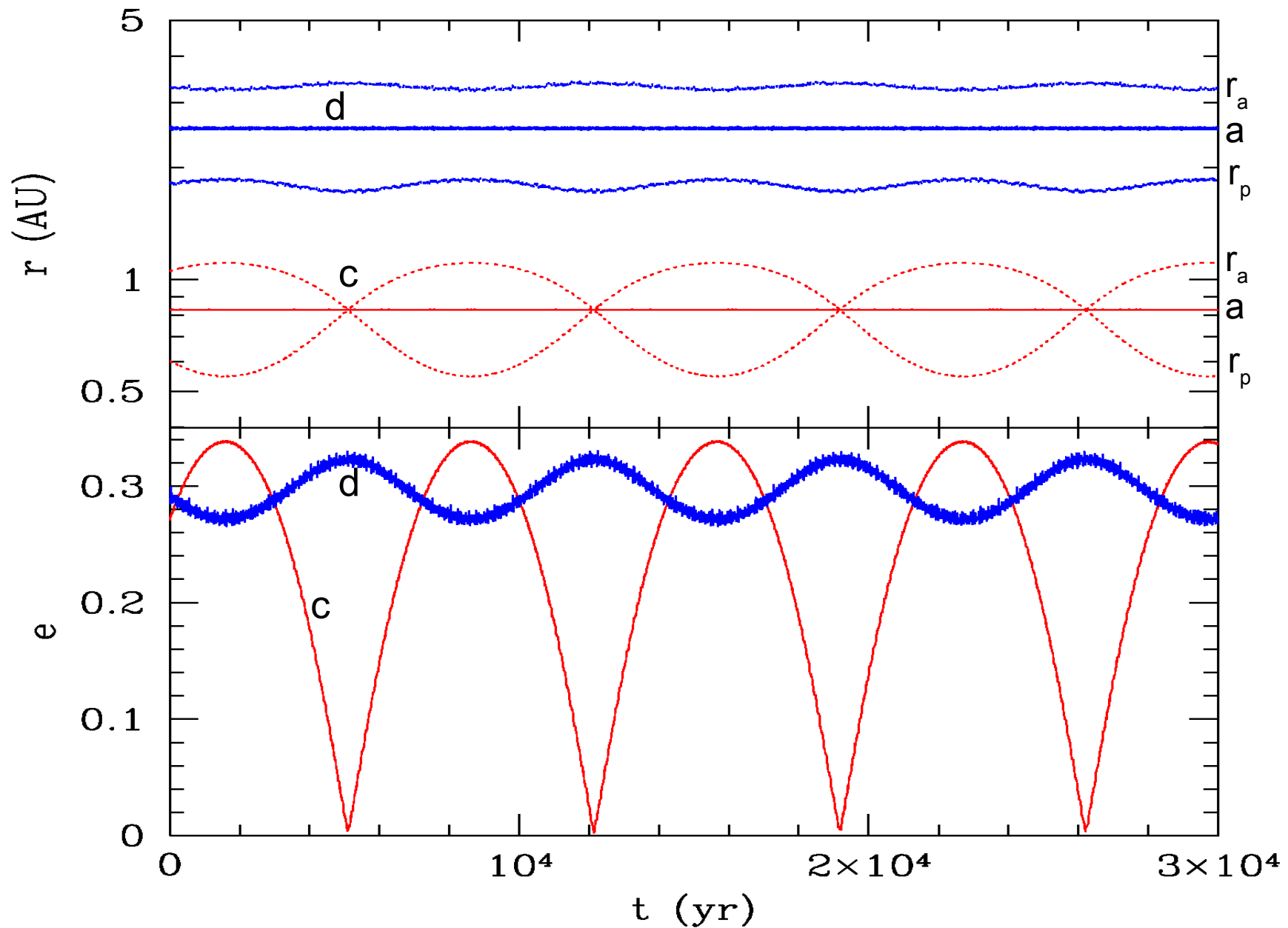
Fischer et al. 2003  
Chiang & Murray 2002



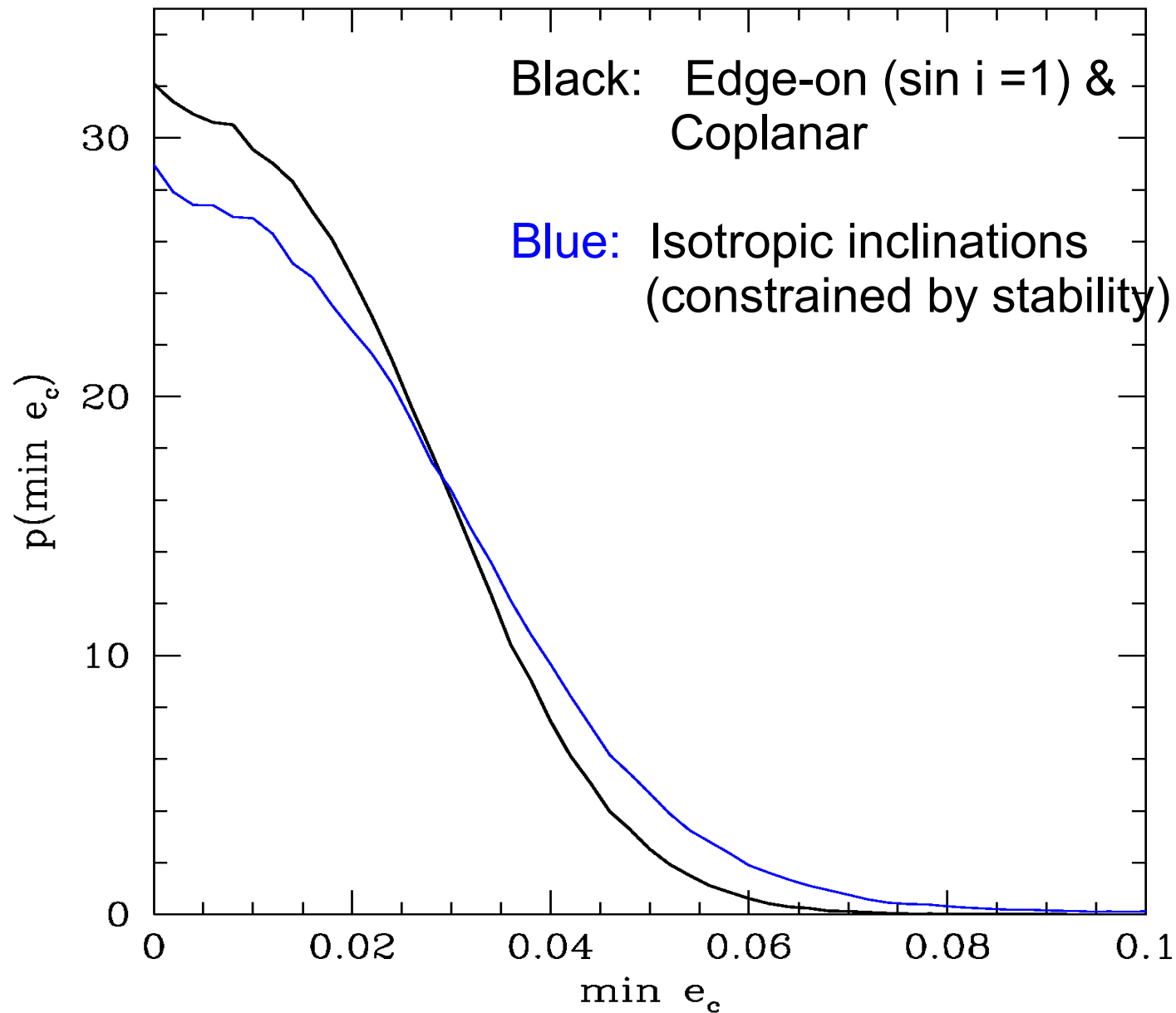
# Current Location in Phase Space



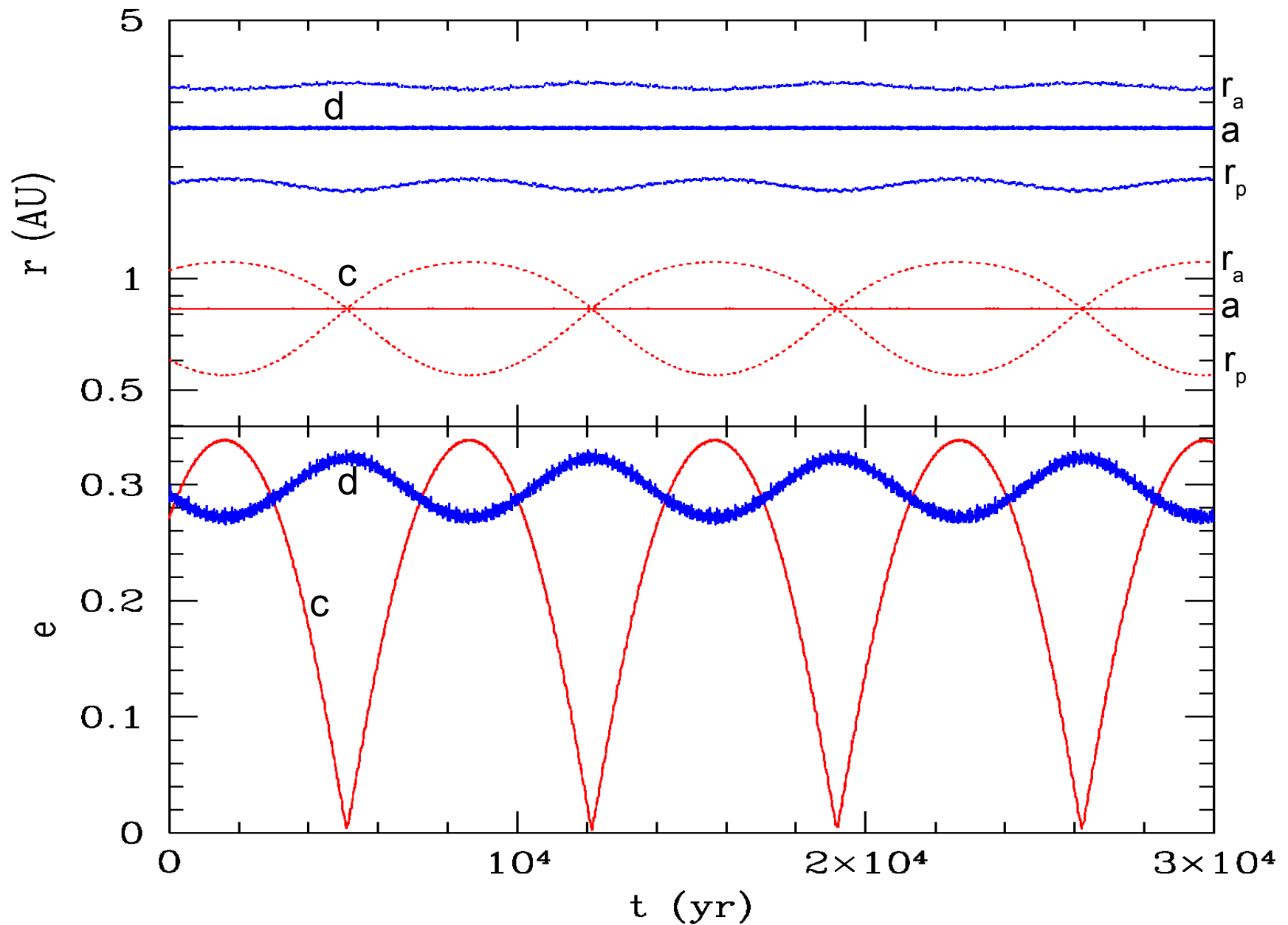
# Secular Evolution



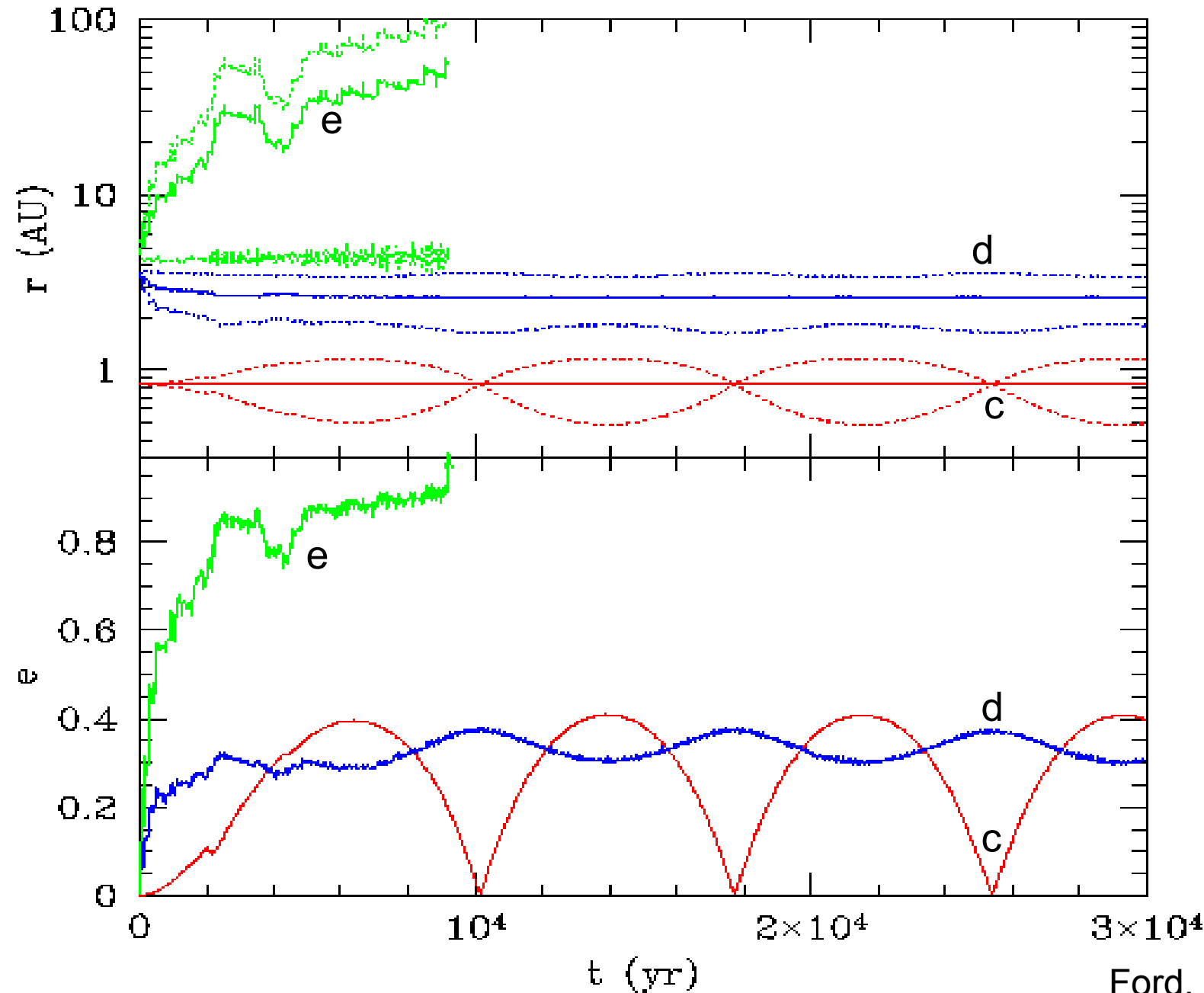
# Minimum Eccentricity of Ups And c



# Secular Evolution



# Impulsive Formation Scenario



Initial:  
 $P_d = 5.8$  yr  
 $m_d = 3.8 M_{\text{Jup}}$   
 $e_d = 0.003$   
 $P_e = 8.7$  yr  
 $m_e = 1.9 M_{\text{Jup}}$   
 $e_e = 0.004$

Final:  
 $P_d = 3.7$  yr  
 $e_d = 0.29$

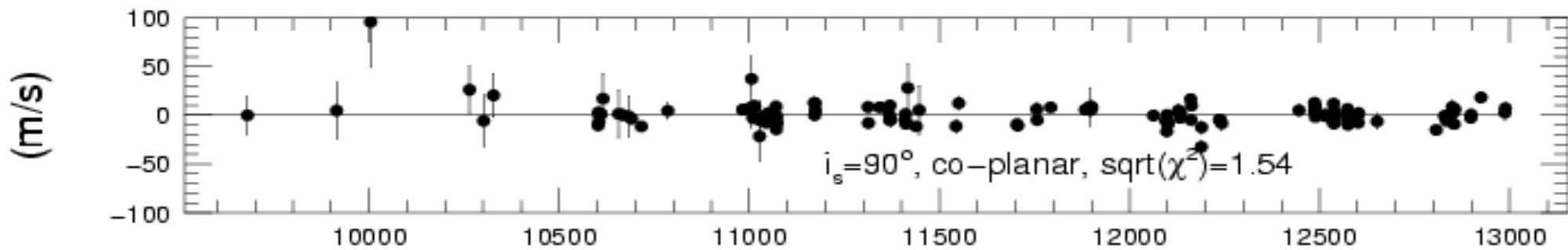
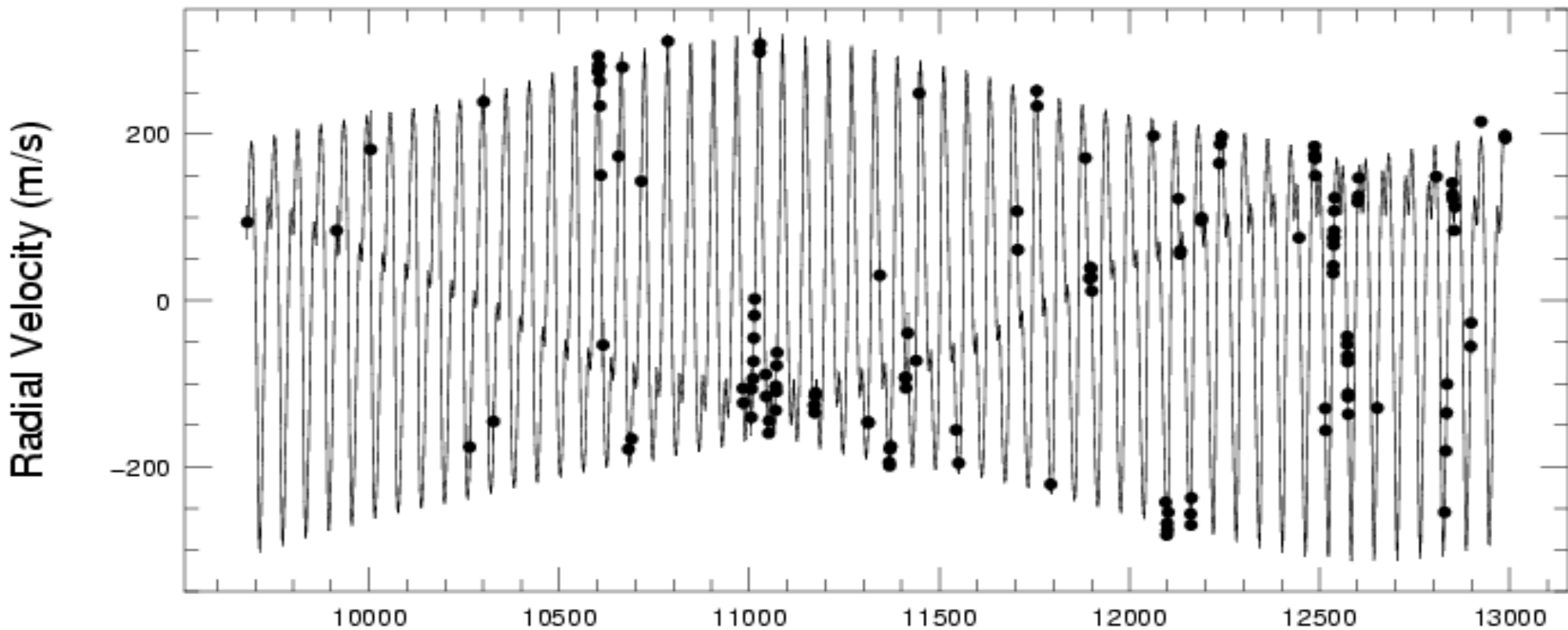
# Conclusions for u And c & d

- Very near boundary of libration & circulation
- If librating, large amplitude
- u And c periodically returns to  $e_c \sim 0.01$
- Implies u And c & d initially on circular orbits when u And d received impulsive perturbation
- Secular evolution transfer eccentricity to u And c
- Impulsive perturbation naturally provided by Planet-Planet scattering of  $\sim 1.9 M_{\text{Jup}}$  planet
- Multiple planet systems can provide valuable information about history of planet formation

# How to Excite Eccentricities?

- **Gas Disk** (Artymowicz 1992, Chiang & Murray 2002, Goldreich & Sari 2003, Papalouizou et al. 2001, Ogilvie & Lubow 2003)
- **Planetesimal Disk** (Murray et al. 1998)
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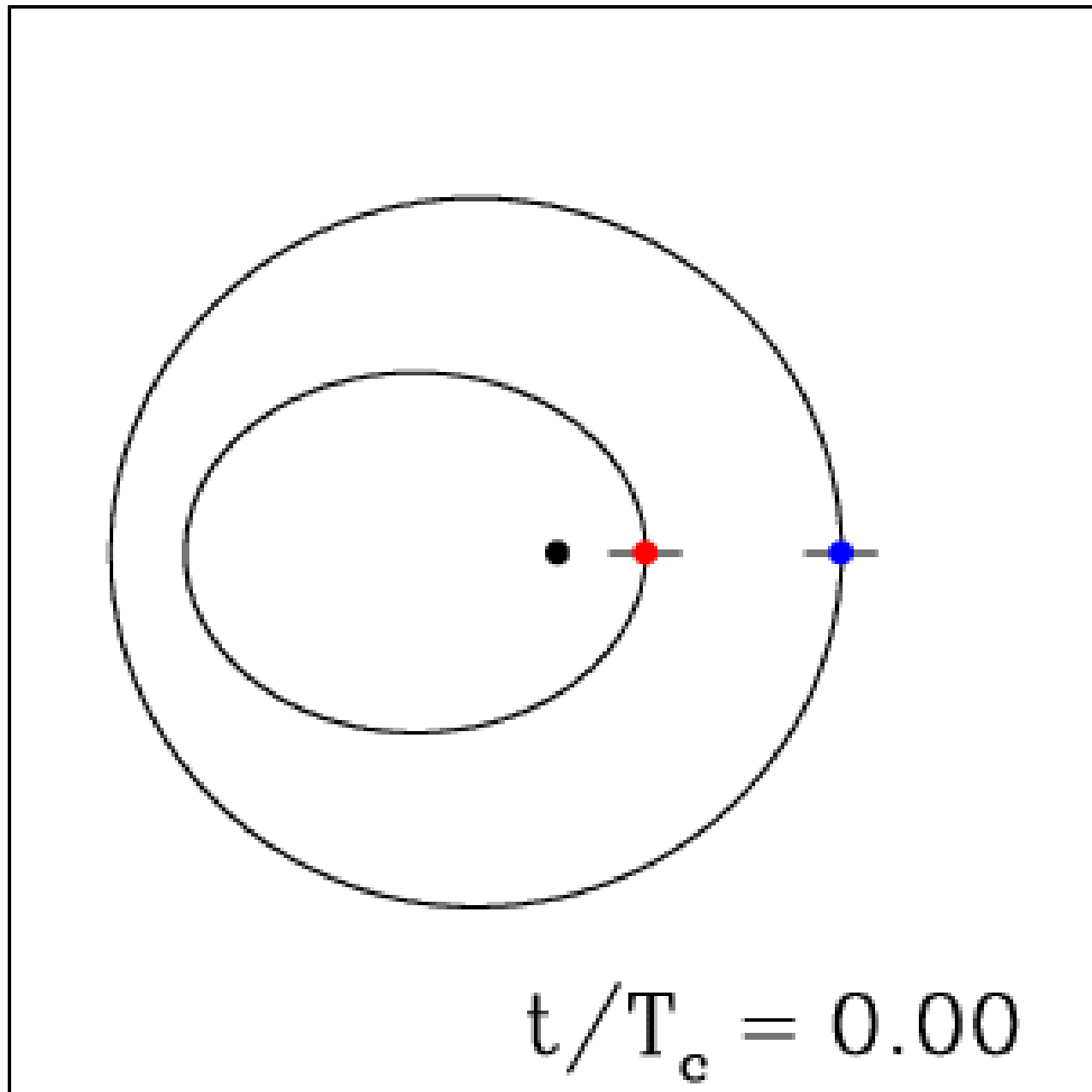
# GJ 876: Radial Velocities



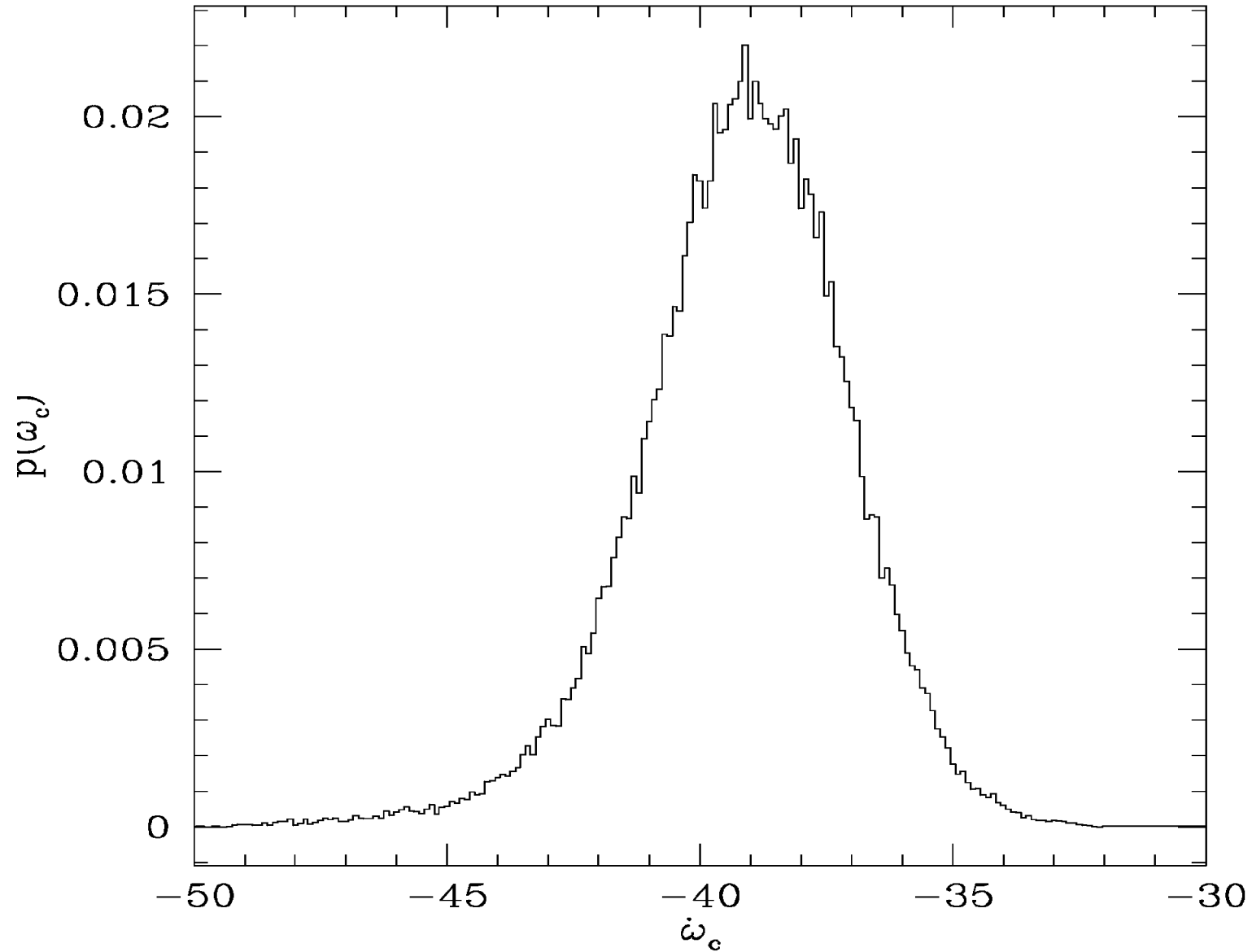
JD-2440000



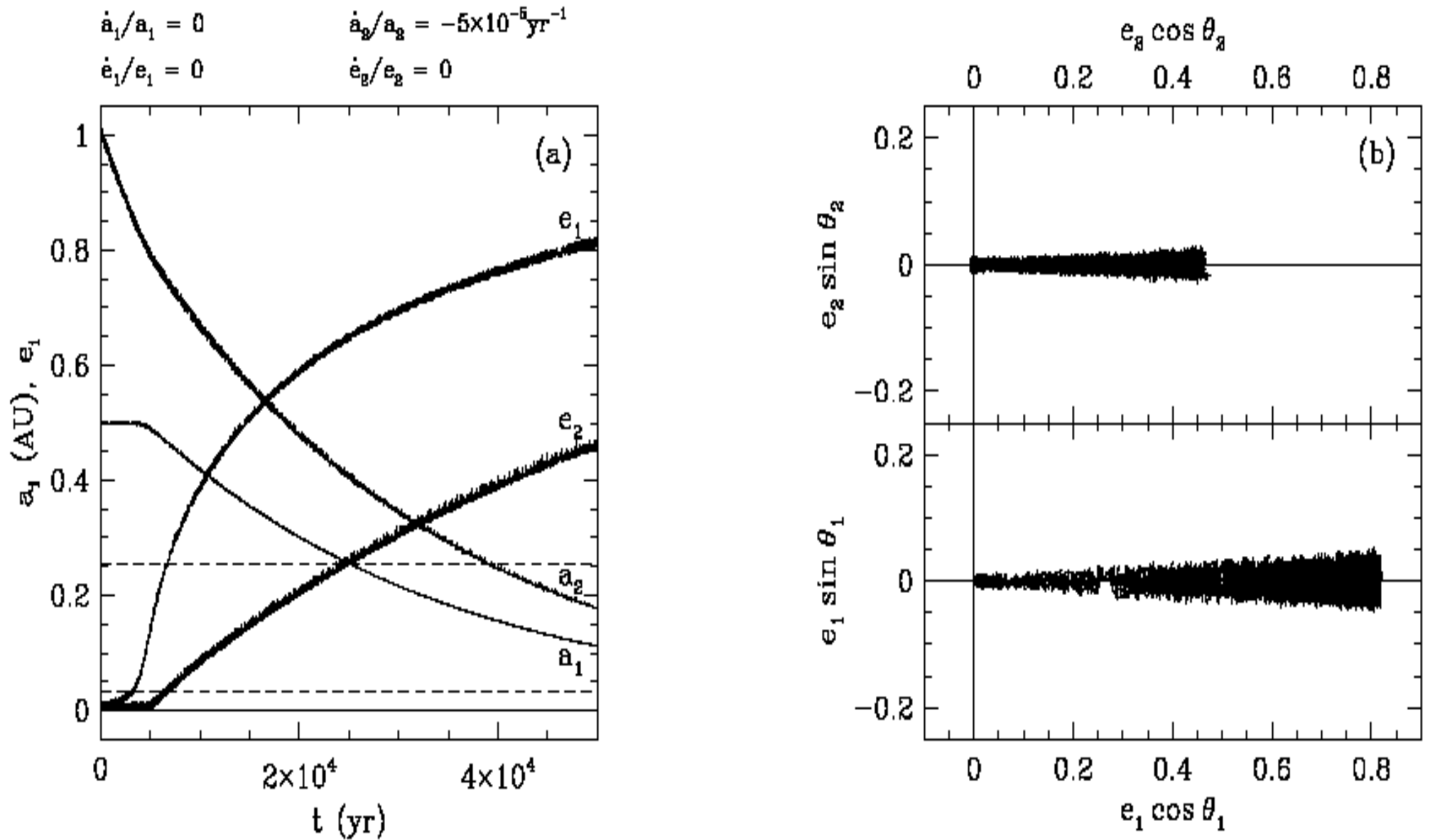
# GJ 876: Geometry



# GJ 876: Precession Rate

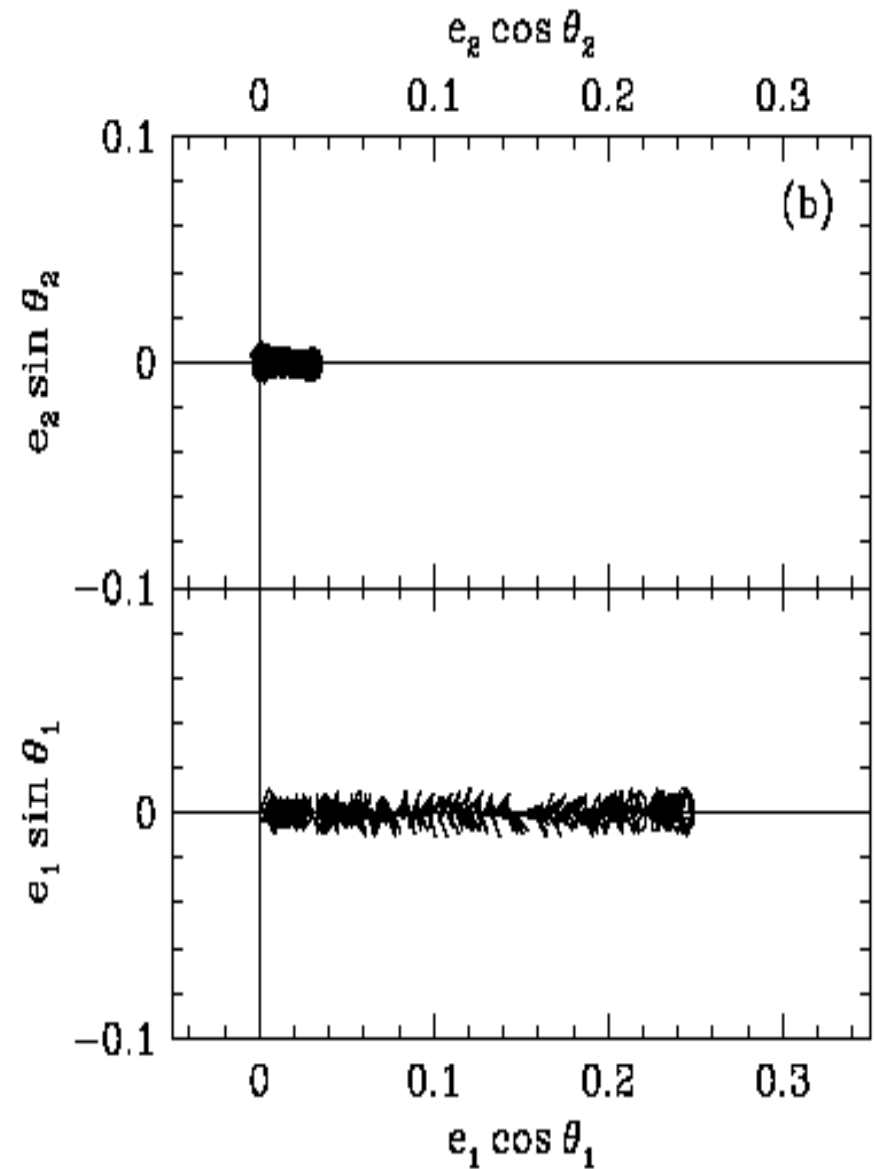
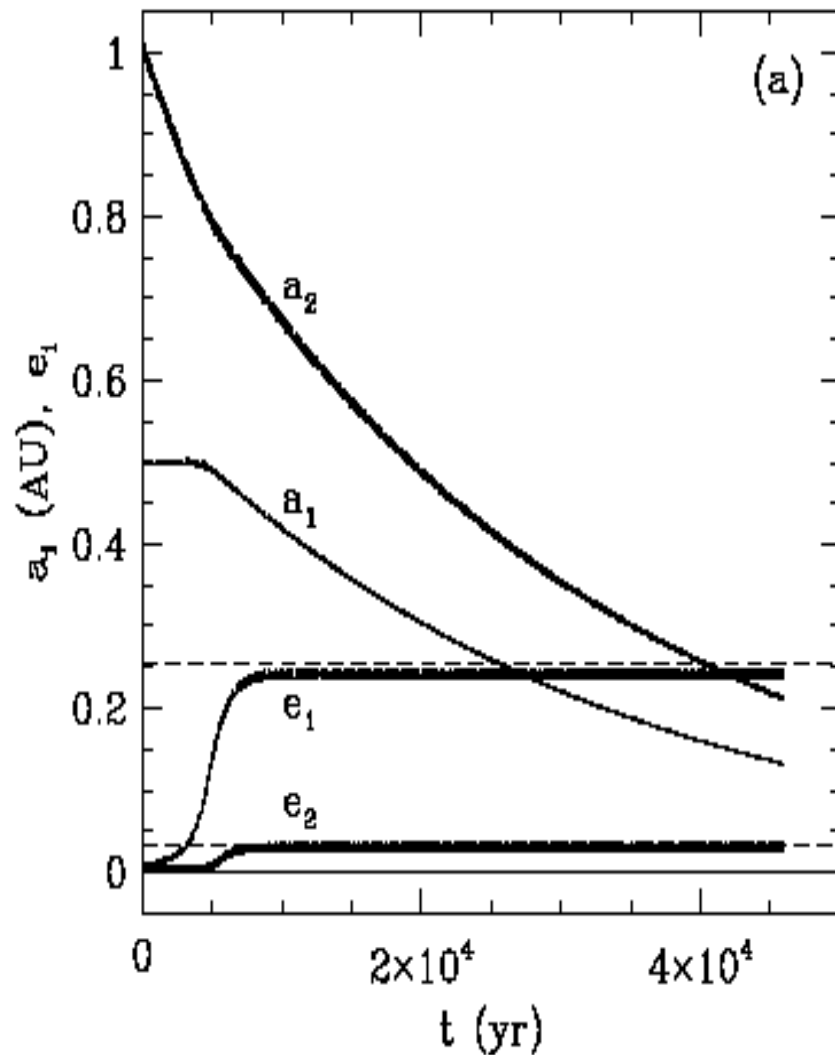


# GJ 876: Basic Migration



# GJ 876: Add Eccentricity Damping

$$\begin{aligned}\dot{a}_1/a_1 &= 0 & \dot{a}_2/a_2 &= -5 \times 10^{-6} \text{ yr}^{-1} \\ \dot{e}_1/e_1 &= 0 & \dot{e}_2/e_2 &= -100 |\dot{a}_2/a_2|\end{aligned}$$



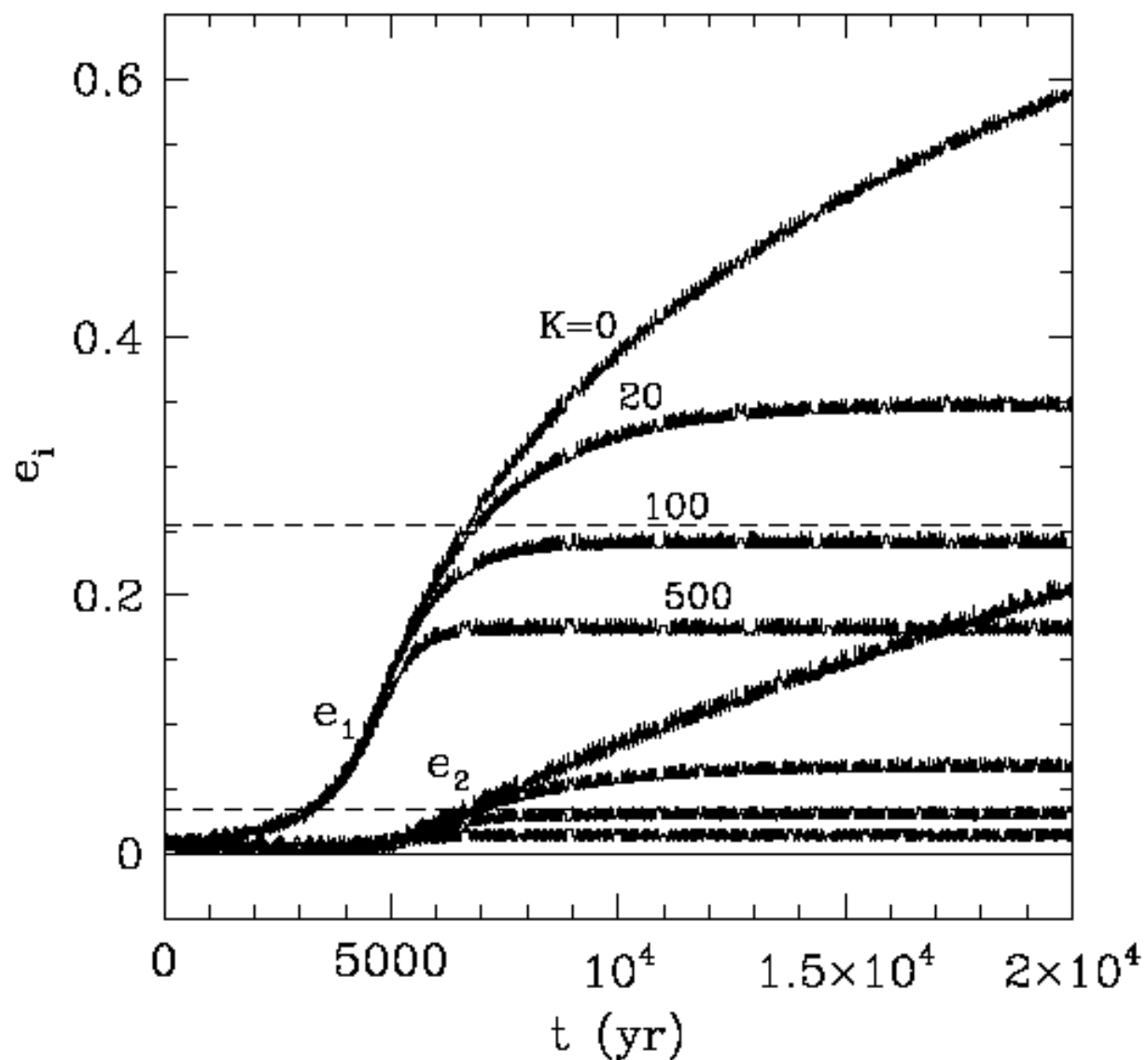
# GJ 876: Final Eccentricity vs Damping

$$\dot{a}_1/a_1 = 0$$

$$\dot{a}_2/a_2 = -5 \times 10^{-5} \text{ yr}^{-1}$$

$$\dot{e}_1/e_1 = 0$$

$$\dot{e}_2/e_2 = -K |\dot{a}_2/a_2|$$



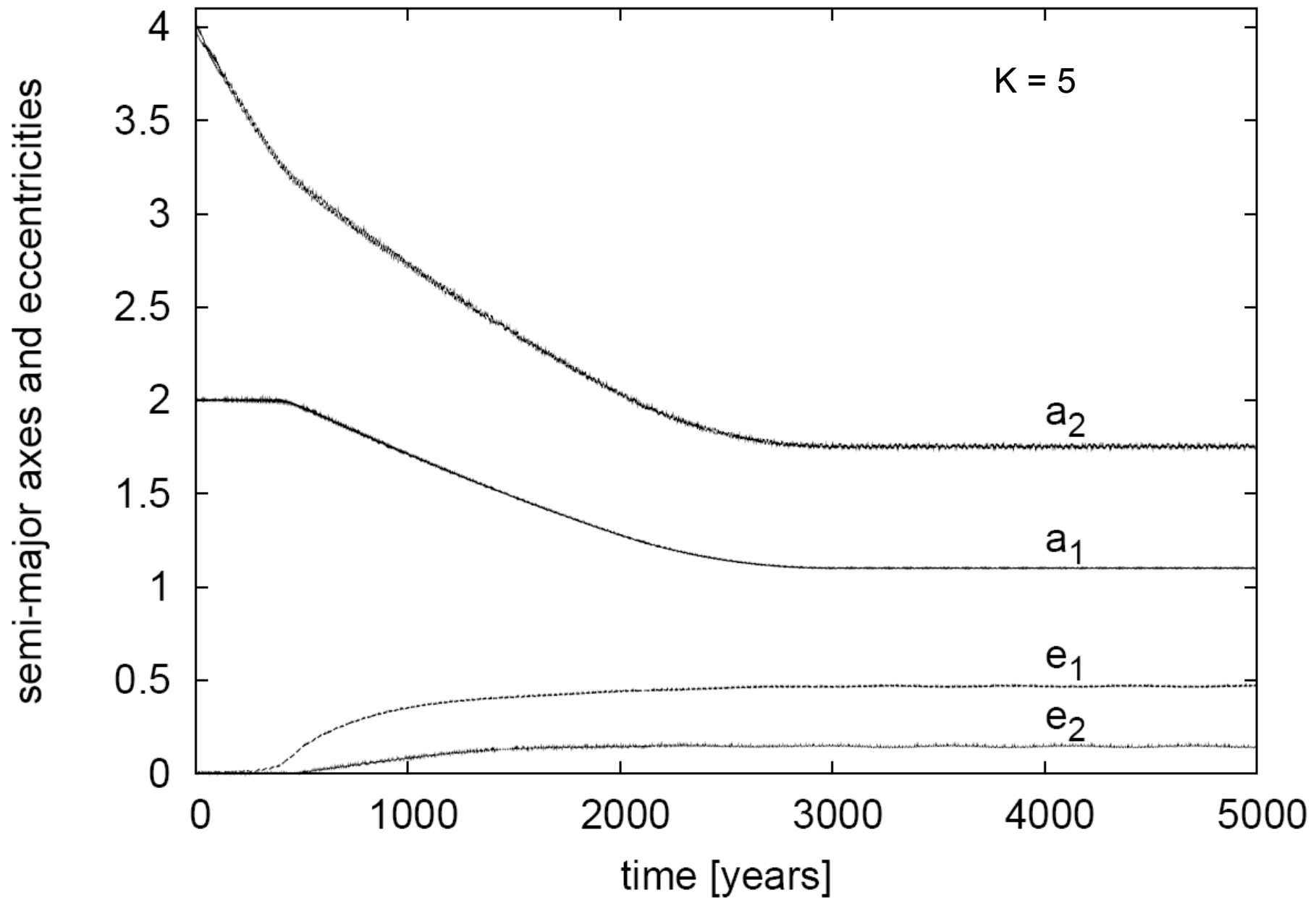
# Conclusions for GJ 876

- Planet-Planet interaction leads to rapid precession
- Precession rate constrains masses & orbits
- Differential migration naturally led to resonant capture into 2:1 mean motion resonance
- Measured eccentricities demand either:
  - Migration halt shortly after resonant capture
  - Strong eccentricity damping during migration
- Multiple planet systems provide valuable information about history of planet formation, especially when interactions are observed.

# Triggers for Dynamical Instability

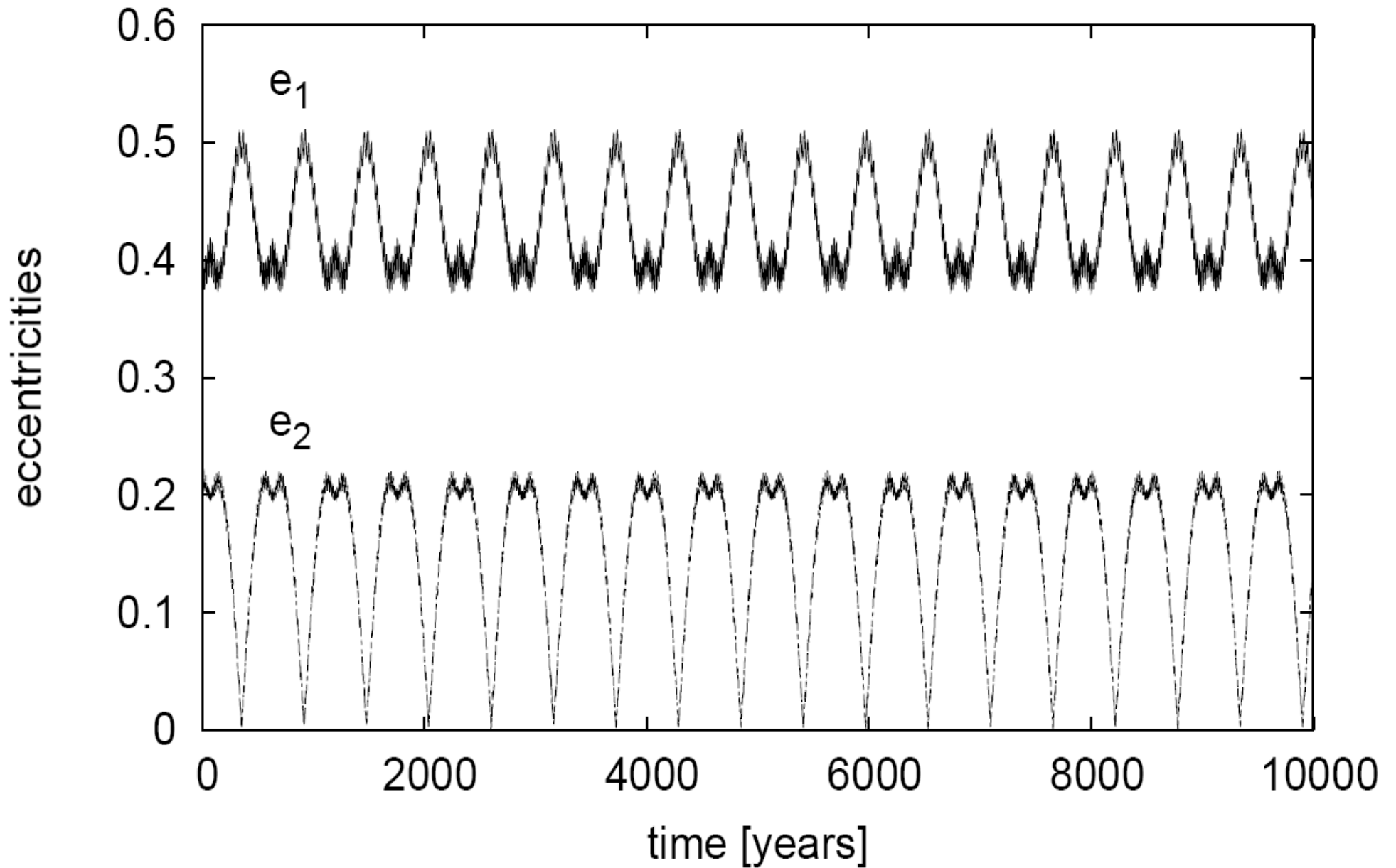
- Dissipation of Protoplanetary Disk
- Mass Growth
- Secular Evolution
  - Multiple Planet Systems
  - Wide Stellar Binary Companions
- Migration
  - Convergent
  - Divergent crossing of Mean Motion resonances
- Distant Stellar Encounters

# HD 128311: Resonant Capture

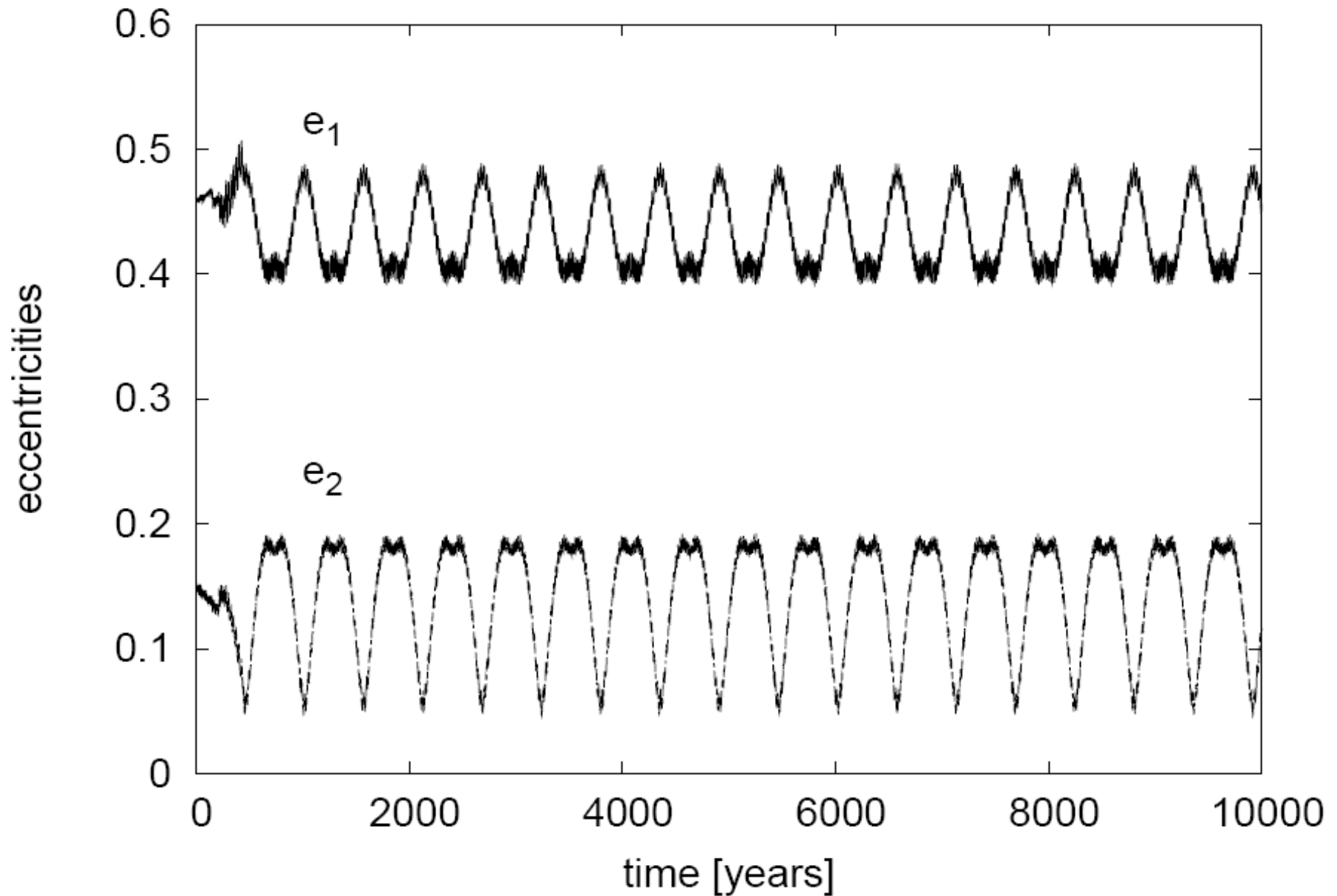




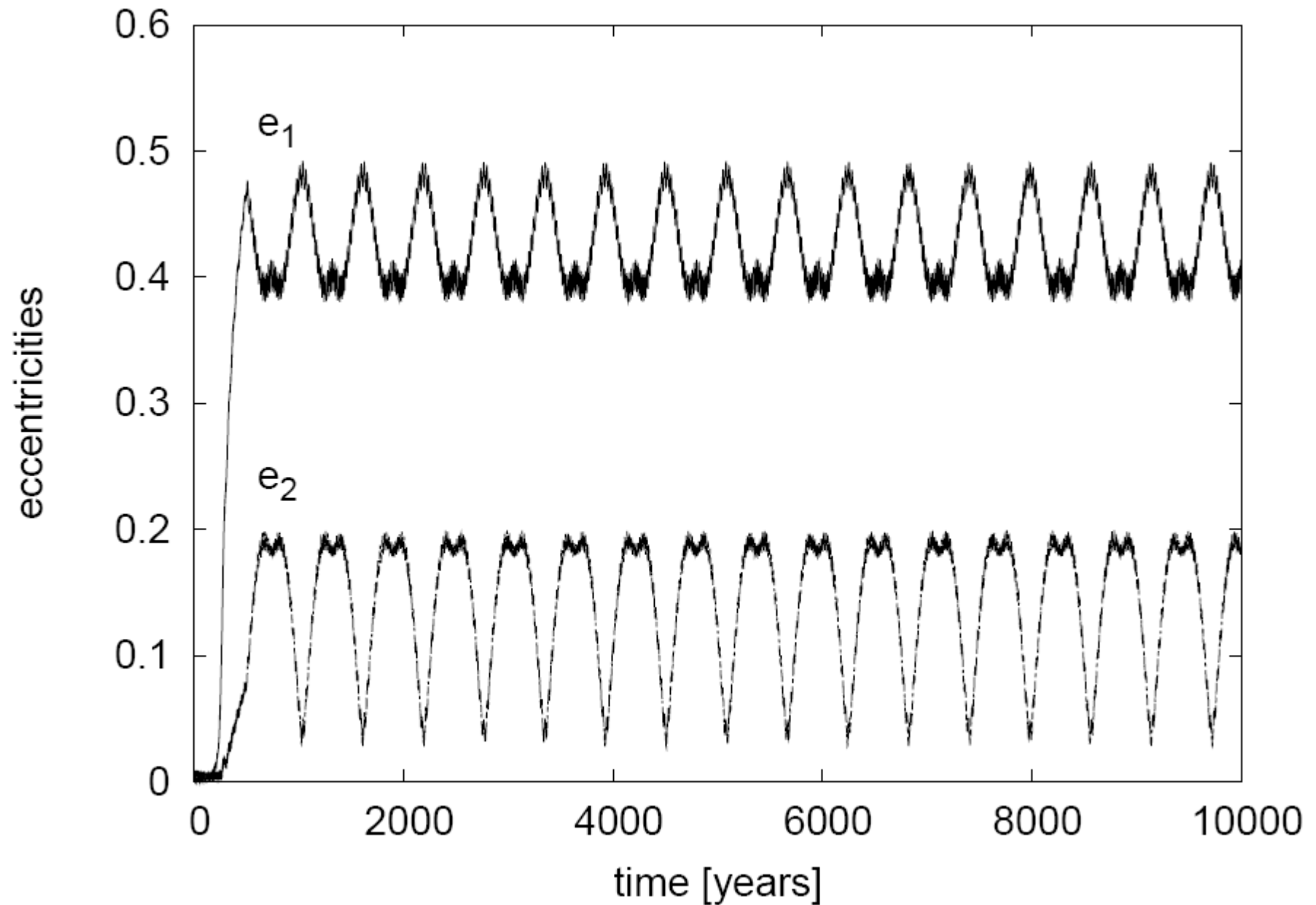
# HD 128311: Secular Evolution



# Resonant Capture + Planet Scattering



# HD 128311: Sudden Halt to Migration



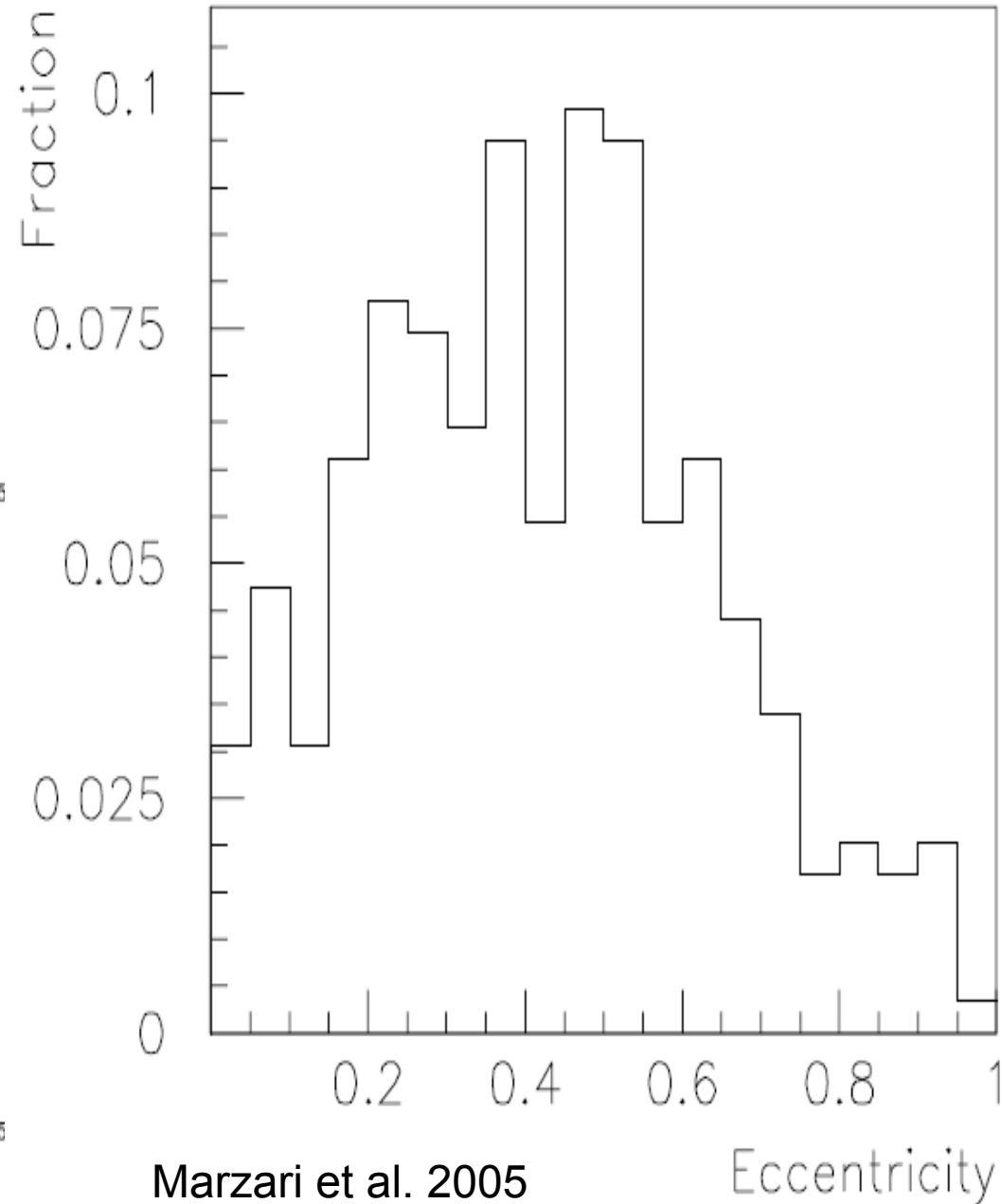
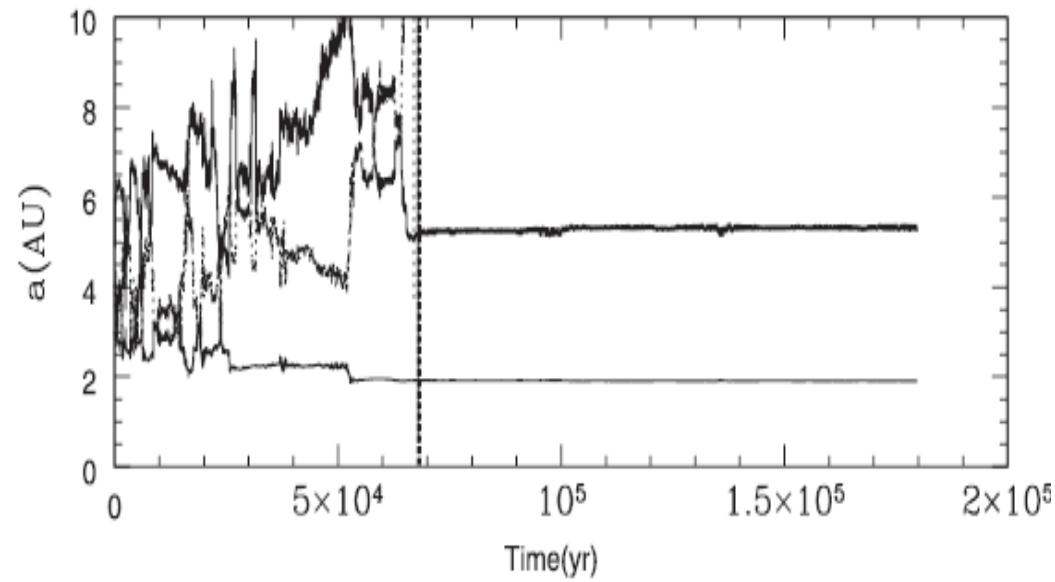
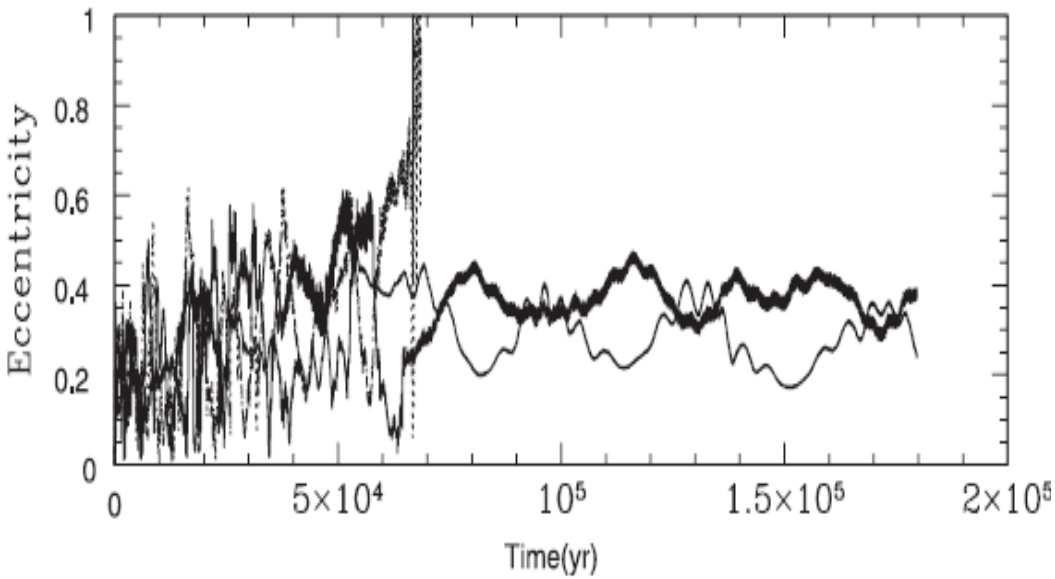
# Conclusions for HD 128311

- 2:1 Mean motion resonance suggests differential migration and resonant capture
- Measured eccentricities again suggest limited eccentricity growth after resonant capture:
  - Strong eccentricity damping during migration, or
  - Migration halting shortly after resonant capture
- Secular evolution suggests an impulsive perturbation, e.g.,
  - Sudden halting of migration, or
  - Planet-Planet scattering after resonant capture
- Multiple planet systems are providing valuable information about history of planet formation

# Triggers for Dynamical Instability

- Dissipation of Protoplanetary Disk
- Mass Growth
- Secular Evolution
  - Multiple Planet Systems
  - **Wide Stellar Binary Companions**
- Migration
  - Convergent
  - Divergent crossing of Mean Motion resonances
- Distant Stellar Encounters

# Planet-Planet Scattering in a Binary



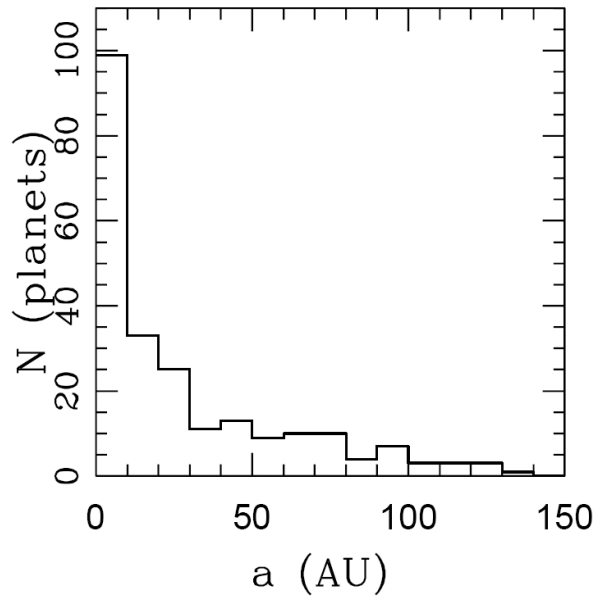
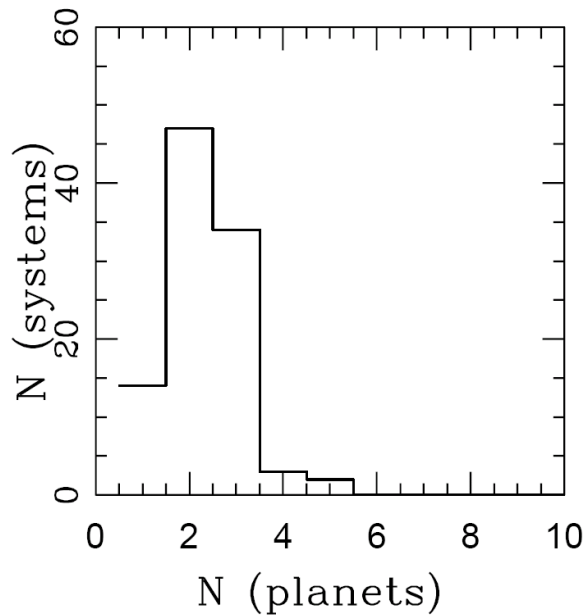
Marzari et al. 2005

Eccentricity

# Triggers for Dynamical Instability

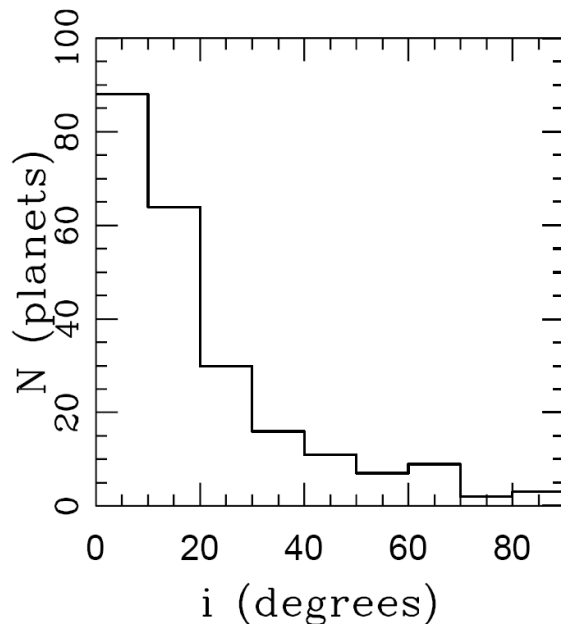
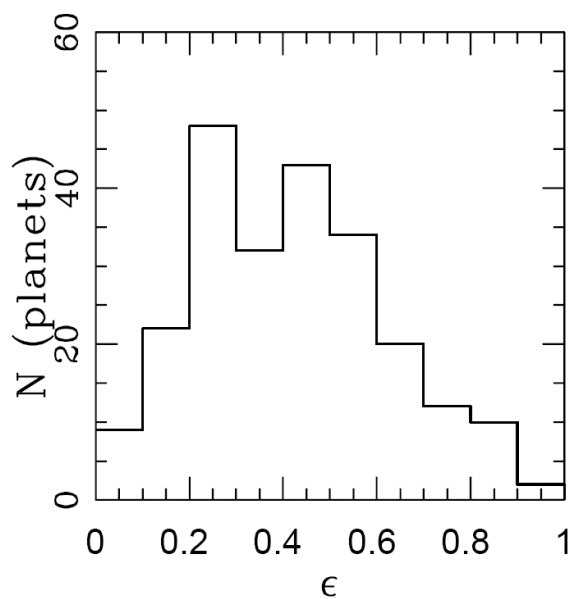
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- Mass Growth
- Secular Evolution
  - Multiple Planet Systems
  - Wide Stellar Binary Companions
- Migration
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# Dynamical Relaxation



- Many giant planets initially on nearly circular orbits

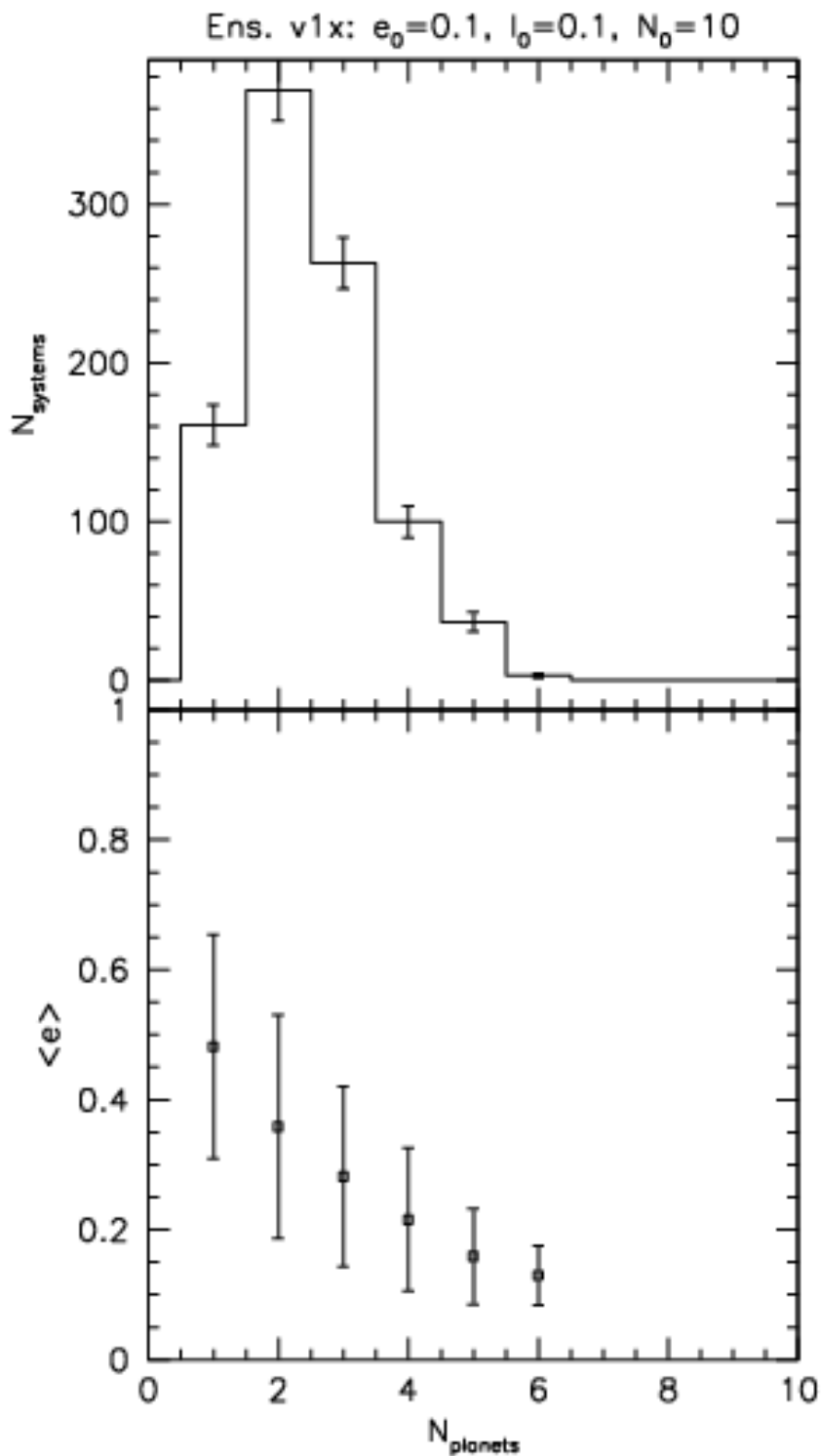
- Many planets removed from system



- Typically 2 or 3 giant planets remain on eccentric orbits

- Often one giant planet in a very wide orbit

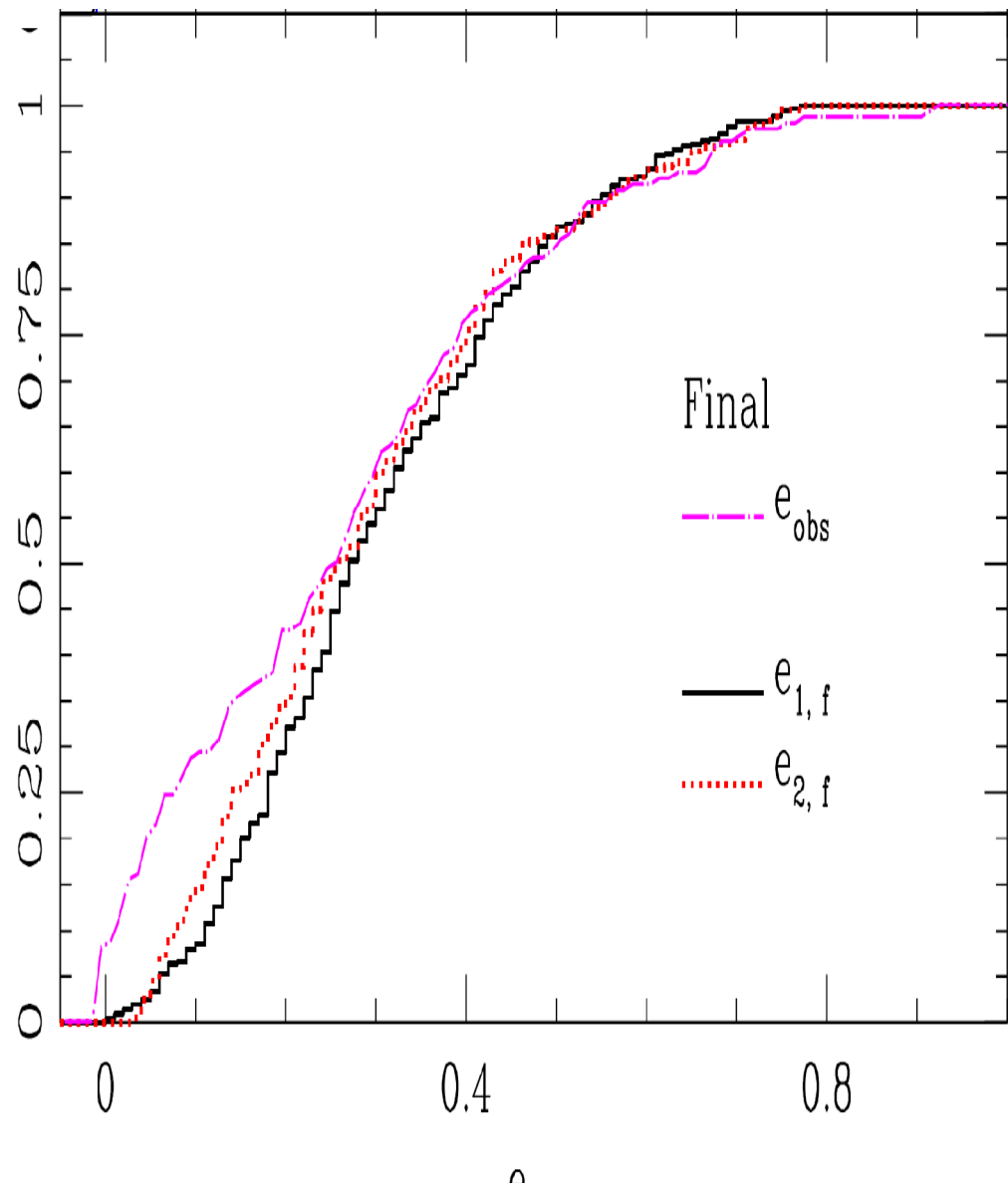
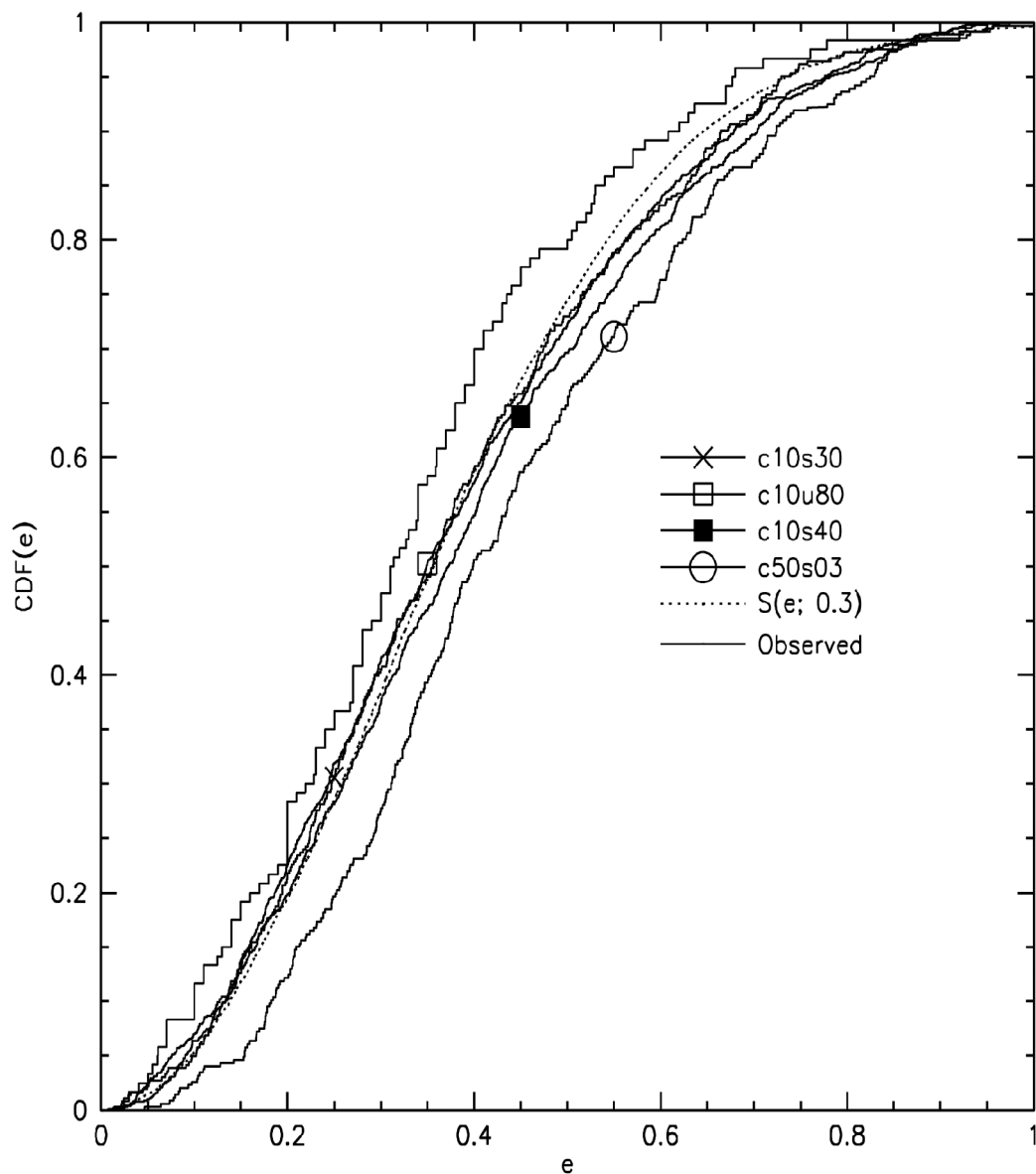




- mean eccentricity of surviving planets is correlated with number of surviving planets
- there are many high-eccentricity systems with 1 or 2 planets (the extrasolar planets?) and rare low-eccentricity systems with more planets (the solar system?)

(Juric & Tremaine 2007)

# Distribution of Eccentricities

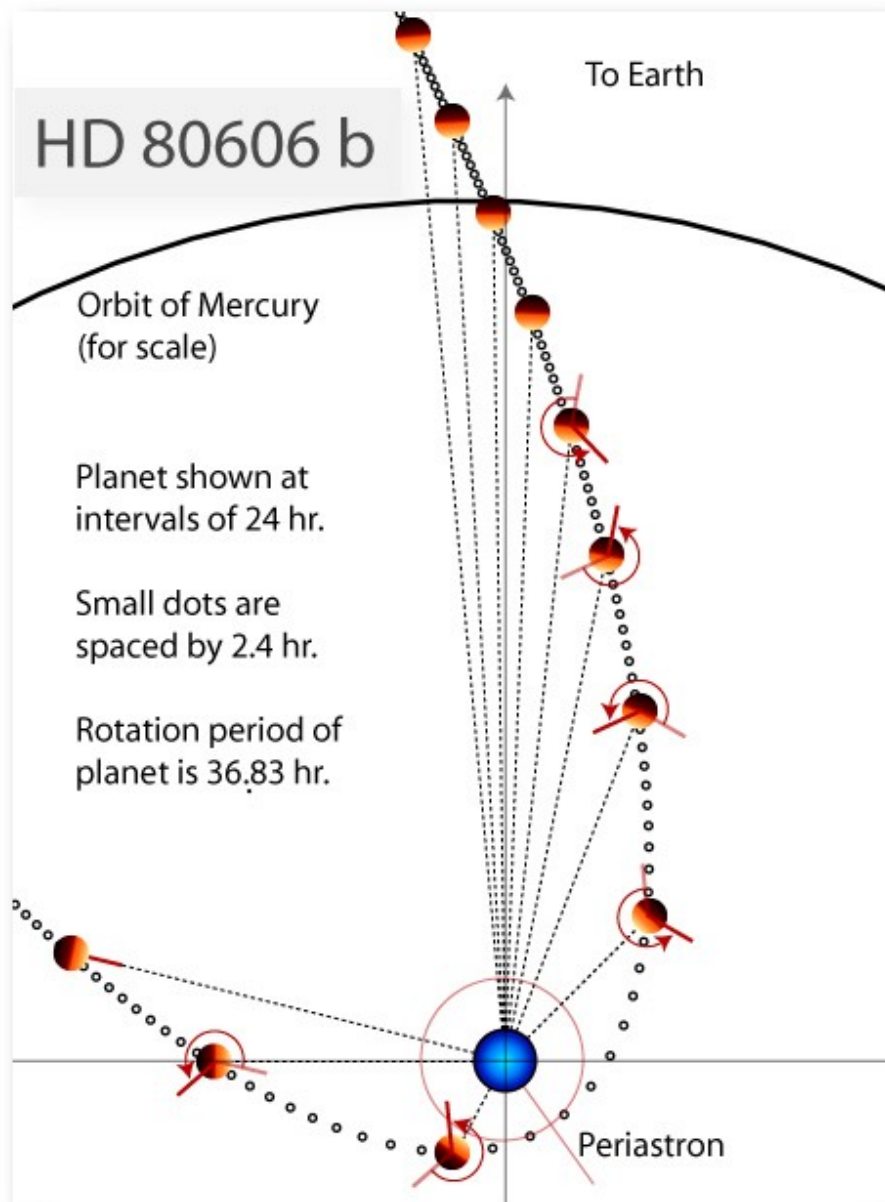
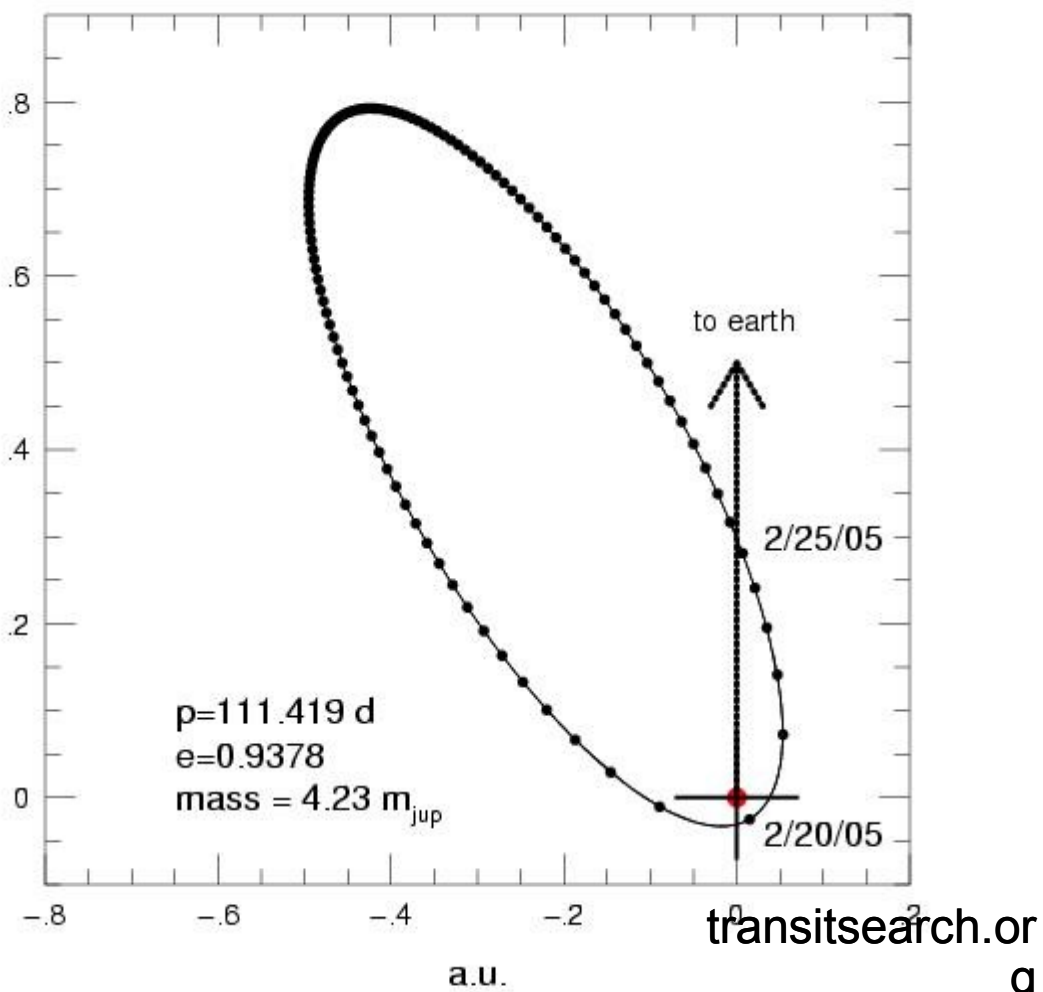


# Very Highly Eccentric Planets

## Highly Eccentric Planets

HD 80606b:  $e=0.94$ ,  $r_p = 0.03$  AU

HD 20782b:  $e=0.92$ ,  $r_p = 0.1$  AU



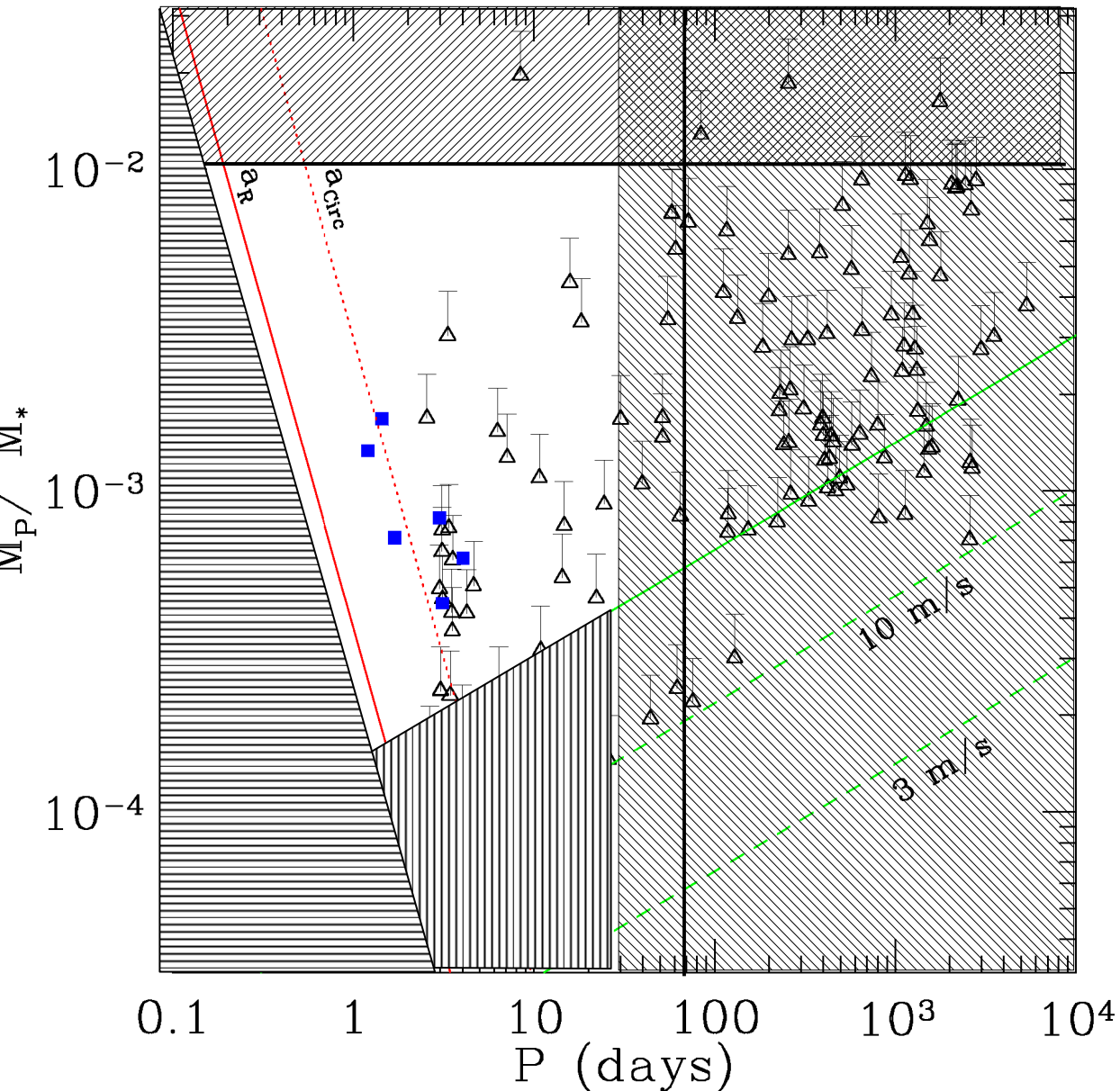
# Constraining Orbital Migration

- What causes hot-Jupiters to migrate?
- What halts migration? Survival?
- Clues from observed distribution of Hot Jupiters?
- Early pile-up of Hot Jupiters at  $P = 3d$
- Recent detections of planets with  $P < 3d$
- What is the theoretical limit for survival?

# Roche Limit & Migration

- Roche Limit ( $a_R$ ):  $R_P = 0.462a_R \left( \frac{M_P}{M_*} \right)^{1/3}$
- Theoretical limits on orbital migration:
  - Slow inspiral: Predicts edge at the Roche limit
    - Gaseous disk
    - Planetesimal scattering
  - Circularization of highly eccentric orbits with small pericenter distances: Predicts edge at *twice* the Roche limit
    - Planet-planet scattering
    - Tidal-capture of free-floating planets
    - Secular perturbations from highly inclined binary star

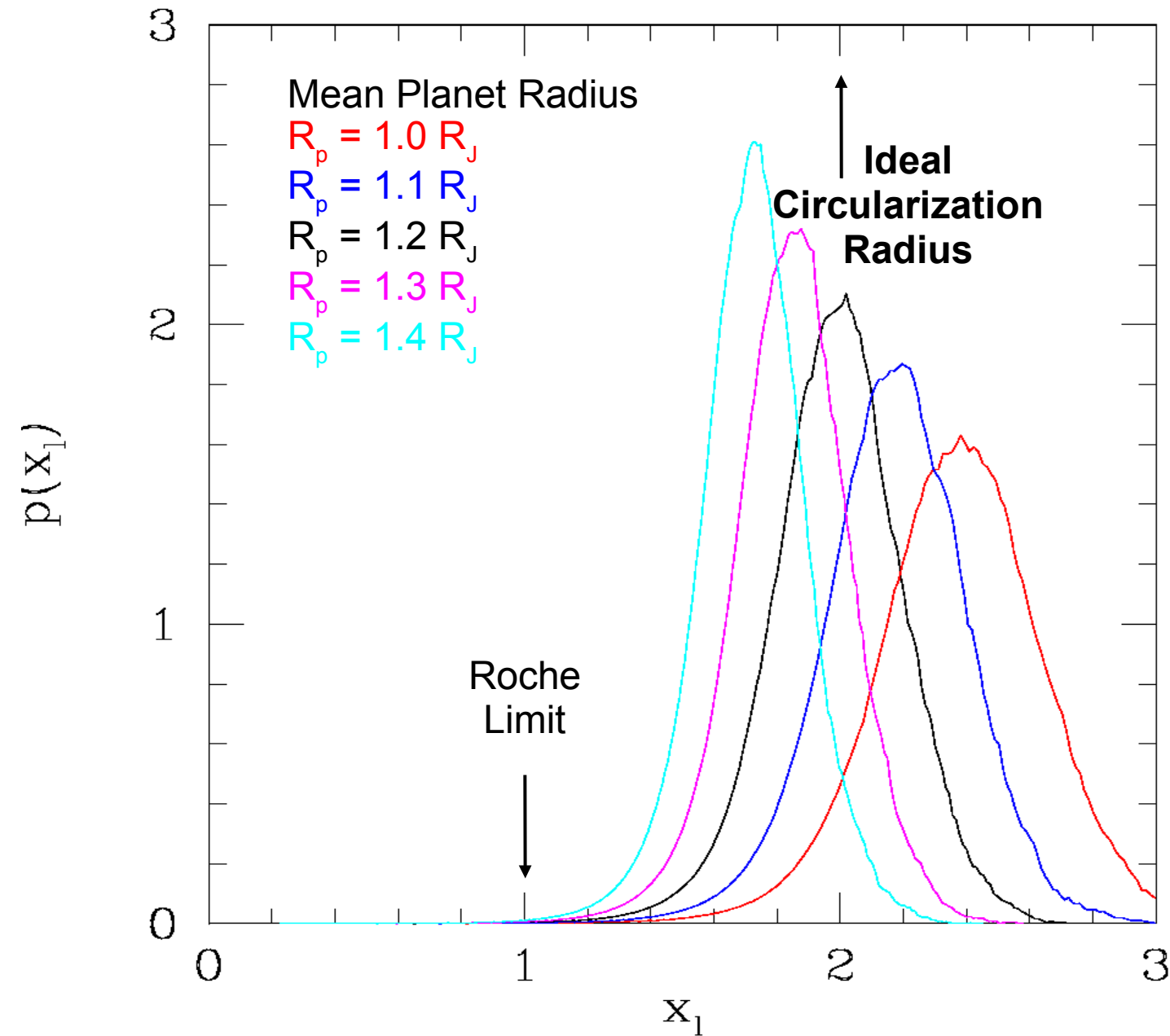
# Very Hot Jupiters



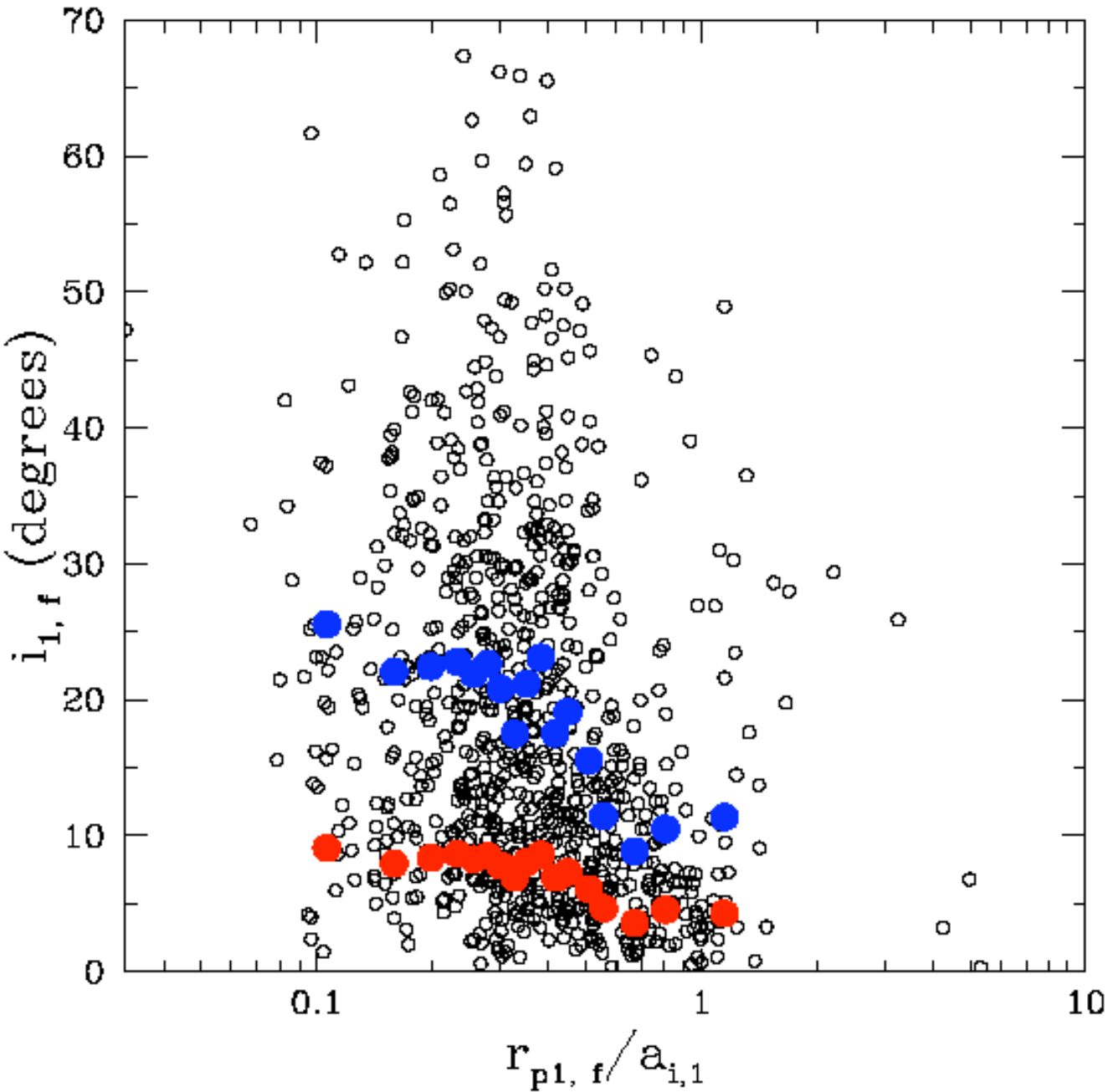
## Assumptions:

- Inner edge proportional to Roche limit
- Power law mass-period distribution with upper limit of  $m = 10 M_J$
- Complete RV survey for  $K > 30 \text{ m/s}$  &  $P < 30 \text{ d}$
- Transiting planets:  
Observed radii & inclinations
- Non-transiting planets  
Normal distribution for radii & isotropic orbits

# Location of Hot Jupiters' Inner Edge



# Planet Scattering & Orbital Migration

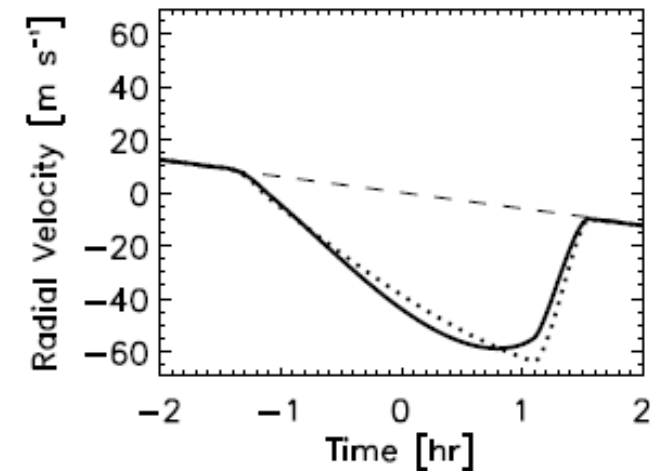
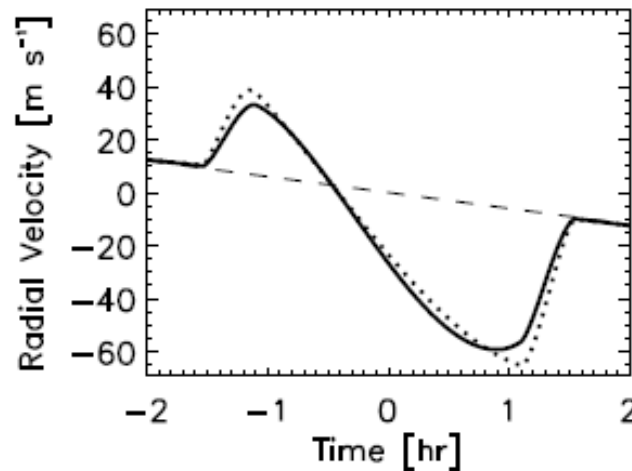
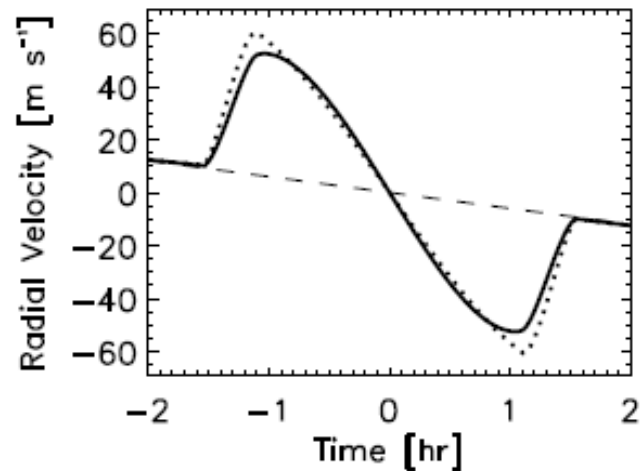
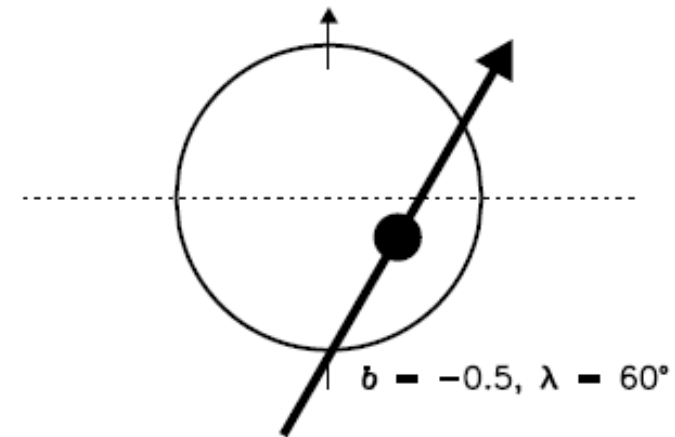
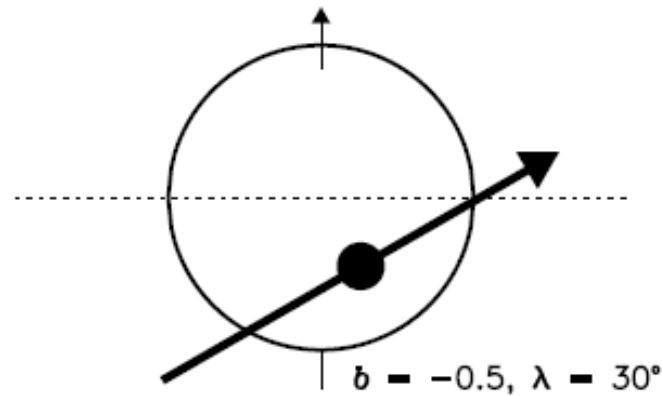
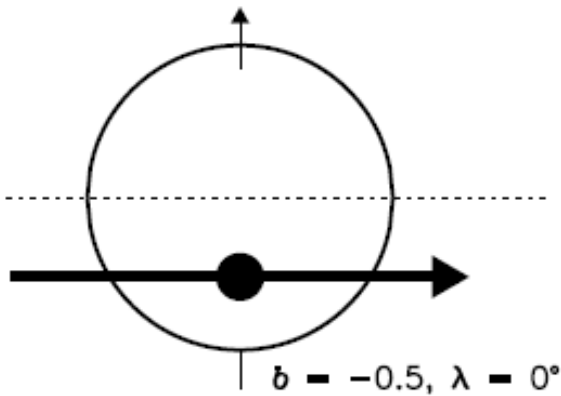


- Black: Final orbital elements from Individual simulations
- Blue: Mean final inner planet inclination
- Red: RMS final inner planet inclination



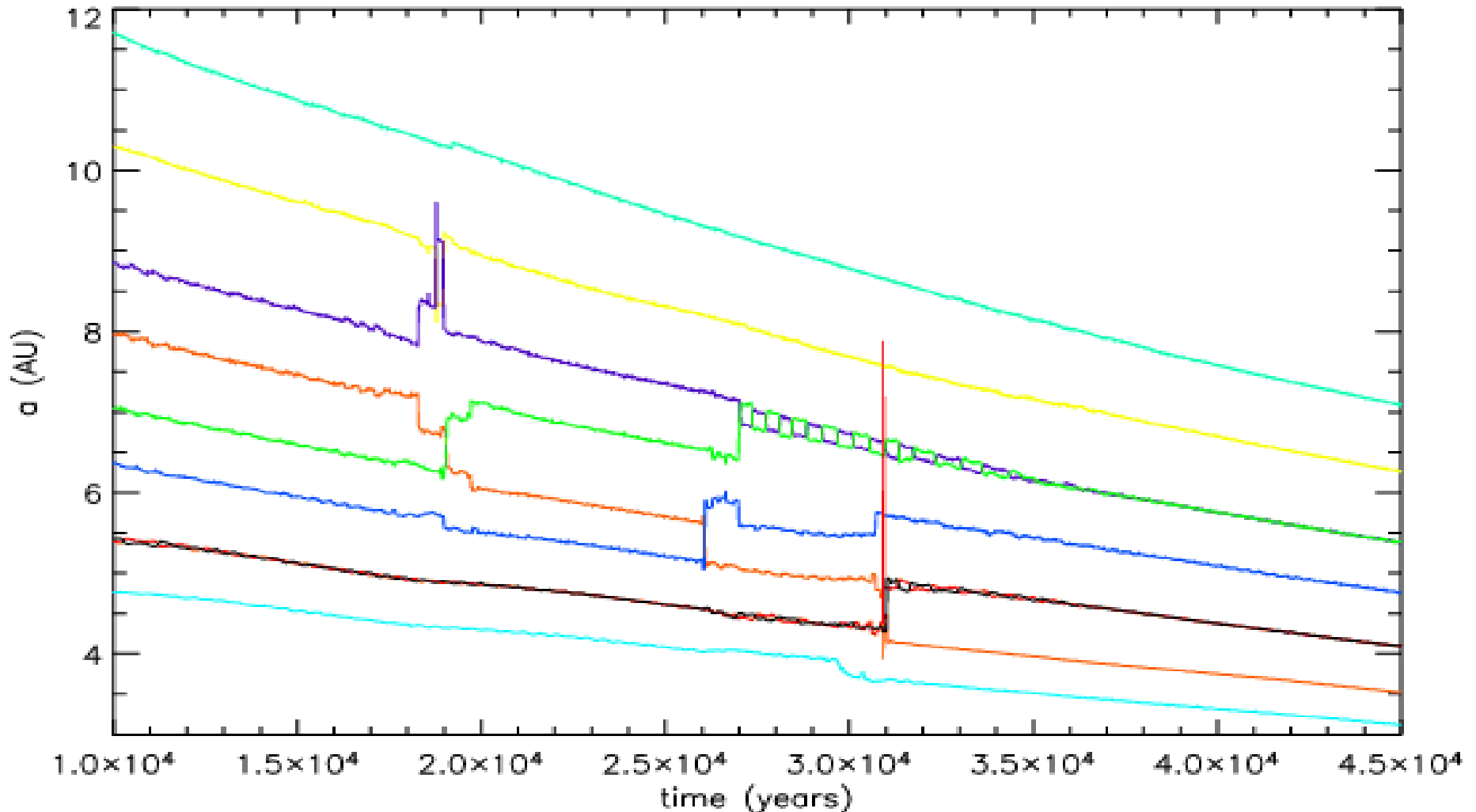
# Future Observational Tests

- Tidal dissipation in the planet rapidly damps eccentricity
- Search for planets with inclination excited by strong scattering



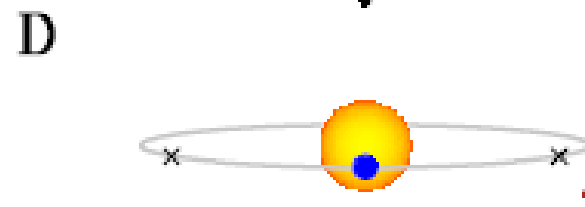
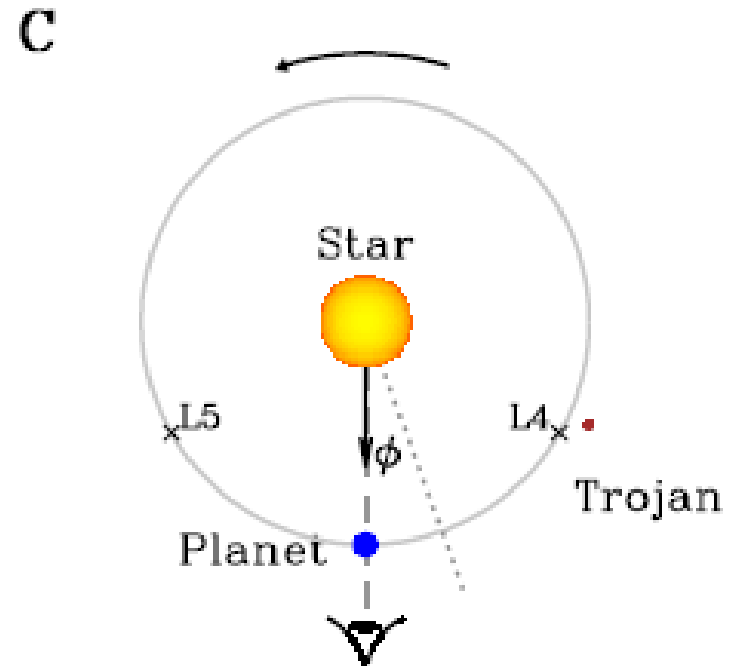
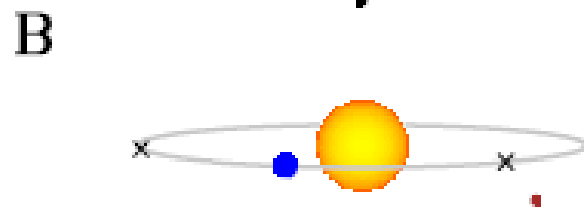
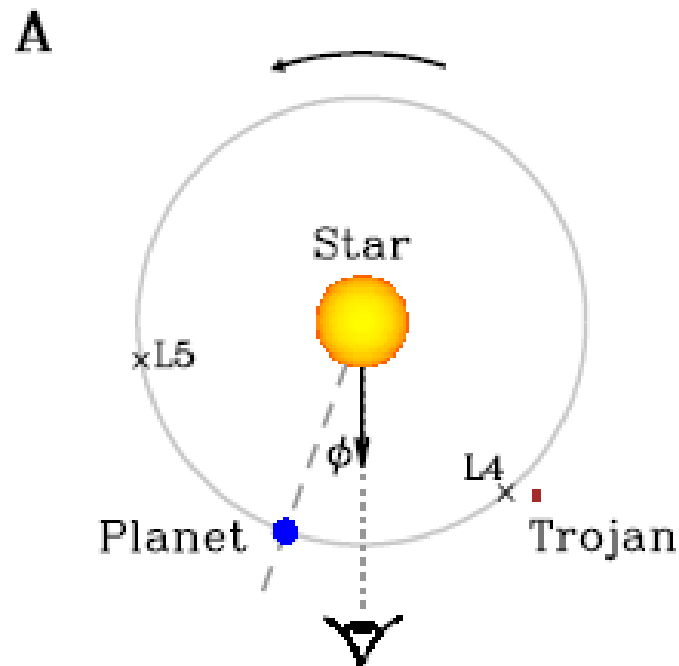
# Future Observational Tests

- Smooth migration can trap planets in resonances
- But planets in resonances can be hard to detect with RVs



# Future Observational Tests

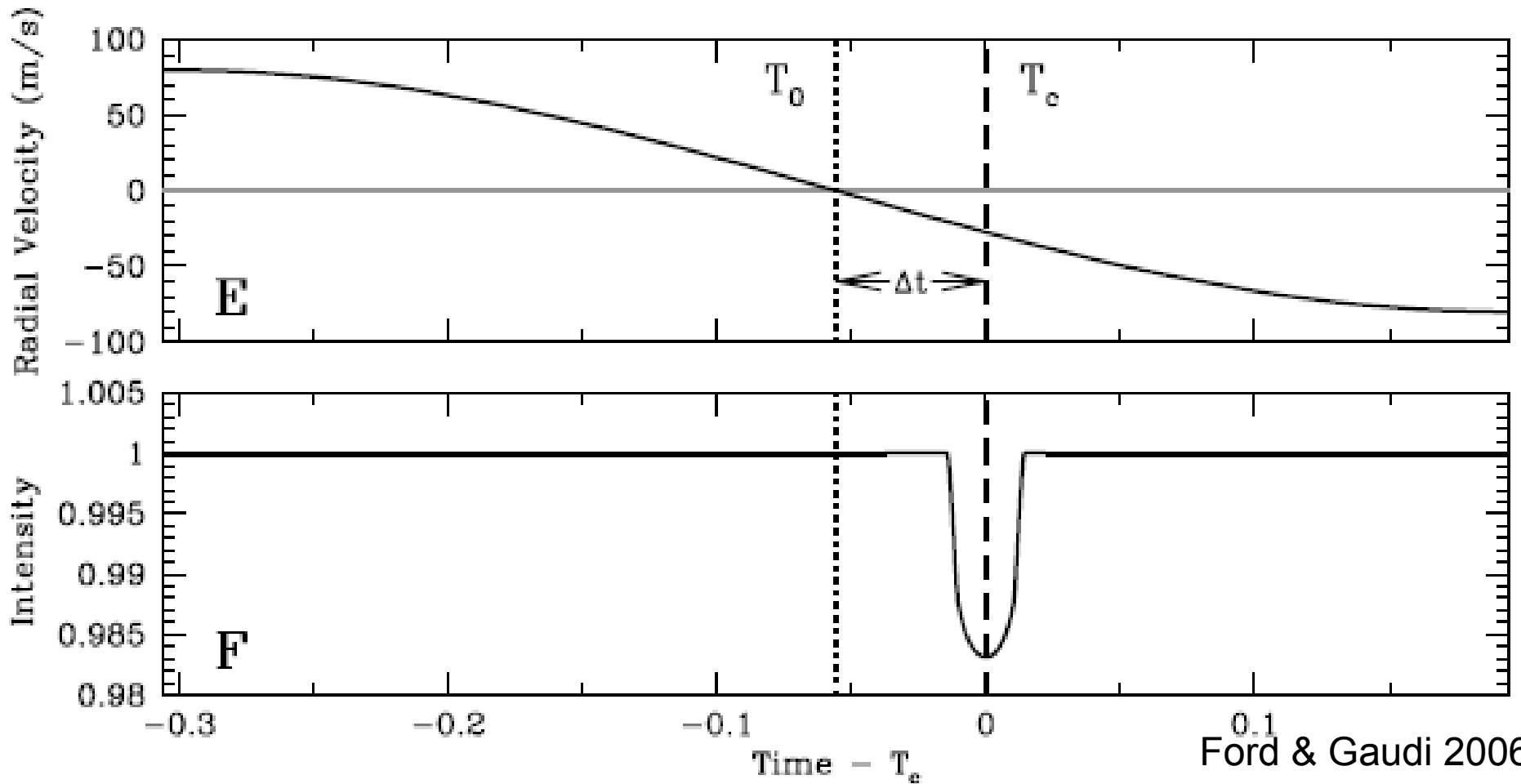
- Gravitational perturbations by another planet affect times of transit (Holman & Murray 2006; Agol et al. 2006)
- “Trojans” result in a constant time offset



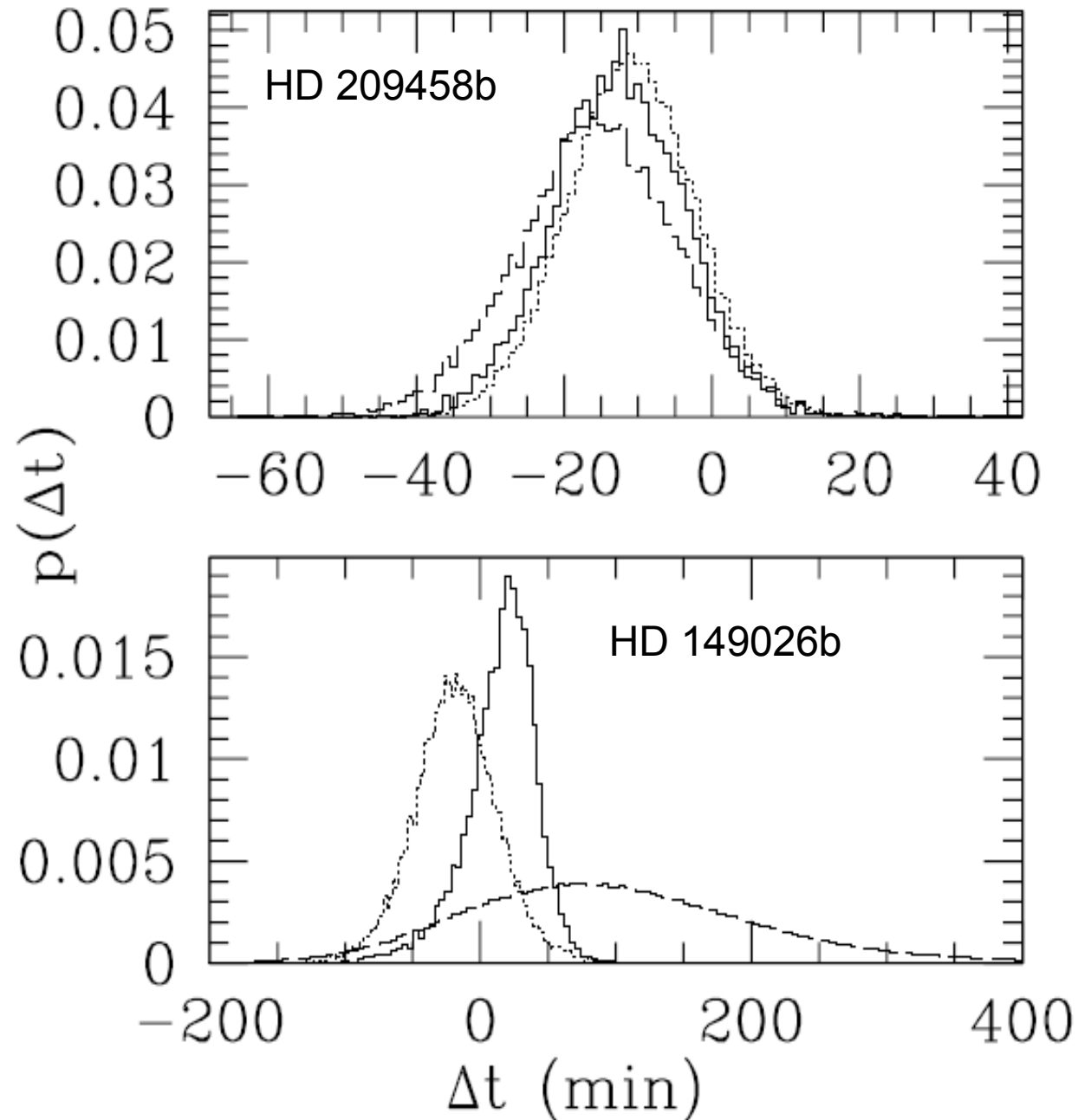
# Future Observational Tests

- Large constant offset between transit & RV null

$$\Delta t \simeq 37.5 \left( \frac{P}{3\text{d}} \right) \left( \frac{m_T}{10m_\oplus} \right) \left( \frac{0.5M_J}{m_p + m_T} \right) \text{min.}$$



# Existing Observational Constraints



Already significant upper limits for spin-orbit inclinations & masses of “Hot-Trojans”:

HD 209458b:

$m_{\text{Trojan}} < 13 M_{\oplus}$  (99.9%)

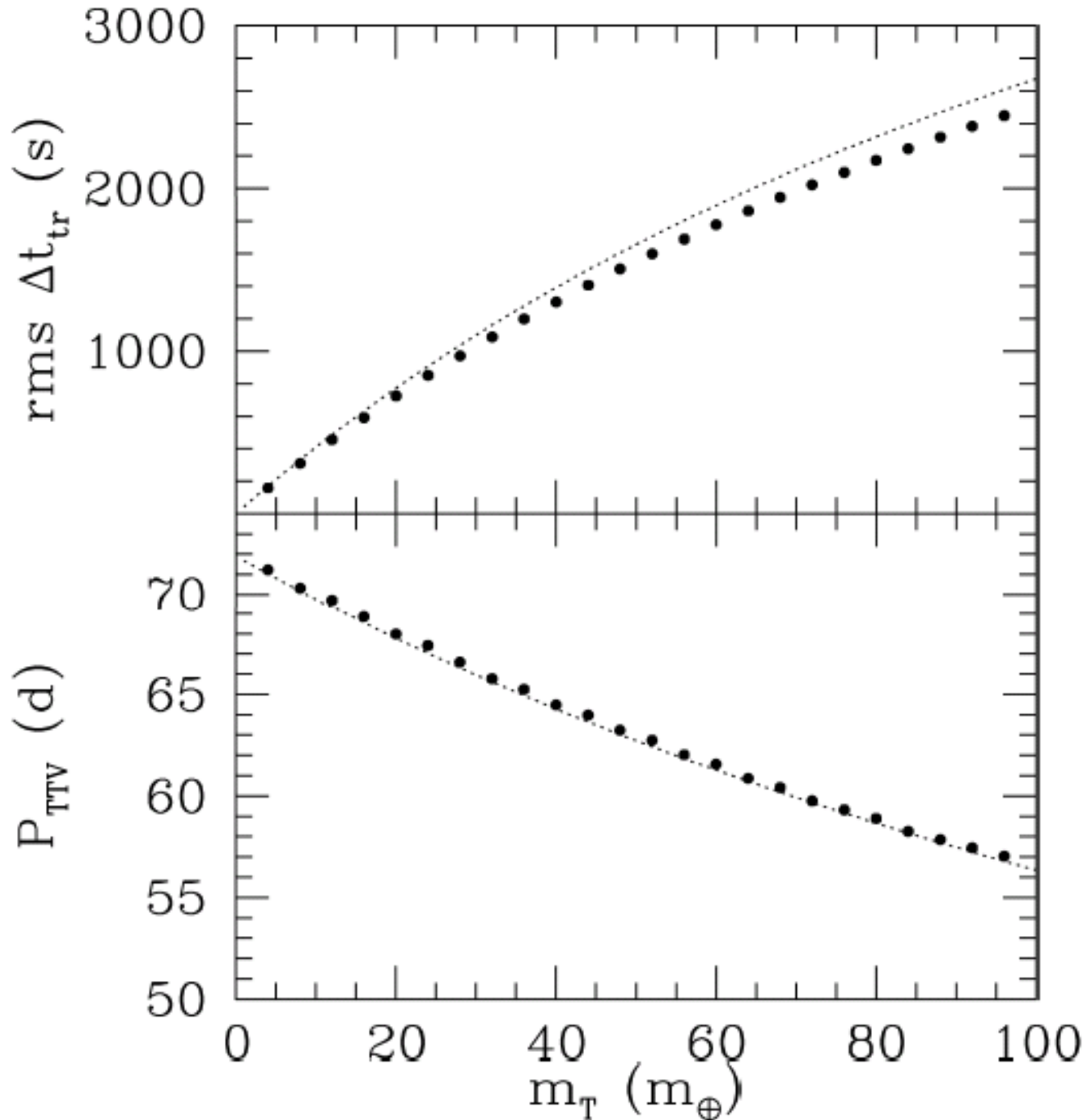
$i = 4.4^{\circ} \pm 1.4^{\circ}$  (Winn et al. 2005)

HD 149025b:

$m_{\text{Trojan}} < 25 M_{\oplus}$  (99.9%)

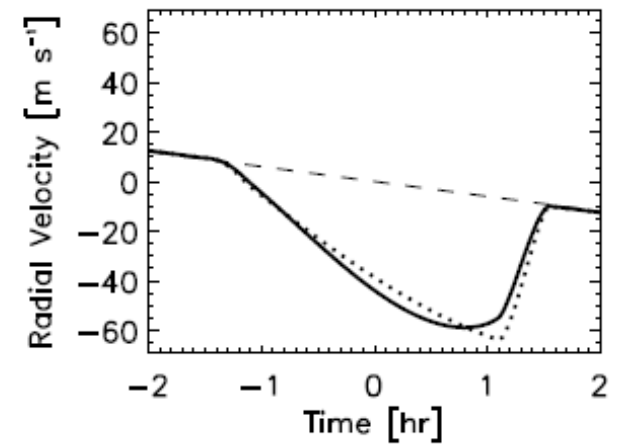
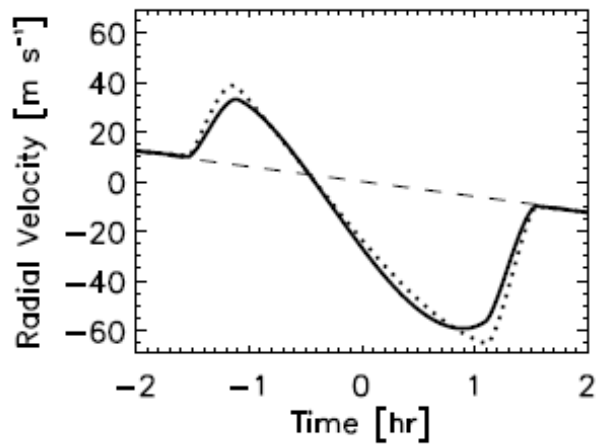
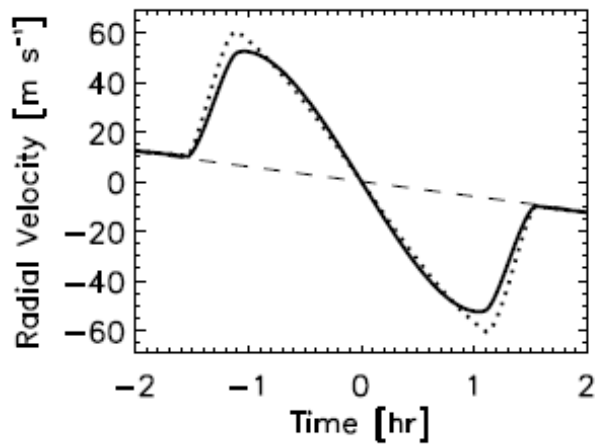
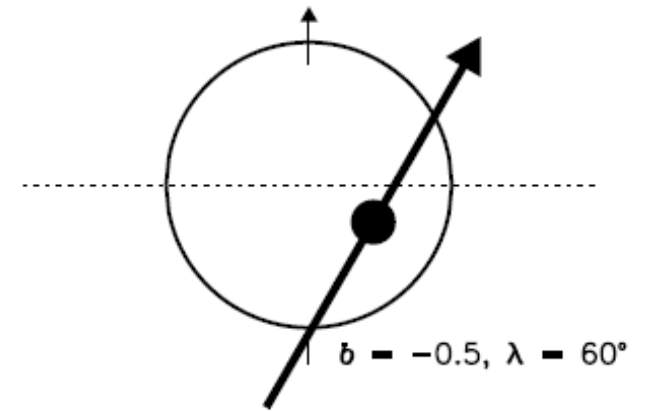
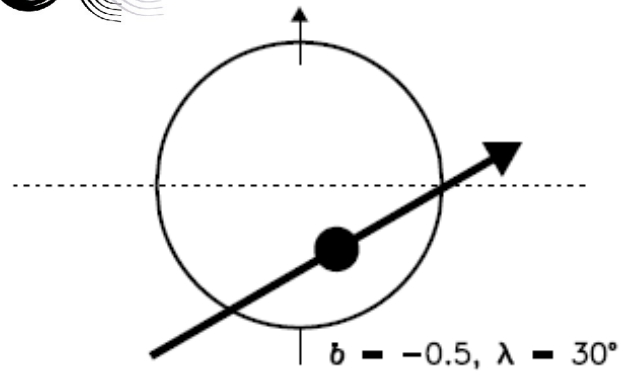
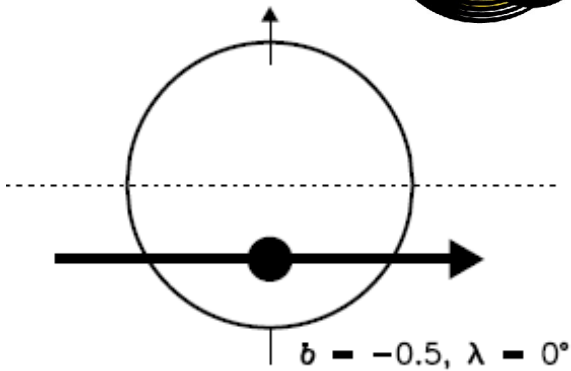
$i = 11^{\circ} \pm 14^{\circ}$  (Wolf et al. 2006)

# Transit Timing of Trojan Planets



- Transiting Giant Planet:  
Semimajor axis: 0.05AU  
Planet Mass:  $0.5 M_J$
- Trojan Planet:  
Libration:  $10^\circ$
- Earth-mass Trojan results in  $\sim 40s$
- Precision of transit time measurements  $\sim 10s$  (Holman et al. 2006)

# Transiting Planets



# Conclusions

- Many giant extrasolar planetary systems very different from our current solar system
- Our own solar system may have once contained giant planets on eccentric orbits
- Interactions of multiple planet systems can contain information about their orbital history
- Planet-planet scattering may frequent sculpt planetary systems
- Follow-up observations can search for additional planets and test orbital migration models